

## **Accelerated Design Optimization of Miniaturized Microwave Passives by Design Reusing and Kriging Interpolation Surrogates**

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### **Abstract**

Electromagnetic (EM) analysis has become ubiquitous in the design of microwave components and systems. One of the reasons is the increasing topological complexity of the circuits. Their reliable evaluation—at least at the design closure stage—can no longer be carried out using analytical or equivalent network representations. This is especially pertinent to miniaturized structures, where considerable EM cross-coupling effects occurring in densely arranged layouts affect the performance in a non-negligible manner. Although mandatory, EM-driven design is normally associated with significant computational expenses. Consequently, expediting the procedures that require massive simulations, such as parametric optimization, is a practical necessity. In this paper, a framework for accelerated parameter tuning is proposed. The keystones of our methodology are a set of pre-existing designs optimized for various design objectives, as well as kriging interpolation surrogates. The latter are constructed to yield—for a given set of performance specifications—a reasonably good starting point and to enable rapid optimization by providing the initial approximation of the Jacobian matrix of the circuit outputs. The proposed approach is validated using two compact impedance matching transformers designed within the objective spaces defined by wide ranges of operating bandwidths. As demonstrated, the average tuning cost corresponds to a few EM simulations of the respective circuit despite large numbers of adjustable parameters.

## 1. Introduction

It is a fact of the matter that full-wave electromagnetic (EM) simulation tools have become deeply rooted in the realm of microwave design [1]-[3]. While, in many cases, the initial designs can still be obtained through analytical considerations or from equivalent network models, it is virtually imperative for the majority of modern structures that the design closure (final adjustment of geometry parameters) is conducted at the level of EM models [4]-[6]. Miniaturized microwave components (couplers, power dividers, filters) belong to representative examples of circuits where EM-driven design is necessary due to considerable cross-coupling effects unaccountable by simpler models, e.g., equivalent networks [7]. At the same time, EM analysis may be computationally demanding which poses practical challenges when a large number of simulations are required. This is pertinent to local parameter adjustment [8] but even more to global search procedures [9]-[11] or uncertainty quantification [12]. A typically large number of parameters required to describe complex layouts of miniaturized components is an additional challenge. Furthermore, global optimization is often necessary due to difficulties in identifying reasonable initial designs for local optimization [13,14], which is yet another byproduct of topological complexity of modern microwave structures.

The aforementioned issues hinder the utilization of conventional optimization algorithms in a large number of practical situations. Hence, the extensive research oriented towards improving the computational efficiency of simulation-based design procedures is by no means a surprise. Among the various techniques developed over the recent years, several categories of methods are worth noting. These include surrogate-assisted algorithms involving physics-based models (space mapping [15], response

correction methods [16], feature-based optimization [17]), along with optimization frameworks employing data-driven surrogates (kriging [11], artificial neural networks [18], Gaussian process regression [19], or polynomial chaos expansion [20]). Another approaches comprise gradient-based algorithms accelerated through adjoint sensitivities [21], [22], or implementing sparse sensitivity updates [23], [24], as well as machine learning approaches (most often utilized in the context of global optimization [25]). Each of these techniques exhibit specific advantages but also limitations. Physics-based surrogates, for that matter, feature excellent generalization (i.e., the ability to render reliable predictions about the high-fidelity model outputs using a small number of training samples) yet their construction requires appropriate low-fidelity models. The latter are problem specific, may not be always available, or not sufficiently reliable. In juxtaposition to this, data-driven models are more flexible and easily transferrable between application domains but they are strongly affected by the curse of dimensionality. This is a serious drawback from the point of view of high-frequency design as a typical microwave device outputs are highly nonlinear [26].

The algorithmic means of alleviating the high cost issue outlined in the previous paragraph generally assume that the design process (e.g., parameter tuning) starts from scratch every time it is executed, with the initial design often obtained through theoretical considerations or parameter sweeping. On the other hand, computational savings can be achieved by incorporating the already existing data, e.g., in the form of previous designs obtained for various sets of performance specifications. Design curves are perhaps the earliest and the simplest examples of this sort of approach [27]-[29]. Recently, the employment of the inverse surrogate models has been fostered in this context [30], also in

variable-fidelity simulation setup [31], as well as supplemented by the iterative correction schemes [32]. Regardless of a particular implementation, the employment of already available information seems to be a potentially attractive way of speeding up the design process.

This paper proposes a surrogate-assisted procedure for expediting the design closure of miniaturized microwave passives. The keystone of the presented approach is an incorporation of the existing designs in the form of two kriging interpolation models, one for yielding a reasonable initial design, and the other to provide an estimation of the system response sensitivities. The latter permits a jump-start of the design refinement process, here, implemented within the trust-region gradient search with Jacobian updates based on the rank-one Broyden formula. Comprehensive verification involving two impedance matching transformers demonstrates the efficacy of the framework with the optimized designs rendered at the cost of a few EM analyses of the respective structure. For both circuits, the optimization process is carried out over wide ranges of operating conditions without the necessity of providing any initial point, which shows a quasi-global search capability while employing local optimizers only.

## **2. Optimization with Design Reusing**

In this section, we delineate the proposed framework for accelerated design optimization of microwave passives by design reusing. Our methodology involves exploitation of pre-optimized reference designs in order to develop kriging surrogates for the two following purposes: (i) identification of a good quality initial design, and (ii) expediting the optimization (design refinement) procedure.

