





## Article

# High Efficiency Dual-Active-Bridge Converter with Triple-Phase-Shift Control for Battery Charger of Electric Vehicles

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**Abstract:** An optimal modulation scheme with triple-phase-shift (TPS) control could increase the efficiency in the entire load range for a dual-active-bridge (DAB) converter under wide output voltage range conditions. Therefore, this study proposes a convergent approach to TPS mode selection, coupled with an optimal modulation scheme, ensuring the circuit's efficiency over the entire range in the realm of a high-power and high-efficiency battery charger for electric vehicles. The convergent approach to TPS mode selection also reduces the numerous cases for small-signal analysis through general average modeling. After verifying the small-signal models under various voltage transfer ratios and load conditions to verify the stability, a converter prototype with a rated power of 15 kW is built and tested. Thus, a peak efficiency of 97.7% can be achieved.

**Keywords:** dual-active-bridge converter; triple-phase-shift control; small signal; general average modeling



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## 1. Introduction

In response to environmental concerns, the rapid expansion of electric vehicles (EVs) is poised to become a major influencer in the global transformation of transportation energy. With the increasing proliferation of electric vehicles, the demand for fast charging is gradually rising. Advanced charging technologies for next-generation electric vehicles have become increasingly attractive for academia and the transportation industry in recent years [1,2].

In the realm of electric vehicle charging, the charge power level is continuously escalating, transitioning from conventional AC charging stations to DC fast charging, with future aspirations set on DC ultra-fast charging. Efficient DC-DC converters play a pivotal role in the realm of electric vehicles, serving as crucial components to enhance overall system performance.

Within the current landscape of electric vehicles, they serve not only as environmentally friendly modes of transportation but also incorporate energy-sharing systems (V2H, V2V or V2G) [3,4]. Importantly, different electric vehicles utilize batteries with varying voltage levels, ranging from a minimum of 200 V to as high as 750 V [5]. Consequently, the design of DC-DC converters in the charging stations must be capable of accommodating a wide range of input and output voltages, as well as bidirectional power functionalities.

High efficiency bidirectional DC-DC converters with a wide voltage range operation are necessary to meet requirements of environment friendliness. The selection of an appropriate converter topology is crucial [6–8]. Among the myriad of DC-DC converters, there exist two distinct types: isolated and non-isolated [9]. Isolated converters offer high

galvanic isolation, and a transformer changes the ratio so that they can be adjusted for a broader voltage output range, in comparison to resonant LLC full-bridge circuits or phase-shift full-bridge circuits, among others [10]. The dual-active-bridge converter provides advantages such as bidirectional power flow control, simplified control methodology, wide-range adjustable voltage output and a reduced number of passive components, making it more advantageous [11–14].

The basic control method of the dual-active-bridge converter involves adjusting the output voltage and power through phase-shift angle control. The single-phase-shift (SPS) modulation stands out as the simplest, involving only one control variable. Consequently, for each determined transmission power, there exists only one corresponding control variable. As a result, the value of circuit's peak value and root-mean-square (RMS) current are also uniquely determined. In the performance evaluation of DAB used in electric vehicles, as discussed in [15], it is observed that even with only some switches entering zero voltage switching (ZVS), the converter can still achieve 96% efficiency under a 10 kW output scenario.

Furthermore, in the application of single-phase-shift control, aside from the reactive power leading to transmission losses from the primary side to the secondary side, when the voltage transfer ratio is not equal to 1, it will result in a constrained range of zero voltage switching in the converter and an increase in both peak and RMS current [16–18]. On the contrary, other control methods such as extended-phase-shift (EPS) modulation, dual-phase-shift (DPS) modulation and triple-phase-shift (TPS) modulation are introduced to address issues related to reactive power at different output voltage ranges, achieve a broader range of zero voltage switching or reduce both peak and RMS current in the DAB converter [19–21].

Among the various control modulation techniques (SPS, EPS, DPS and TPS) applied to the dual-active-bridge converter, in addition to the analysis of the control methods in the time domain, the analysis of the frequency domain for each individual control technique is equally crucial. Small-signal models for frequency domain analysis are pivotal for assessing the stability of the circuit's frequency response, transient response, and guiding the design direction of the circuit controller [22,23].

Based on the presented analysis, the application of control modulation techniques to the dual-active-bridge converter will prompt the introduction of both time-domain and frequency-domain analyses. Through the implementation of various control techniques, it will be verified whether the circuit demonstrates improved efficiency across a broad output range. Additionally, an optimal control scheme based on existing control methods will be proposed, their operational range analyzed, and their small-signal accuracy validated. The circuit will be designed to closely align with the voltage range of contemporary electric vehicle batteries, ensuring a performance evaluation that closely mirrors practical applications. Finally, a 15 kW prototype will be implemented to validate the proposed approaches.

## 2. Dual-Active-Bridge Converter

The dual-active-bridge converter topology and the phase shift angle between power switches are defined in Figure 1. The duty cycle of each switch is 50%, and the logic of the two switches in the same leg is complementary.  $D_1$  is the duty of the primary voltage  $V_p$  on the primary side, corresponding to the phase shift angle between switches  $Q_1$  and  $Q_3$ .  $D_2$  is the duty on the secondary voltage  $V_s$  of the secondary side, corresponding to the phase shift angle between switches  $Q_5$  and  $Q_7$ .  $D_\phi$  is the phase shift between the center points of  $D_1$  and  $D_2$ .  $D_3$  is the time difference between the rising edges of  $V_p$  and  $V_s$ , corresponding to the phase shift between switches  $Q_1$  and  $Q_5$ . The definition of the voltage transfer ratio  $M$  is shown in (1).

$$M = N \frac{V_o}{V_{in}} \quad (1)$$



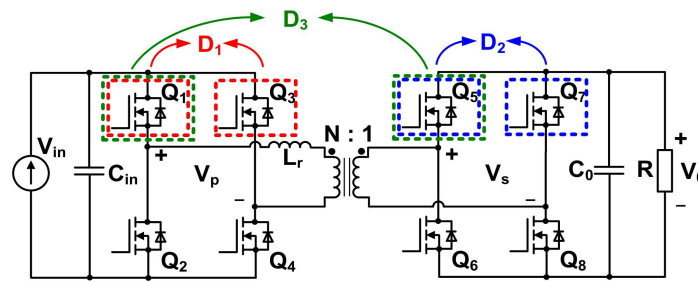


Figure 1. DAB converter and the definition of phase shift.

Each phase shift is defined as the ratio of the phase shift angle  $\theta_x$  to a period  $2\pi$ , as shown in (2). The relationship between phase shift  $D_3$  and other phase shifts is shown in (3), and the timing diagram is presented in Figure 2.

$$D_x = \frac{\theta_x}{2\pi}, x = 1, 2, 3, \varphi \tag{2}$$

$$D_3 = D_\varphi + \frac{D_1}{2} - \frac{D_2}{2} \tag{3}$$

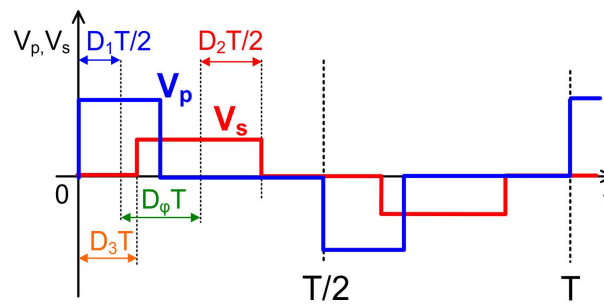


Figure 2. Timing diagram of  $V_p$  and  $V_s$  waveforms.