## 2.1. Figures of Interest and Database Designs

The proposed methodology assumes the existence of a database comprising the reference designs optimized for the chosen values of design objectives. The required number of such designs is normally small (e.g., a few). Let  $X$  refer to the parameter space of tunable variables of the microwave component under design, and let  $F$  represent the objective space of performance figures such as a required operating frequency (or frequencies in the case of multi-band structures), bandwidth, power split ratio (in the case of couplers/dividers) or material parameters (e.g., permittivity or height of the substrate used to realize the structure). The performance figure vector  $\mathbf{F} = [F_1 \dots F_N]^T \in F$  represents the aggregated design specifications. The aforementioned reference designs  $\mathbf{x}_b^{(j)}, j = 1, \dots, p$ , are optimized for the objective vectors  $\mathbf{F}^{(j)} = [F_1^{(j)} \dots F_N^{(j)}]^T$  by solving

$$\mathbf{x}^* = \arg \min_{\mathbf{x}} U(\mathbf{R}(\mathbf{x}), \mathbf{F}) \quad (1)$$

where  $\mathbf{R}(\mathbf{x})$  denotes the EM-simulated response of the component, e.g., the scattering parameters versus frequency;  $\mathbf{x} = [x_1 \dots x_n]^T \in X$ , and  $U$  refers to the scalar cost function. For the sake of brevity, the design optimized in the sense of (1) with  $\mathbf{F}$  being a target vector will be referred to as  $U_F(\mathbf{F})$ . In particular, the  $j$ th reference design of the design database will be denoted as  $\mathbf{x}_b^{(j)} = U_F(\mathbf{F}^{(j)})$ . The vectors  $\mathbf{F}^{(j)}$  may be arbitrarily allocated within the objective space  $F$ , although uniform distribution is preferred. The space  $F$  itself is defined as an  $N$ -dimensional interval delimited by the intended ranges of the figures of interest, i.e.,  $F_{k,\min} \leq F_k \leq F_{k,\max}$ . These ranges determine the region of validity of the proposed framework. The database designs may either be acquired during prior work with the structure in question or pre-optimized especially for the purposes of setting up the optimization procedure. In addition, let the Jacobian matrices of the component

response at  $\mathbf{x}_b^{(j)}$  be denoted as  $\mathbf{J}_b^{(j)} = \mathbf{J}(\mathbf{x}_b^{(j)})$ ,  $j = 1, \dots, p$ . The sensitivity data is normally obtained as an additional outcome of solving (1).

In order to explain the above mentioned concepts, let us consider a filter designed to minimize  $|S_{11}|$  within the operating band defined by the center frequency  $f_0$  and the fractional bandwidth  $B$ . Hence, we have a two-objective space  $F$ :  $F_1 = f_0$  and  $F_2 = B$ . In this case, the following objective function  $U$  might be employed  $U(\mathbf{R}(\mathbf{x}), \mathbf{F}) = \max\{F_1(1 - F_2/2) \leq f \leq F_1(1 + F_2/2) : |S_{11}(\mathbf{x}, f)|\}$ .

## 2.2. Kriging Surrogates

In the proposed framework, the two following kriging [33] surrogates are constructed based on the set of database designs:

- $s_x: F \rightarrow X$ , configured from the pairs  $\{\mathbf{F}^{(j)}, \mathbf{x}_b^{(j)}\}_{j=1, \dots, p}$ ;
- $s_J(\cdot): F \rightarrow X \times \dots \times X$  ( $m$ -times Cartesian product of  $X$ , with where  $m$  refers to the dimension of the component response vector  $\mathbf{R}(\cdot)$ ), constructed from the data set  $\{\mathbf{F}^{(j)}, \mathbf{J}_b^{(j)}\}_{j=1, \dots, p}$ .

The output of the model  $s_x(\mathbf{F})$  approximates the design optimized with respect to the performance figure vector  $\mathbf{F}$ . Thus,  $s_x$  is an inverse surrogate. The model  $s_J$  provides approximation of the component response sensitivities at the design produced by  $s_x$ . A graphical illustration of the relationship between the kriging models and the objective space has been shown in Fig. 1.

### 2.3. Initial Design

The inverse model  $s_x$  delivers the best available approximation of the optimum design set  $U_F(F)$  that can be obtained based on the reference designs  $\mathbf{x}_b^{(j)} = U_F(\mathbf{F}^{(j)})$ ,  $j = 1, \dots, p$ . In particular, the initial estimate of the design  $U_F(\mathbf{F}_t)$  optimum with respect to a target vector  $\mathbf{F}_t \in F$  may be found as

$$\mathbf{x}^{(0)} = s_x(\mathbf{F}_t) \quad (2)$$

Additionally, an approximation of the Jacobian matrix of the component responses at  $\mathbf{x}^{(0)}$  is provided by the second surrogate  $s_J$  as

$$\mathbf{J}^{(0)} = s_J(\mathbf{F}_t) \quad (3)$$

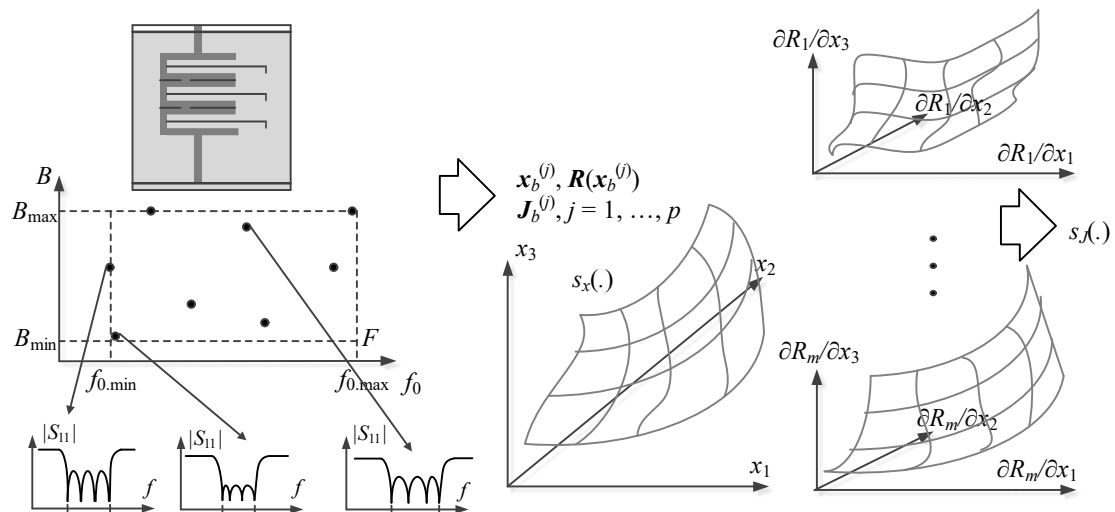


Fig. 1. Graphical illustration of the objective space (delimited by the lower and upper bounds on the center frequency  $f_0$  and the fractional bandwidth  $B$ ) for a fourth-order bandpass filter presented at the top, along with exemplary filter responses optimized for the selected bandwidths that correspond to the objective vectors from the objective space  $F$  (left panel). The surrogates  $s_x$  and  $s_J$  (right panel) are set up with the use of the database designs (black circles) and corresponding filter responses along with their sensitivities.

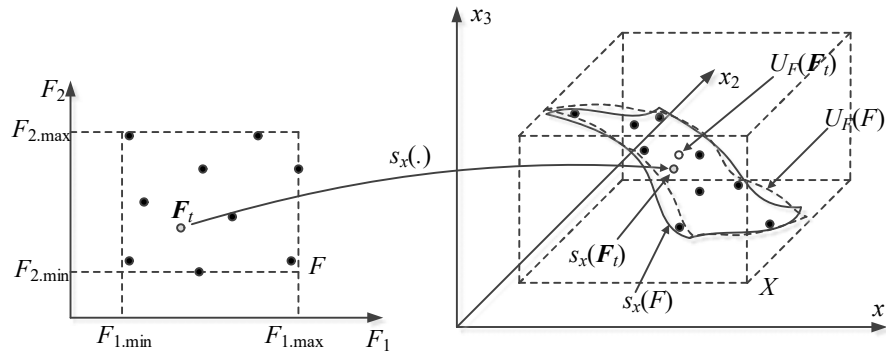


Fig. 2. Conceptual illustration of the image  $s_x(F)$  (solid lines) of the objective space  $F$ , along with the optimum design manifold  $U_F(F)$  (dashed lines). The exemplary initial design  $s_x(F_t)$  (gray-shaded circle) corresponds to the target vector  $F_t$ . The surrogate  $s_x(\cdot)$  is constructed based on the reference designs (black circles). The true optimum design  $U_F(F_t)$  (white-shaded circle) differs from  $s_x(F_t)$  because  $s_x(F)$  merely approximates  $U_F(F)$ .

The above concepts are illustrated graphically in Fig. 2. The initial design  $\mathbf{x}^{(0)}$ , established using (2), is only an approximation of  $U_F(F_t)$ , and its quality is determined, among others, by the number of the database designs and the nonlinearity of the component response. Hence, it needs to be further refined which is carried out with the use of a trust-region (TR) gradient search algorithm [34].

The TR algorithm is an iterative procedure that produces a series of approximations  $\mathbf{x}^{(i)}$ ,  $i = 0, 1, \dots$ , to  $\mathbf{x}^* = U_F(F_t)$  by solving subproblems

$$\mathbf{x}^{(i+1)} = \arg \min_{\mathbf{x}; -d^{(i)} \leq \mathbf{x} - \mathbf{x}^{(i)} \leq d^{(i)}} U(\mathbf{G}^{(i)}(\mathbf{x}), F_t) \quad (4)$$

where  $\mathbf{G}^{(i)}(\mathbf{x})$  is a first-order Taylor expansion of  $\mathbf{R}$

$$\mathbf{G}^{(i)}(\mathbf{x}) = \mathbf{R}(\mathbf{x}^{(i)}) + \mathbf{J}_R(\mathbf{x}^{(i)}) \cdot (\mathbf{x} - \mathbf{x}^{(i)}) \quad (5)$$

Usually, the Jacobian  $\mathbf{J}_R$  is updated in each algorithm iteration through computationally expensive finite differentiation (FD), at the cost of  $n$  additional EM simulations of the device at hand. By exploiting the fact that the initial design (2) is typically good, a reduction of the computational overhead associated with solving (4) can be attained



through updating the Jacobian  $\mathbf{J}_R$  in consecutive iterations with the use of the Broyden formula [34] rather than FD. In addition, in the first iteration, the Jacobian is jump-started with  $s_J(\mathbf{F}_1)$  yielded by the forward model  $s_J$ . As a consequence, the cost of the optimization process is significantly reduced to no more than a few EM analyses of the component under design.