Numerous studies have presented various approaches to phase-shift control, such as single-phase-shift (SPS) control, extend-phase-shift (EPS) control, dual-phase-shift (DPS) control, and notably, triple-phase-shift (TPS) control [21–32]. TPS offers various phase-shift control combinations through the control of  $D_1$ ,  $D_2$  and  $D_\varphi$ . Some of these combinations can extend the range of zero voltage switching on both the primary and secondary sides, consequently increasing efficiency. Other combinations can reduce the RMS current of the circuit, thereby improving conduction and switching losses in the circuit [21,27,31,32].

Despite the numerous advantages offered by TPS, its practical application necessitates the implementation of a closed-loop controller to regulate the output voltage. Based on [33,34], this study analyzes small signals to achieve precise control of their transient response and introduces a small-signal modeling method called Generalized Average Modeling (GAM) to derive the open-loop power-stage transfer function for a closed-loop controller design.

Due to TPS having various phase shift combinations of  $D_1$ ,  $D_2$ , and  $D_\varphi$  at same output power condition, a specific target must be set before the design, and a suitable operation mode must be selected for the analysis [21,32]. The foundation of each TPS operation mode can be referred to as the operation mode analyzed in [21,27,31,32]. Table 1 shows the relationship and definition between the name of each operation mode and its corresponding phase shift under a positive power flow.

To simplify the multiple selection of these operation mode, which need to be analyzed to obtain its output power function, RMS current and switching points current are used.

**Table 1.** Definition of each operation mode of TPS.

<i>SM<sub>i</sub></i>	<i>Case 1</i>	<i>Case 2</i>
SM1	$0 < D_\varphi \leq \left(\frac{D_1-D_2}{2}\right)$	$0 < D_\varphi \leq \left(\frac{D_2-D_1}{2}\right)$
SM2	$\left(\frac{D_1-D_2}{2}\right) < D_\varphi \leq \left(\frac{D_1+D_2}{2}\right)$	$\left(\frac{D_2-D_1}{2}\right) < D_\varphi \leq \left(\frac{D_2+D_1}{2}\right)$
SM2*	$\left(\frac{D_1-D_2}{2}\right) < D_\varphi \leq \left(1 - \frac{D_1+D_2}{2}\right)$	$\left(\frac{D_2-D_1}{2}\right) < D_\varphi \leq \left(1 - \frac{D_2+D_1}{2}\right)$
SM3	$\left(\frac{D_1+D_2}{2}\right) < D_\varphi \leq \left(1 - \frac{D_1+D_2}{2}\right)$	$\left(\frac{D_2+D_1}{2}\right) < D_\varphi \leq \left(1 - \frac{D_2+D_1}{2}\right)$
SM3*	$\left(1 - \frac{D_1+D_2}{2}\right) < D_\varphi \leq \left(\frac{D_1+D_2}{2}\right)$	$\left(1 - \frac{D_2+D_1}{2}\right) < D_\varphi \leq \left(\frac{D_2+D_1}{2}\right)$
SM4	$\left(1 - \frac{D_1+D_2}{2}\right) < D_\varphi \leq \left(1 - \frac{D_1-D_2}{2}\right)$	$\left(1 - \frac{D_2+D_1}{2}\right) < D_\varphi \leq \left(1 - \frac{D_2-D_1}{2}\right)$
SM5	$\left(1 - \frac{D_1-D_2}{2}\right) < D_\varphi \leq 1$	$\left(1 - \frac{D_2-D_1}{2}\right) < D_\varphi \leq 1$

This study adopted an optimized control method [21,32], entering ZVS mode during light loads to eliminate switching losses. As the output current increases, efforts are directed towards minimizing the circuit’s RMS current to optimize conduction losses. Through this control method, the computational complexity of numerous modes in TPS is simplified, along with reducing the computational burden on the controller. The dedicated power range  $P_{o1}$ , which determines whether to adopt ZVS mode, is shown in (4).

$$P_{o1} = \left[ \begin{array}{l} \frac{V_{in}^2 M^2 (1-M)}{4L f_s}, M < 1 \\ \frac{V_{in}^2 (M-1)}{4L f_s M}, M > 1 \end{array} \right] \tag{4}$$

When the output power range is  $P \in [0, P_{o1}]$ , DAB will operate in SM1 (ALL-ZVS mode), and when the output power range is  $P \in [P_{o1}, M\pi/4]$ , DAB will operate in SM3\* (Minimum Peak Current mode). The optimized phase shift variables,  $D_1$ ,  $D_2$  and  $D_\varphi$ , are shown in Table 2 and are, respectively, labeled according to the voltage conversion ratio  $M$  and switching waveform shown in Figure 3. The goal is to achieve ZVS for all switches under light load conditions so that TPS operates in SM1. Table 3 shows the required switching point current, which can achieve ZVS.

**Table 2.** Optimized phase shift angle value.

<i>Power Range</i>	<i>M</i>	<i>M &lt; 1</i> <i>(Case 2)</i>	<i>M &gt; 1</i> <i>(Case 1)</i>
$P \in [0, P_{o1}]$		$D_{1\_opt} = \sqrt{\frac{2P_o}{(1-M)\pi}}$	$D_{1\_opt} = \frac{1}{M} \sqrt{\frac{2P_o}{M(M-1)\pi}}$
		$D_{2\_opt} = \sqrt{\frac{2P_o}{M^2(1-M)\pi}}$	$D_{2\_opt} = \sqrt{\frac{2P_o}{M(M-1)\pi}}$
		$D_{\varphi\_opt} = \sqrt{\frac{2(1-M)\pi P_o}{2\pi M}}$	$D_{\varphi\_opt} = \sqrt{\frac{2P_o(M-1)}{M\pi}}$
$P \in [P_{o1}, M\pi/4]$		$D_{1\_opt} = 1 - (1-M) \sqrt{\frac{M\pi - 4P_o}{(1-2M+2M^2)M\pi}}$	$D_{1\_opt} = 1$
		$D_{2\_opt} = 1$	$D_{2\_opt} = 1 - \sqrt{\left(1 - \frac{4P_o}{M\pi}\right) \frac{(M-1)^2}{(M-1)^2 + 1}}$
		$D_{\varphi\_opt} = 0.5 - 0.5 \sqrt{\frac{M(M\pi - 4P_o)}{(1-2M+2M^2)\pi}}$	$D_{\varphi\_opt} = 1 - \sqrt{2D_{2\_opt} - D_{\varphi\_opt}^2 - \frac{4P_o}{M\pi}}$

TPS has the most remarkable effect on improving the reactive power, current peak value and RMS value because of its diversity and capability of providing a larger ZVS range and wider voltage conversion ratio, making it possible to achieve ZVS under light load conditions. The drawback of TPS is its complexity in control. With the optimal control method for selecting limited modes in TPS, the number of modes requiring analysis has been reduced. In this study, a small-signal model analysis of TPS within the optimal

operational range was proposed. The obtained results focus on analyzing specific modes (Case 1 SM1, Case 2 SM1, Case 1 SM3\* and Case 2 SM3\*), but the approach can still be broadly applied to other TPS modes. Utilizing the analysis results, a compensator can be designed to assess loop stability through a bode plot. In practical experiments, an Ambiguous mode needs to be applied between the ALL-ZVS mode and the Minimum Peak Current mode to ensure a smooth transient response.