### 3. Verification Case Studies

In this section, numerical validation of the methodology of Section 2.3 is provided using the three- and four-section impedance matching transformers described by fifteen and twenty geometry parameters, respectively. The results confirm the ability of the proposed framework to deliver high quality designs satisfying assumed target specifications at a low computational cost.

#### 3.1. Benchmark structures

The verification structures are two compact impedance matching transformers shown in Fig. 3(b) and (c). The circuits are composed of compact microstrip resonant cells (CMRCs) shown in Fig. 3(a). Both transformers are implemented on a 0.762-mm-thick Taconic RF35 substrate ( $\epsilon_r = 3.5$ ). The geometry parameters are presented in Table 1. The three-section transformer has been optimized for various operating bands  $[f_1 f_2]$  within the ranges  $1.5 \text{ GHz} \leq f_1 \leq 3.5 \text{ GHz}$ , and  $4.5 \text{ GHz} \leq f_2 \leq 6.5 \text{ GHz}$ . Here, the optimum design minimizes the maximum of the reflection  $|S_{11}|$  within  $[f_1 f_2]$ . Whereas in the case of the four-section transformer the region of interest is defined by  $1.5 \text{ GHz} \leq f_1 \leq 3.5 \text{ GHz}$ , and  $5.5 \text{ GHz} \leq f_2 \leq 6.5 \text{ GHz}$ .

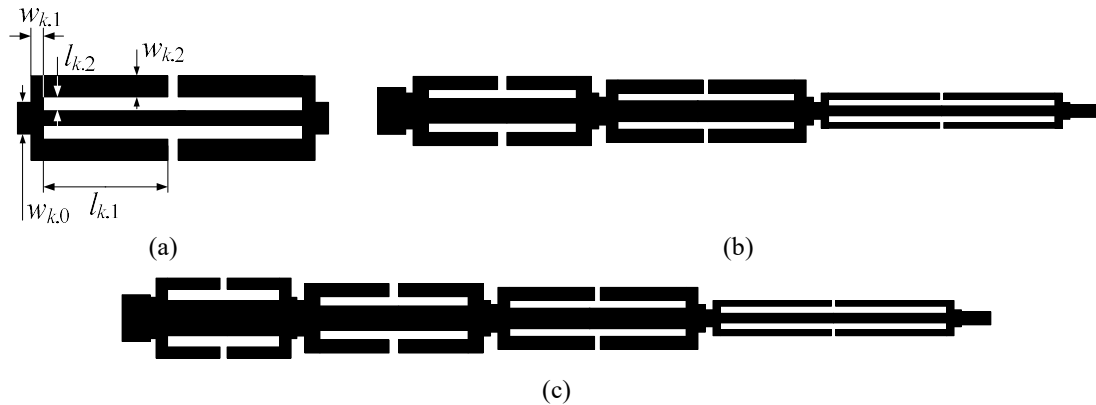


Fig. 3. Verification test cases: (a) CMRC cell, (b) and (c) CMRC-based miniaturized three- and four-section impedance matching transformers, respectively.

Table 1. Geometry Parameters of the Three- and Four Section Impedance Transformers

Circuit	Geometry Parameters
3-section	$[l_{1,1} \ l_{1,2} \ w_{1,1} \ w_{1,2} \ w_{1,0} \ l_{2,1} \ l_{2,2} \ w_{2,1} \ w_{2,2} \ w_{2,0} \ l_{3,1} \ l_{3,2} \ w_{3,1} \ w_{3,2} \ w_{3,0}]^T$
4-section	$[l_{1,1} \ l_{1,2} \ w_{1,1} \ w_{1,2} \ w_{1,0} \ l_{2,1} \ l_{2,2} \ w_{2,1} \ w_{2,2} \ w_{2,0} \ l_{3,1} \ l_{3,2} \ w_{3,1} \ w_{3,2} \ w_{3,0} \ l_{4,1} \ l_{4,2} \ w_{4,1} \ w_{4,2} \ w_{4,0}]^T$

In the case of the three-section transformer, five reference designs  $\mathbf{x}_b^{(j)}$ , corresponding to the pairs  $\{f_1, f_2\}$ :  $\{1.5, 4.5\}$ ,  $\{1.5, 6.5\}$ ,  $\{2.5, 5.5\}$ ,  $\{3.5, 4.5\}$ , and  $\{3.5, 6.5\}$  (frequencies in GHz), have been used. For the four-section transformer, the number of the reference designs was nine, representing the following operational bandwidths:  $\{1.5, 5.5\}$ ,  $\{1.5, 6.5\}$ ,  $\{1.5, 7.5\}$ ,  $\{2.5, 5.5\}$ ,  $\{2.5, 6.5\}$ ,  $\{2.5, 7.5\}$ ,  $\{3.5, 5.5\}$ ,  $\{3.5, 6.5\}$ , and  $\{3.5, 7.5\}$  (frequencies in GHz). It should be emphasized that the design optimization tasks are challenging due to a small number of the reference designs but also high dimensionality of the parameter spaces.

Tables 2 and 3 gather the numerical results obtained by optimizing the three- and four-section transformers, respectively, for the target performance vectors selected for

validation purposes. Figures 4 and 5, respectively, show the components responses at the initial designs (obtained using (2)), as well as the final designs yielded by solving (4), (5). The average computational cost of the optimization process does not exceed eight EM simulations of the transformer circuit (in the case of three-section transformer) and for four-section transformer the computational overhead is as low as nine EM simulations.

### 3.2. Discussion

The initial designs, yielded by the first-level (inverse) surrogate (cf. (2)), are of high quality for all verification cases and for both transformers. Employing TR algorithm (4) and (5) permits further design improvement for the majority of the cases.

Table 2. Optimization Results for Three-Section Impedance Transformer

Test case		1	2	3	4	5	6
Target operating band	$f_1$ [GHz]	2.0	1.8	2.7	2.7	3.5	2.8
	$f_2$ [GHz]	5.0	6.0	5.2	5.8	6.0	4.9
Geometry parameters [mm]	$l_{1,1}$	2.94	2.82	2.57	2.42	2.17	2.56
	$l_{1,2}$	0.34	0.15	0.29	0.35	0.33	0.38
	$w_{1,1}$	0.75	0.80	0.79	0.80	0.81	0.76
	$w_{1,2}$	0.51	0.47	0.54	0.55	0.52	0.54
	$w_{1,0}$	1.25	0.86	1.14	0.61	0.76	1.26
	$l_{2,1}$	3.57	3.38	3.42	3.44	3.06	3.33
	$l_{2,2}$	0.35	0.15	0.18	0.23	0.16	0.30
	$w_{2,1}$	0.54	0.68	0.52	0.66	0.62	0.52
	$w_{2,2}$	0.27	0.15	0.32	0.15	0.24	0.34
	$w_{2,0}$	0.83	0.32	0.99	0.36	0.81	1.03
	$l_{3,1}$	4.07	3.94	3.80	3.58	3.35	3.85
	$l_{3,2}$	0.22	0.15	0.15	0.15	0.14	0.18
	$w_{3,1}$	0.35	0.46	0.34	0.37	0.37	0.33
	$w_{3,2}$	0.20	0.15	0.17	0.15	0.15	0.20
$w_{3,0}$	0.59	1.00	0.66	0.60	0.55	0.51	

For the three-section transformer, in one occurrence (cf. Fig. 4(e)), the initial design characterized by a very low in-band reflection has not been altered by (4). This was due to the presence of numerical noise in EM simulations results that hinders the gradient search based on approximated sensitivity data. In the case of four-section transformer, the initial designs produced by (2) are of good quality for all considered cases. Also, for all target operating bands, the gradient-based refinement (4) brings visible improvement.

Table 3. Optimization Results for Four-Section Impedance Transformer

Test case	1	2	3	4	5	6	
Target operating band	$f_1$ [GHz]	1.8	2.0	2.2	2.2	2.4	2.8
	$f_2$ [GHz]	5.8	7.5	5.8	6.4	7.0	6.3
Geometry parameters [mm]	$l_{1.1}$	3.14	2.30	2.70	2.69	2.35	2.31
	$l_{1.2}$	0.12	0.24	0.10	0.15	0.25	0.14
	$w_{1.1}$	0.99	0.96	1.00	1.00	0.98	0.98
	$w_{1.2}$	0.42	0.34	0.43	0.40	0.38	0.46
	$w_{1.0}$	0.32	0.46	0.45	0.63	0.50	0.81
	$l_{2.1}$	3.84	3.27	3.70	3.61	3.36	3.53
	$l_{2.2}$	0.19	0.13	0.18	0.17	0.16	0.17
	$w_{2.1}$	0.79	0.86	0.82	0.85	0.86	0.88
	$w_{2.2}$	0.15	0.10	0.15	0.13	0.13	0.11
	$w_{2.0}$	0.20	0.18	0.17	0.20	0.18	0.46
	$l_{3.1}$	4.18	3.24	3.99	3.74	3.38	3.53
	$l_{3.2}$	0.13	0.10	0.10	0.10	0.10	0.10
	$w_{3.1}$	0.43	0.47	0.42	0.42	0.45	0.40
	$w_{3.2}$	0.11	0.10	0.10	0.10	0.10	0.10
	$w_{3.0}$	0.22	0.12	0.36	0.38	0.17	0.56
	$l_{4.1}$	3.54	2.61	3.25	3.05	2.70	2.78
	$l_{4.2}$	0.14	0.15	0.15	0.14	0.13	0.13
	$w_{4.1}$	0.17	0.17	0.15	0.16	0.16	0.13
	$w_{4.2}$	0.10	0.13	0.10	0.10	0.13	0.10
	$w_{4.0}$	1.45	1.30	1.31	1.37	1.27	1.39