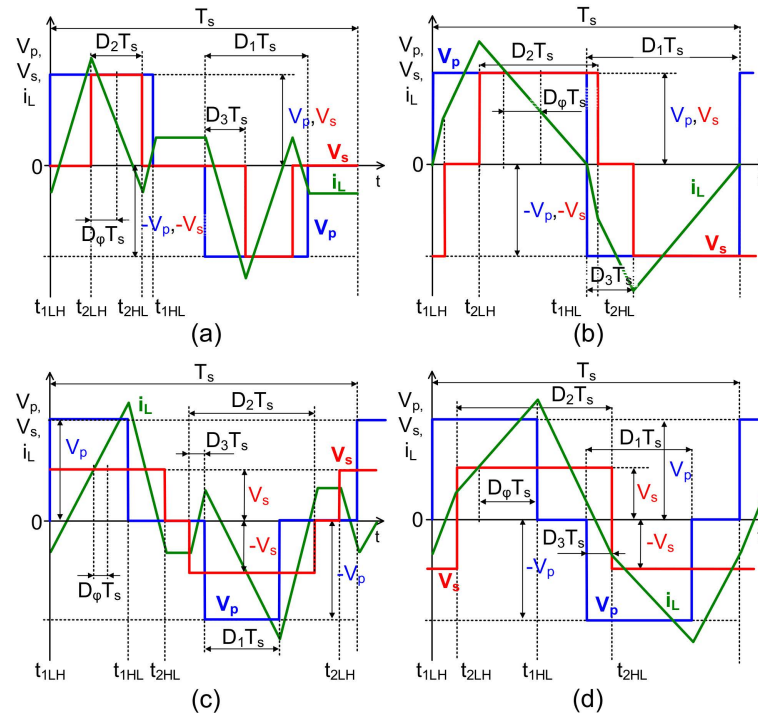


Figure 3. Timing diagram of TPS, (a) Case 1 SM1, (b) Case 1 SM3\*, (c) Case 2 SM1, (d) Case 2 SM3\*.

Table 3. ZVS conditions of SM1.

Switches	ZVS Conditions
$Q_1$	$i_{L(t_{1LH})} \leq I_{\min\_Q1} (-\sqrt{\frac{2V_{in}^2 C_{oss}(1-2M)}{L}})$
$Q_3$	$i_{L(t_{1HL})} \leq I_{\min\_Q3} (\sqrt{\frac{2V_{in}^2 C_{oss}(1-2M)}{L}})$
$Q_5$	$i_{L(t_{2LH})} \leq I_{\min\_Q5} (\sqrt{\frac{2V_{in}^2 C_{oss}}{L}})$
$Q_7$	$i_{L(t_{2HL})} \leq I_{\min\_Q7} (-\sqrt{\frac{2V_{in}^2 C_{oss}}{L}})$

### 3. Small-Signal Modeling and Analysis of TPS

In the conventional state–space averaging method, the state variables of the circuit (e.g., output capacitor voltage and inductor current) are averaged, The AC components are ignored and calculated as pure DC values. This method is suitable for a topology with a small AC component, but the inductor current in DAB is pure AC. If the traditional state–space averaging method is applied, then the state cannot be accurately represented; thus, the generalized state–space averaging method must be used [33]. The definition of the state–space model to be used is shown in (5), and the  $A$ ,  $B$ ,  $C$  and  $D$  matrices are the targets of the derivation.

$$\begin{aligned} \dot{x}_s &= Ax_s + Bu_s \\ y_s &= Cx_s + Du_s \end{aligned} \tag{5}$$

Next, the state variable matrix  $x_s$ , the output variable matrix  $y_s$  and the input variable matrix  $u_s$  required for the derivation are defined, and their included variables are shown in (6).

$$x_s = \begin{bmatrix} \Delta v_c \\ \Delta i_{L_1R} \\ \Delta i_{L_1I} \\ \Delta v_o \\ 0 \end{bmatrix} \quad u_s = \begin{bmatrix} \Delta d_1 \\ \Delta d_2 \\ \Delta d_\phi \\ \Delta v_{in} \\ \Delta i_N \end{bmatrix} \quad y_s = \begin{bmatrix} \Delta v_o \\ \Delta i_o \\ 0 \\ 0 \\ 0 \end{bmatrix} \quad (6)$$

The switches are assumed to be ideal without resistance  $R_{DS(on)}$  to simplify the analysis. The magnetizing inductance  $L_m$  of the transformer is regarded as infinite and ignorable. The input is considered an ideal voltage source; thus, the input capacitor  $C_{in}$  is ignored.  $R_t$  is the sum of the wire resistance of the transformer and the inductor equivalent on the primary side.  $r_c$  is the equivalent series resistance (ESR) of the output capacitors.  $i_N$  is the disturbance of the output current  $I_o$ . The model used for the derivation is shown in Figure 4.

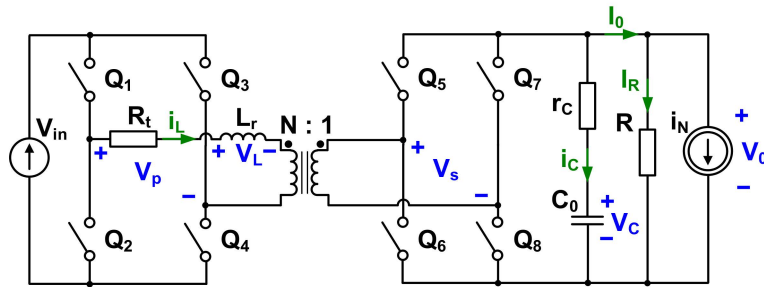


Figure 4. Small-signal model.

Different voltage conversion ratios and load conditions result in various switching sequence and corresponding inductor current shapes. Thus, four operation modes are used in this study, and the derivation details are conducted with *SM1* of *Case 2*. The relationship between  $V_p, V_s$ , and the input and output voltages  $V_{in}, V_o$ , must be defined in the small-signal model, as shown in (7).

$$\begin{aligned} V_p(t) &= s_1(t) \times V_{in} \\ V_s(t) &= s_2(t) \times V_o \end{aligned} \quad (7)$$

$s_1$  and  $s_2$  represent the timing of the primary and secondary side switches, respectively. The expression of the waveforms of  $V_p$  and  $V_s$  in Figure 3c are listed, as shown in (8) and (9), respectively. The period  $T$  is the reciprocal of switching frequency  $f_s$ .

$$s_1(t) = \begin{pmatrix} 1, & 0 \leq t < D_1 T \\ 0, & D_1 T \leq t < \frac{T}{2} \\ -1, & \frac{T}{2} \leq t < \frac{T}{2} + D_1 T \\ 0, & \frac{T}{2} + D_1 T \leq t < T \end{pmatrix} \quad (8)$$

$$s_2(t) = \begin{pmatrix} 1, & 0 \leq t < D_\phi T + \frac{(D_1+D_2)T}{2} \\ 0, & D_\phi T + \frac{(D_1+D_2)T}{2} \leq t < D_\phi T + \frac{(1+D_1-D_2)T}{2} \\ -1, & D_\phi T + \frac{(1+D_1-D_2)T}{2} \leq t < D_\phi T + \frac{(1+D_1+D_2)T}{2} \\ 0, & D_\phi T + \frac{(1+D_1+D_2)T}{2} \leq t < D_\phi T + \frac{(2+D_1-D_2)T}{2} \\ 1, & D_\phi T + \frac{(2+D_1-D_2)T}{2} \leq t < T \end{pmatrix} \quad (9)$$

Next, according to Kirchhoff’s voltage and current laws, the relationship between inductor voltage and current and that between output capacitor voltage and current, the

relational expression of output voltage, and the relational expression of output current can be listed, as shown in (10)–(13).

$$V_L(t) = L_t \frac{di_L(t)}{dt} = V_p(t) - V_{R_t}(t) - NV_s(t) \quad (10)$$

$$i_c(t) = C_o \frac{dV_c(t)}{dt} = N \times i_L(t) - i_R(t) - i_N(t) \quad (11)$$

$$V_o(t) = \frac{R \times r_c}{R + r_c} \times N \times s_2(t) i_L(t) - \frac{R \times r_c}{R + r_c} \times i_N(t) + \frac{R}{R + r_c} \times V_c(t) \quad (12)$$

$$I_o(t) = \frac{r_c}{R + r_c} \times N \times s_2(t) i_L(t) + \frac{1}{R + r_c} \times V_c(t) + \frac{R}{R + r_c} \times i_N(t) \quad (13)$$

Given that  $i_R = V_o/R$ , (12) can be used to replace  $i_R$  in (13); thus, (14) can be obtained.

$$i_c(t) = C_o \frac{dV_c(t)}{dt} = \frac{NR}{R + r_c} \times i_L(t) s_2(t) - \frac{1}{R + r_c} \times V_c(t) - \frac{R}{R + r_c} \times i_N(t) \quad (14)$$

The four aforementioned equations can be converted into three equations: zero-order, and first-order (one real part and one imaginary part) [28]. The rewritten equations of the first-order real and imaginary parts of  $i_L$  are shown in (15) and (16), respectively.

$$\frac{d}{dt} \langle i_L \rangle_{1R} = \frac{-R_t}{L_t} \langle i_L \rangle_{1R} + \omega_s \langle i_L \rangle_{1I} + \frac{1}{L_t} \langle s_1 \rangle_0 \langle v_{in} \rangle_{1R} + \frac{1}{L_t} \langle s_1 \rangle_{1R} \langle v_{in} \rangle_0 - \frac{N}{L_t} \langle s_2 \rangle_0 \langle v_o \rangle_{1R} - \frac{N}{L_t} \langle s_2 \rangle_{1R} \langle v_o \rangle_0 \quad (15)$$

$$\frac{d}{dt} \langle i_L \rangle_{1I} = \frac{-R_t}{L_t} \langle i_L \rangle_{1I} - \omega_s \langle i_L \rangle_{1R} + \frac{1}{L_t} \langle s_1 \rangle_0 \langle v_{in} \rangle_{1I} + \frac{1}{L_t} \langle s_1 \rangle_{1I} \langle v_{in} \rangle_0 - \frac{N}{L_t} \langle s_2 \rangle_0 \langle v_o \rangle_{1I} - \frac{N}{L_t} \langle s_2 \rangle_{1I} \langle v_o \rangle_0 \quad (16)$$

Most of the output capacitor voltage  $v_c$  is a DC component, and the proportion of the AC component is relatively small; thus,  $v_c$  does not need to consider its first-order real and imaginary terms but only needs to consider its zero-order term.

$$\begin{aligned} \frac{d}{dt} \langle v_c \rangle_0 &= \frac{-R}{C_o(R+r_c)} \langle i_N \rangle_0 - \frac{1}{C_o(R+r_c)} \langle v_c \rangle_0 + \frac{NR}{C_o(R+r_c)} \langle s_2 \rangle_0 \langle i_L \rangle_0 \\ &+ \frac{2NR}{C_o(R+r_c)} \langle s_2 \rangle_{1R} \langle i_L \rangle_{1R} + \frac{2NR}{C_o(R+r_c)} \langle s_2 \rangle_{1I} \langle i_L \rangle_{1I} \end{aligned} \quad (17)$$

As output variables,  $v_o$  and  $i_o$  do not need to be differentiated, and these are mainly DC components.

$$\langle v_o \rangle_0 = \frac{NRr_c}{R + r_c} \langle s_2 \rangle_0 \langle i_L \rangle_0 + \frac{2NRr_c}{R + r_c} \langle s_2 \rangle_{1R} \langle i_L \rangle_{1R} + \frac{2NRr_c}{R + r_c} \langle s_2 \rangle_{1I} \langle i_L \rangle_{1I} - \frac{Rr_c}{R + r_c} \langle i_N \rangle_0 + \frac{R}{R + r_c} \langle v_c \rangle_0 \quad (18)$$

$$\langle i_o \rangle_0 = \frac{Nr_c}{R + r_c} \langle s_2 \rangle_0 \langle i_L \rangle_0 + \frac{2Nr_c}{R + r_c} \langle s_2 \rangle_{1R} \langle i_L \rangle_{1R} + \frac{2Nr_c}{R + r_c} \langle s_2 \rangle_{1I} \langle i_L \rangle_{1I} + \frac{R}{R + r_c} \langle i_N \rangle_0 + \frac{1}{R + r_c} \langle v_c \rangle_0 \quad (19)$$

The five aforementioned equations reveal several new variables, and some of these variables can be defined to simplify the equation. Assume that the dynamic characteristics of input voltage and load are substantially slower than the dynamic characteristics of DAB. Therefore, the first-order real and imaginary terms of  $v_{in}$  and  $i_o$  are set to 0, and the zero-order term is its DC value, as shown in (20).

$$\begin{aligned} \langle v_{in} \rangle_{1R} &= \langle v_{in} \rangle_{1I} = 0, \langle v_{in} \rangle_0 = V_{in} \\ \langle i_o \rangle_{1R} &= \langle i_o \rangle_{1I} = 0, \langle i_o \rangle_0 = I_o \end{aligned} \quad (20)$$

Next, the switching signals  $s_1$  and  $s_2$  must be processed using the Fourier series. The timing equations of the switches are integrated to obtain the three coefficients of  $s_1$  and  $s_2$

separately. The calculation only considers the first-order harmonic; thus, the order  $k$  in  $a_1$  and  $b_1$  is substituted for 1. The results of  $s_1$  and  $s_2$  are shown in (21) and (22), respectively.

$$\begin{aligned} a_0 &= 0 \\ a_1 &= \frac{2 \sin(2\pi D_1)}{\pi} \\ b_1 &= -\frac{2 \cos(2\pi D_1) - 2}{\pi} \end{aligned} \tag{21}$$

$$\begin{aligned} a_0 &= 0 \\ a_1 &= \frac{2 \sin[\pi(D_1 + D_2 + 2D_\varphi)] - 2 \sin[\pi(D_1 - D_2 + 2D_\varphi)]}{\pi} \\ b_1 &= -\frac{2 \cos[\pi(D_1 + D_2 + 2D_\varphi)] - 2 \cos[\pi(D_1 - D_2 + 2D_\varphi)]}{\pi} \end{aligned} \tag{22}$$