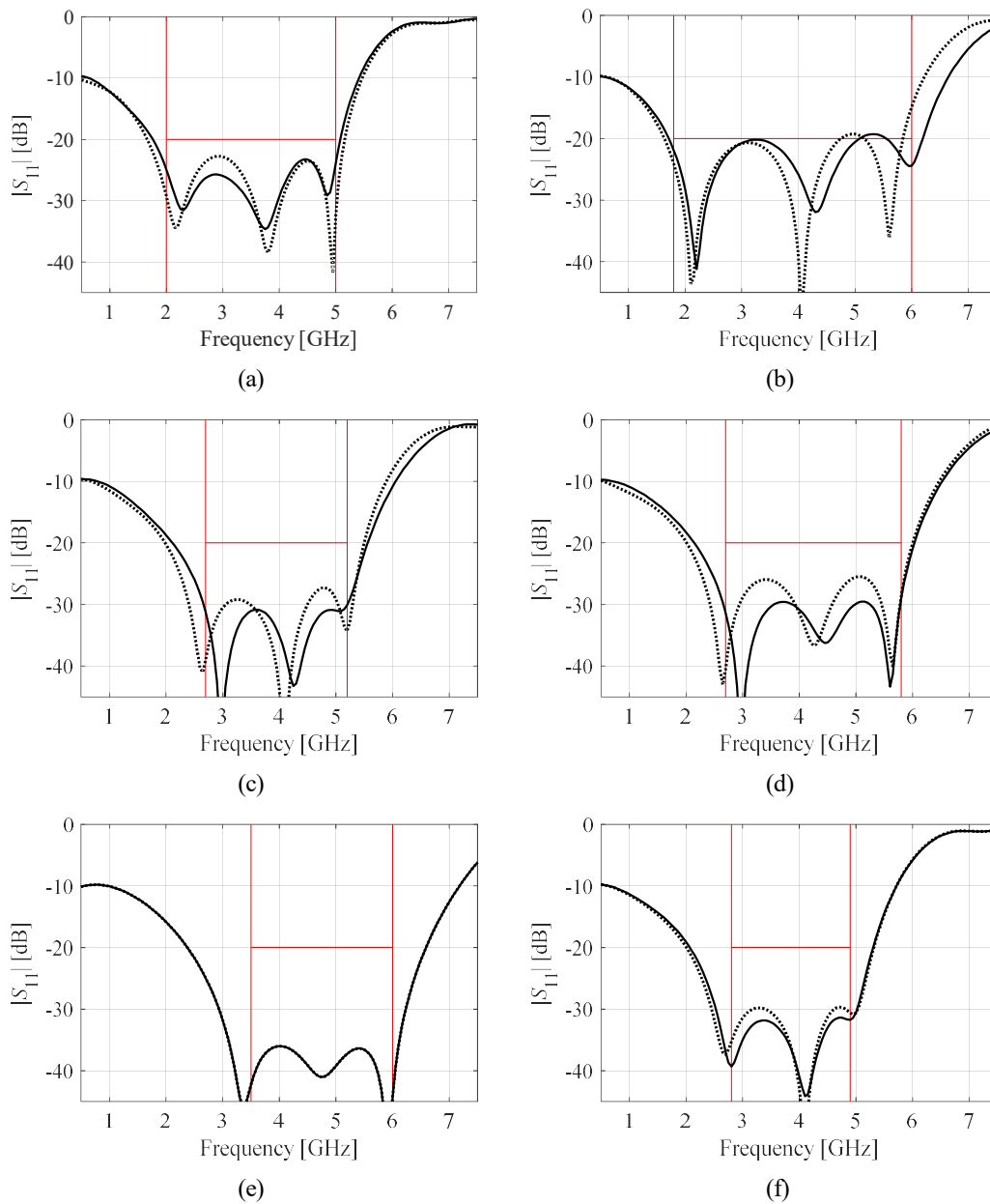


Fig. 4. The responses of three-section impedance matching transformer: initial design found using (2) (····) and the final design obtained using (4), (5) (—). Shown are designs corresponding to the target vectors of Table 2: (a)  $f_1 = 2.0$  GHz,  $f_2 = 5.0$  GHz, (b)  $f_1 = 1.8$  GHz,  $f_2 = 6.0$  GHz, (c)  $f_1 = 2.7$  GHz,  $f_2 = 5.2$  GHz, (d)  $f_1 = 2.7$  GHz,  $f_2 = 5.8$  GHz, (e)  $f_1 = 3.5$  GHz,  $f_2 = 6.0$  GHz, (f)  $f_1 = 2.8$  GHz,  $f_2 = 4.9$  GHz. Red lines indicate intended bandwidths as well as performance specifications.