The above results must be averaged using the concept of sliding average to address the changes in the state variables, and the order  $k$  is substituted for 1 [34]. The results are arranged to obtain the averaged first-order real and imaginary part coefficients. The results of  $s_1$  and  $s_2$  are shown in (23) and (24), respectively; these results are the same as those of other operation modes.

$$\begin{aligned} \langle s_1 \rangle_{1R} &= \frac{\sin(2\pi D_1)}{\pi} \\ \langle s_1 \rangle_{1I} &= \frac{\cos(2\pi D_1) - 1}{\pi} \end{aligned} \tag{23}$$

$$\begin{aligned} \langle s_2 \rangle_{1R} &= \frac{\sin[\pi(D_1 + D_2 + 2D_\varphi)] - \sin[\pi(D_1 - D_2 + 2D_\varphi)]}{\pi} \\ \langle s_2 \rangle_{1I} &= \frac{\cos[\pi(D_1 + D_2 + 2D_\varphi)] - \cos[\pi(D_1 - D_2 + 2D_\varphi)]}{\pi} \end{aligned} \tag{24}$$

Subsequently, a disturbance is added to each variable, as shown in (25), where the uppercase part and the lowercase with  $\Delta$  represent its DC and AC small-signal components, respectively.

$$\begin{aligned} D_1 &= D_1 + \Delta d_1 \\ D_2 &= D_2 + \Delta d_2 \\ D_\varphi &= D_\varphi + \Delta d_\varphi \\ \langle v_{in} \rangle_0 &= V_{in_0} + \Delta v_{in_0} \\ \langle v_o \rangle_0 &= V_{o_0} + \Delta v_{o_0} \\ \langle i_L \rangle_{1R} &= I_{L_1R} + \Delta i_{L_1R} \\ \langle i_L \rangle_{1I} &= I_{L_1I} + \Delta i_{L_1I} \\ \langle i_o \rangle_0 &= I_{o_0} + \Delta i_{o_0} \end{aligned} \tag{25}$$

$I_{L_1R}$  and  $I_{L_1I}$  are the first-order real and imaginary part coefficients of the inductor current, respectively, and the processing steps are the same as  $s_{1_1R}$  and  $s_{1_1I}$ . The current definition of each point is shown in Figure 5.

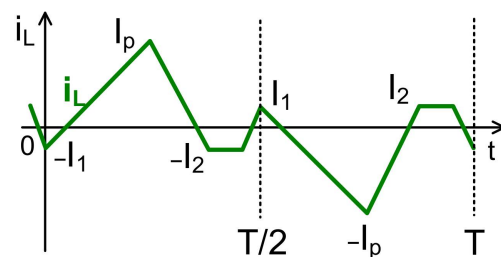


Figure 5. Name of each point of the inductor current.

The point currents  $I_1$ ,  $I_2$  and  $I_p$  must also be defined. In accordance with the expression of the inductor current of Case 2 SM1 in each interval, the equation of each point current can be obtained. The results are shown in (26)–(28).

$$I_1 = \frac{2D_1 \left( \frac{V_{in_0}}{N} - V_{o_0} \right) - 4V_{o_0} D_\varphi}{4L_t f_s \frac{1}{N}} \tag{26}$$



$$I_2 = -\frac{2D_1 \frac{V_{in,0}}{N} - 2D_2 V_{o,0}}{4L_t f_s \frac{1}{N}} \tag{27}$$

$$I_p = \frac{2D_1(\frac{V_{in,0}}{N} - V_{o,0}) + 4V_{o,0}D_\varphi}{4L_t f_s \frac{1}{N}} \tag{28}$$

The waveform sequence of the inductor current can then be defined. The inductor current equation and the definition of each time point are shown in (29). The sequence can be processed using the Fourier series to obtain the DC term  $a_0$  and the first-order Fourier coefficients  $a_1$  and  $b_1$ , and the sliding average same is the same as  $s_{1\_1R}$  and  $s_{1\_1I}$ . The results of  $I_{L\_1R}$  and  $I_{L\_1I}$  are not presented in this study because the equations are too long.

$$i_L(t) = \left\{ \begin{array}{ll} -I_1 + \frac{v_{in} - Nv_o}{L_t} * (t - 0) & , 0 \leq t < t_1 \\ I_p + \frac{0 - Nv_o}{L_t} * (t - t_1) & , t_1 \leq t < t_2 \\ -I_2 + \frac{0 - 0}{L_t} * (t - t_2) & , t_2 \leq t < t_3 \\ -I_2 + \frac{0 - (-Nv_o)}{L_t} * (t - t_3) & , t_3 \leq t < t_4 \\ I_1 + \frac{(-v_{in}) - (-Nv_o)}{L_t} * (t - t_4) & , t_4 \leq t < t_5 \\ -I_p + \frac{0 - (-Nv_o)}{L_t} * (t - t_5) & , t_5 \leq t < t_6 \\ I_2 + \frac{0 - 0}{L_t} * (t - t_6) & , t_6 \leq t < t_7 \\ I_2 + \frac{0 - Nv_o}{L_t} * (t - t_7) & , t_7 \leq t < T \end{array} \right\} \tag{29}$$

$$t_1 = D_1 T, t_2 = \frac{(D_1 + D_2)T}{2} + D_\varphi T, t_3 = \frac{(1 + D_1 - D_2)T}{2} + D_\varphi T$$

$$t_4 = \frac{T}{2}, t_5 = \frac{T}{2} + D_1 T, t_6 = \frac{(1 + D_1 + D_2)T}{2} + D_\varphi T$$

$$t_7 = \frac{(2 + D_1 - D_2)T}{2} + D_\varphi T$$

Finally, the small-signal coefficient terms of the variables of each equation in (15)–(19) must be arranged. The results are substituted into (5) and put into matrices  $A$ ,  $B$ ,  $C$  and  $D$ . The detailed elements are presented in Appendix A, specifically labeled from (A1) to (A5). The first Equation (5) is then sorted into the form  $x_s$  and entered as  $y_s$ . Equation (30) can be obtained after sorting. In this form, different combinations of input variables  $u_s$  and output variables  $y_s$  can be freely selected to express the relationship between the two variables.

$$\frac{y_s}{u_s} = C(sI - A)^{-1}B + D \tag{30}$$

Next, the result is verified. The phase shifts  $D_1$  and  $D_2$  are calculated through the phase shift  $D_\varphi$ , thus the relationship between  $\Delta d_\varphi$  and  $\Delta v_o$  is verified. The transfer function is defined as  $G_{v\varphi(s)}$ , as shown in (31).

$$G_{v\varphi}(s) = \frac{\Delta v_o}{\Delta d_\varphi} = (1 \ 0 \ 0 \ 0 \ 0) \left[ C(sI - A)^{-1}B \begin{pmatrix} 0 \\ 0 \\ 1 \\ 0 \\ 0 \end{pmatrix} + D \begin{pmatrix} 0 \\ 0 \\ 1 \\ 0 \\ 0 \end{pmatrix} \right] \tag{31}$$

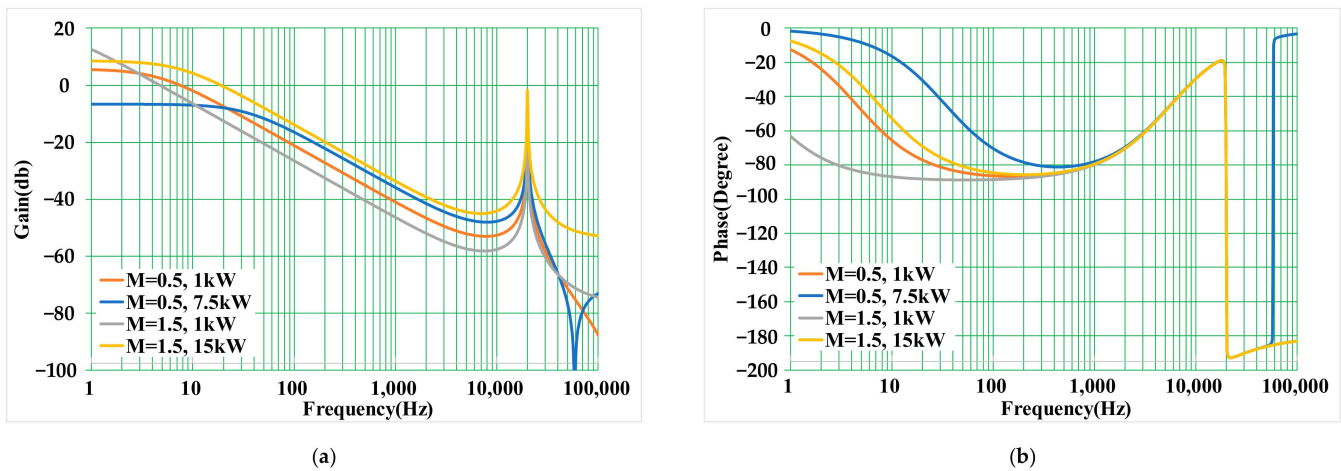
The output voltage of the phase shift angle transfer function (32) can be obtained after sorting  $G_{v\varphi}(s)$ . This function contains the PWM modulation gain  $F_m(s)$ , a simplified second-order formula  $K_s(s)$ , and one zero, one pole and a set of complex conjugate poles. The zero comprise  $C_o$  and its ESR; the pole comprises the load  $R$ ,  $C_o$  and its ESR; and the complex conjugate poles are affected by  $\omega_s$ .

$$G_{v\varphi}(s) = \frac{F_m(s) \times 4NR \times (sC_o r_c + 1)K_s(s)}{\pi(sC_o r_c + sC_o R + 1)(s^2 L_t^2 + 2sL_t R_t + L_t^2 \omega_s^2 + R_t^2)} \tag{32}$$

The composition of the derivation results of each operation mode (*Case 1 SM1*, *Case 1 SM3\**, *Case 2 SM1* and *Case 2 SM3\**) is the same as (32). Table 4 shows the circuit parameters. Figure 6 shows the open-loop bode plot of the power stage based on these parameters.

**Table 4.** Circuit parameter table.

Parameters	Value
Switching Frequency ( $f_s$ )	20 kHz
Input Voltage ( $V_{in}$ )	750 V
Load Resistance ( $R$ )	62.5 $\Omega$ ( $M = 0.5, 1 \text{ kW}$ )
	8.33 $\Omega$ ( $M = 0.5, 7.5 \text{ kW}$ )
	562.5 $\Omega$ ( $M = 1.5, 1 \text{ kW}$ )
	37.5 $\Omega$ ( $M = 1.5, 15 \text{ kW}$ )
Output Capacitance ( $C_o$ )	560 $\mu\text{F}$
Output Capacitor ESR ( $r_c$ )	50 m $\Omega$
Series Inductance ( $L_t$ )	164 $\mu\text{H}$
Circuit DCR ( $R_t$ )	55 m $\Omega$
Turns Ratio ( $N$ )	1.55:1
PWM Modulation Gain ( $F_m(s)$ )	1/3000



**Figure 6.** Bode plot of  $G_{v\phi}(s)$ . (a) Gain, (b) Phase.

#### 4. Control Loop Design Consideration

A high efficiency algorithm must be implemented to achieve the full range of high efficiency operation. In light loads ( $P \in [0, P_{o1}]$ ), DABs with low efficiency due to switching loss will operate in ALL-ZVS mode (*Case 1 SM1* or *Case 2 SM1*). Along with increasing output current ( $P \in [P_{o1}, M\pi/4]$ ), the Minimum Peak Current mode (*Case 1 SM3\** or *Case 2 SM3\**) must be applied to lower the RMS current. Between the two modes, the Ambiguous mode calculates parameters derived from the equations of both ALL-ZVS mode and Minimum Peak Current mode to resolve the transition. The final output parameter is determined by the solved parameters, specifically  $D_1$  and  $D_2$ , with the greater value taking precedence. However, the situation is reversed for  $D_\phi$ . The system block diagram and the correlation between the phase shift angle and output power are depicted in Figures 7 and 8. The result of the Ambiguous mode calculation is represented by the purple line.

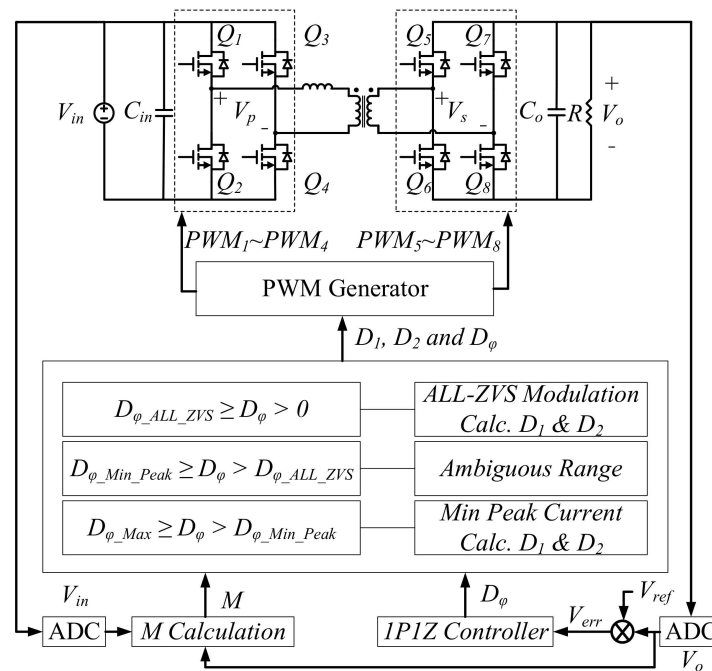


Figure 7. System block diagram.

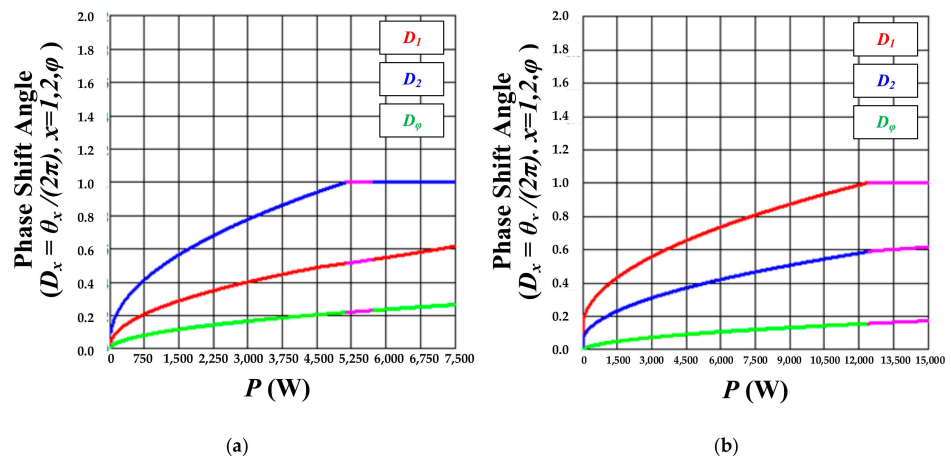


Figure 8. Phase shift angle to output power. (a)  $V_o = 250$  V, (b)  $V_o = 750$  V.