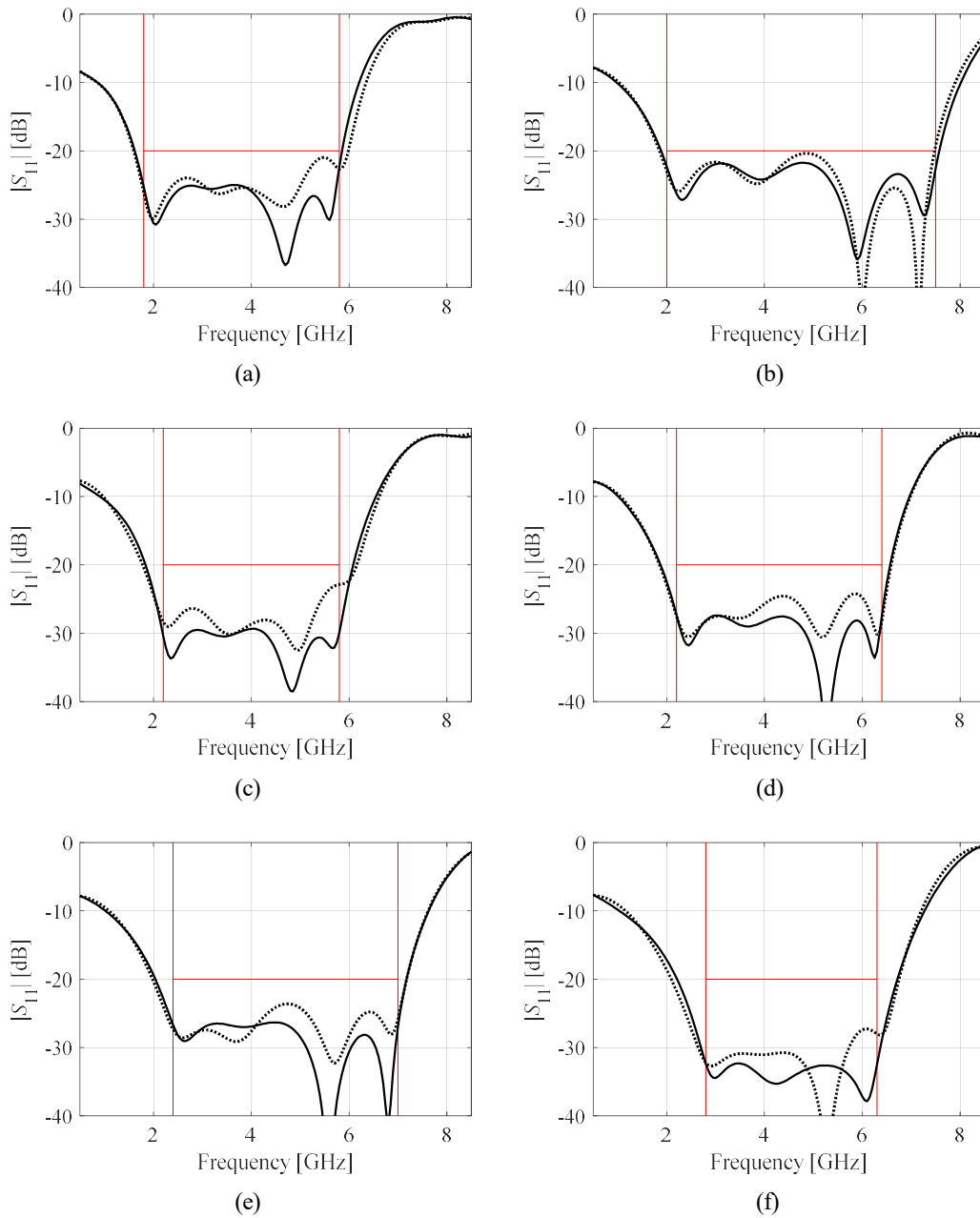


Fig. 5. The responses of four-section impedance matching transformer obtained with the optimization framework set up with nine reference designs: initial design found using (2) (····) and the final design obtained using (4), (5) (—). Shown are designs corresponding to the target vectors of Table 3: (a)  $f_1 = 1.8$  GHz,  $f_2 = 5.8$  GHz, (b)  $f_1 = 2.0$  GHz,  $f_2 = 7.5$  GHz, (c)  $f_1 = 2.2$  GHz,  $f_2 = 5.8$  GHz, (d)  $f_1 = 2.2$  GHz,  $f_2 = 6.4$  GHz, (e)  $f_1 = 2.4$  GHz,  $f_2 = 7.0$  GHz, (f)  $f_1 = 2.8$  GHz,  $f_2 = 6.3$  GHz. Red lines indicate intended bandwidths as well as performance specifications.



In order to further demonstrate the robustness of the proposed framework, optimization of the four-section transformer has been repeated using only five reference designs, corresponding to the following bandwidths: {1.5, 5.5}, {1.5, 7.5}, {2.5, 6.5}, {3.5, 5.5}, and {3.5, 7.5} (frequency in GHz). Figure 6 shows the transformer responses at the initial and optimized designs. The average computational cost of the parameter tuning process is similar to the previous case (i.e., around eight EM simulations), and both the initial and final designs are of good quality. Table 4 gathers the maximum in-band reflection levels for both situations (nine and five reference designs). The average reflection level (over the considered target bandwidth) is only lower by 0.3 dB in favor of the nine-reference-design setup.

### 3. Conclusions

The paper proposed a simple yet efficient framework for expedited design optimization of miniaturized microwave components. Our methodology exploits the pre-existing designs optimized for the selected values of performance figures pertinent to the component at hand, as well as two kriging surrogate models.

Table 4. Design Quality Comparison for Four-Section Impedance Transformer: Optimization Framework with Nine versus Five Reference Designs

Test case	1	2	3	4	5	6
Target $f_1$ [GHz]	1.8	2.0	2.2	2.2	2.4	2.8
operating band $f_2$ [GHz]	5.8	7.5	5.8	6.4	7.0	6.3
Maximum in-band reflection (nine reference designs)	-22.4 dB	-21.7 dB	-29.3 dB	-27.3 dB	-26.3 dB	-32.3 dB
Maximum in-band reflection (five reference designs)	-23.4 dB	-23.1 dB	-25.1 dB	-27.5 dB	-24.5 dB	-33.8 dB