The closed loop must be implemented to control the output power and voltage. The control loop gain is shown in (33) and (34), and the feedback gain  $K$  is 0.002. Meanwhile, the compensator  $G_{ea}(s)$  provides one pole and one zero.

$$\frac{\hat{v}_o}{\hat{i}_o} = \frac{-Z_o(s)}{1 + G_{loop}(s)} = \frac{-Z_o(s)}{1 + G_{v\phi}(s) \times K \times G_{ea}(s) \times F_m(s)} \tag{33}$$

$$Z_o(s) = \frac{\Delta v_o}{\Delta i_o} = (1 \ 0 \ 0 \ 0 \ 0) \left[ C(sI - A)^{-1}B \begin{pmatrix} 0 \\ 0 \\ 0 \\ 0 \\ 1 \end{pmatrix} + D \begin{pmatrix} 0 \\ 0 \\ 0 \\ 0 \\ 1 \end{pmatrix} \right] \tag{34}$$

Next, the simulation result of the closed-loop  $G_{loop}(s)$  Bode plot is shown in Figure 9. The original  $M = 0.5$ , 7.5 kW condition is limited by sufficient DC gain to regulate the output voltage, which can be solved after compensation. The simulation results only records from 100 Hz to 250 kHz because the full frequency range simulation is time-consuming.

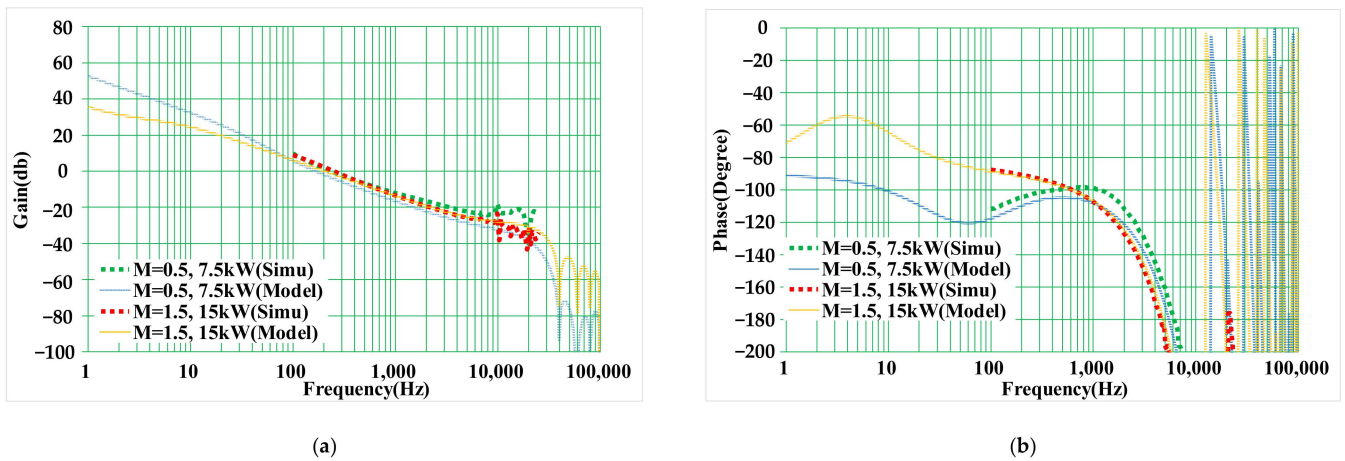


Figure 9. Bode plot of  $G_{loop}(s)$ . (a) Gain, (b) Phase.

### 5. Experimental Verifications

Table 5 is the specification parameter table for the DAB converter. The soft-start, transient response and TPS/SPS comparison tests are conducted. Figure 10 illustrates that the output power is constrained by the maximum constant current point and maximum output power, emulating the actual charging behavior of the battery.

Table 5. Specifications parameter table of DAB.

Parameters	Value
Switching Frequency ( $f_s$ )	20 kHz
Input Voltage ( $V_{in}$ )	750 V
Output Voltage ( $V_o$ )	250 V~750 V
Maximum Output Power ( $P_o$ )	15 kW
Maximum Output Current ( $I_o$ )	30 A (Constant Current)
Output Capacitance ( $C_o$ )	560 $\mu\text{F}$
Output Capacitor ESR ( $r_c$ )	50 m $\Omega$
Series Inductance ( $L_t$ )	164 $\mu\text{H}$
MOSFET Output Capacitance ( $C_{oss}$ )	550 pF
Turns Ratio ( $N$ )	(Infineon FF23MR12W1M1_B11) 1.55:1

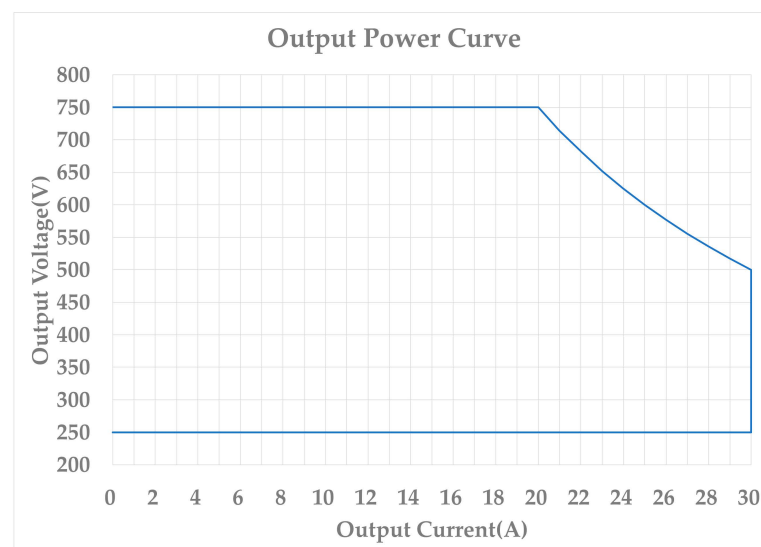
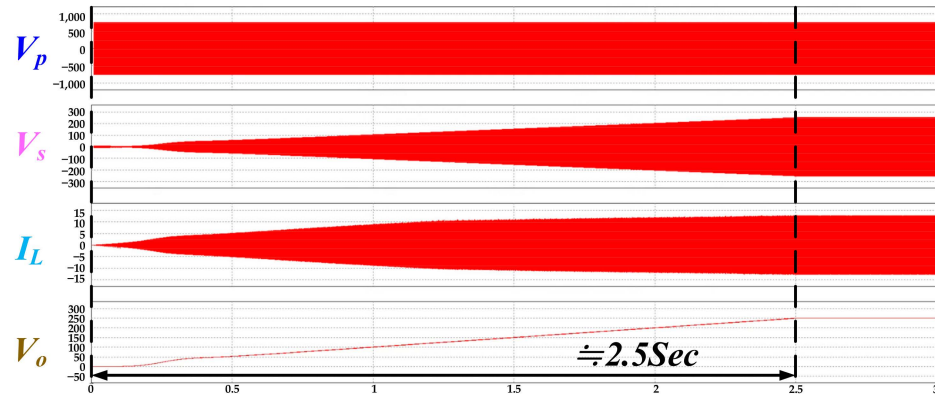