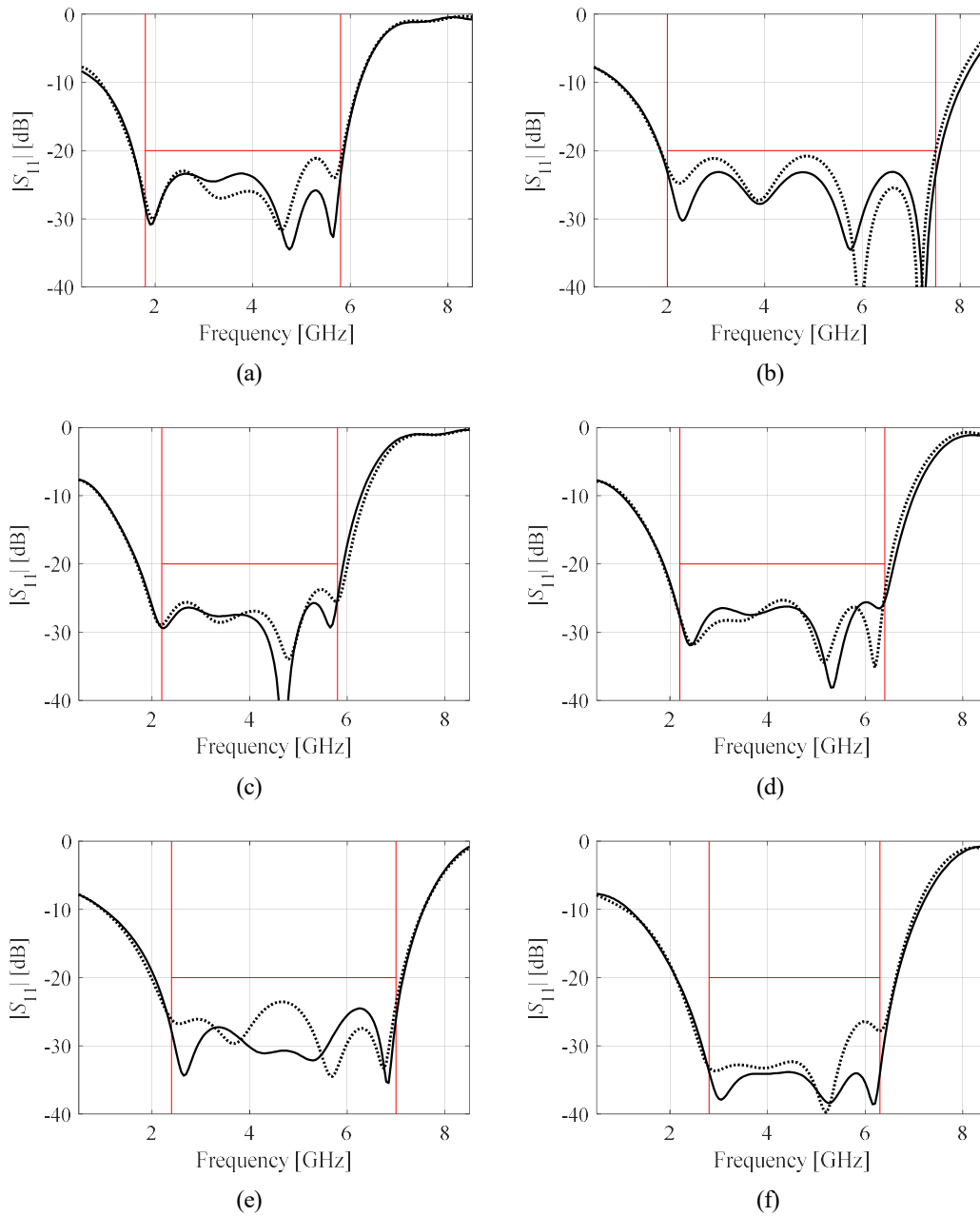


Fig. 6. The responses of four-section impedance matching transformer obtained with the optimization framework set up with five reference designs: initial design found using (2) (····) and the final design obtained using (4), (5) (—). Shown are designs corresponding to the target vectors of Table 3: (a)  $f_1 = 1.8$  GHz,  $f_2 = 5.8$  GHz, (b)  $f_1 = 2.0$  GHz,  $f_2 = 7.5$  GHz, (c)  $f_1 = 2.2$  GHz,  $f_2 = 5.8$  GHz, (d)  $f_1 = 2.2$  GHz,  $f_2 = 6.4$  GHz, (e)  $f_1 = 2.4$  GHz,  $f_2 = 7.0$  GHz, (f)  $f_1 = 2.8$  GHz,  $f_2 = 6.3$  GHz. Red lines indicate intended bandwidths as well as performance specifications.





The first model yields a reasonably good initial design corresponding to the target performance figures, whereas the second model delivers an approximation of the Jacobian matrix of the component response, utilized to jump-start the design refinement process. The optimization procedure is further accelerated by replacing costly finite-differentiation-based Jacobian updates with the Broyden formula.

The proposed framework has been validated using two impedance matching transformers described by large numbers of geometry parameters (fifteen and twenty, respectively), optimized within wide ranges of operating bandwidths. The obtained results demonstrate the capability of the presented approach of yielding high-quality designs at the computational cost as low as a few EM simulations of the structure at hand. Additional experiments conducted for the four-section transformer corroborate the robustness of our methodology as being capable of yielding good results even if the number of pre-existing designs is severely limited. At the same time, because no user-provided initial design is necessary, the framework can be considered a quasi-global procedure (within the range of validity in terms of the considered performance figures).

The proposed approach can be a suitable tool for expediting the parameter tuning procedures especially whenever a certain number of designs are already available for a given structure, or the expected multiple use of the framework justifies the initial effort associated with generating the reference designs required to set up the kriging surrogates.

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