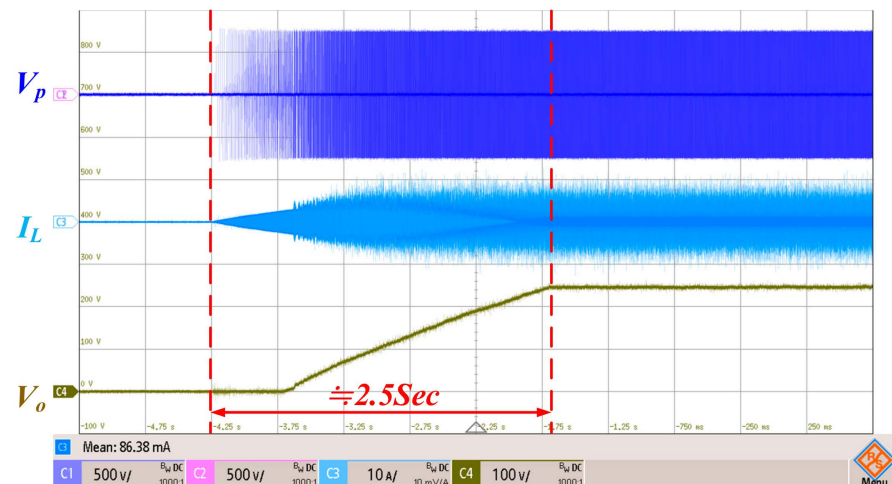
Figure 10. Output voltage–current curve.

### 5.1. Result of Soft-Start and Transient Response

Firstly, the output voltage is 250 V as the test condition, and the soft start will establish the output voltage smoothly without causing sudden inductor current change. This ensures the stability of the control loop and the effectiveness of the soft start. The simulation result is depicted in Figure 11, while the experimental result is presented in Figure 12.



**Figure 11.** Simulation waveform of TPS soft start with  $V_o = 250$  V ( $V_p$ : 500 V/div;  $V_s$ : 100 V/div;  $I_L$ : 5 A/div; time: 500 ms/div).

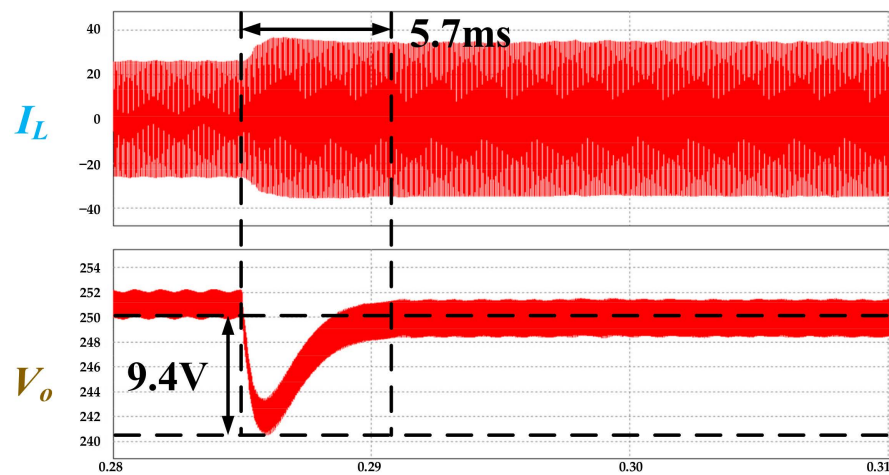


**Figure 12.** Experimental waveform of TPS soft start with  $V_o = 250$  V ( $V_p$ : 500 V/div;  $I_L$ : 10 A/div; time: 500 ms/div).

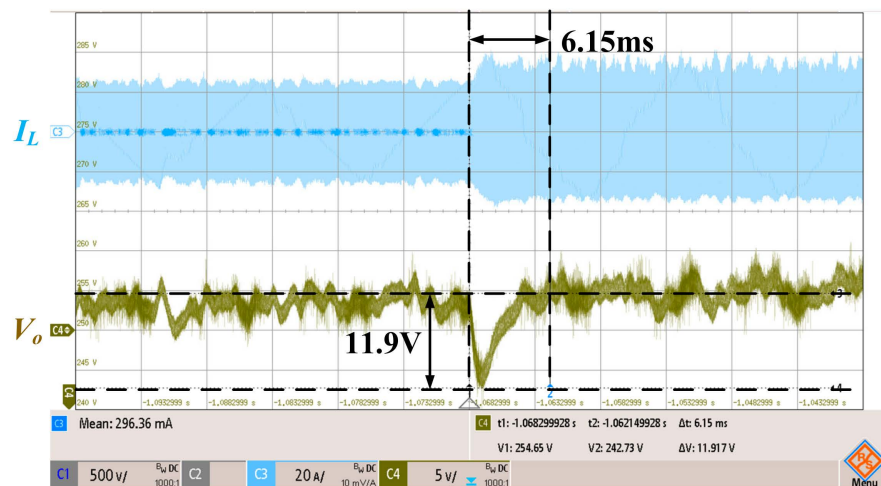
Load variation measurements were conducted to verify closed-loop performance and circuit stability within the test conditions ranging from 4.5 kW to 7.5 kW. The comparison of simulated and experimental waveforms aimed to assess the alignment of differences and trends in small-signal modeling and practical measurements appropriately. The results are shown in Figures 13 and 14, respectively.

Next, the output voltage is 750 V as the test condition, the soft start will establish the output voltage smoothly without causing sudden inductor current change. The simulation result is depicted in Figure 15, while the experimental result is presented in Figure 16.

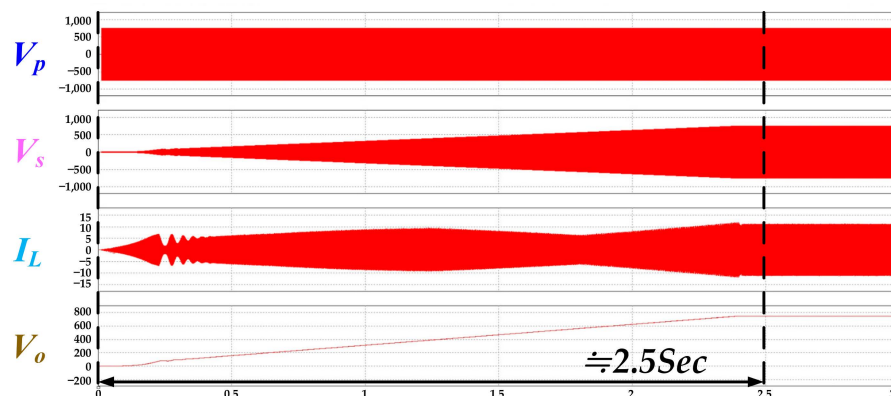
Load variation measurements were also conducted to verify closed-loop performance and circuit stability within the test conditions ranging from 7.5 kW to 15 kW. The comparison of simulated and experimental waveforms aimed to assess the alignment of differences and trends in small-signal modeling and practical measurements appropriately. The results are shown in Figures 17 and 18, respectively.



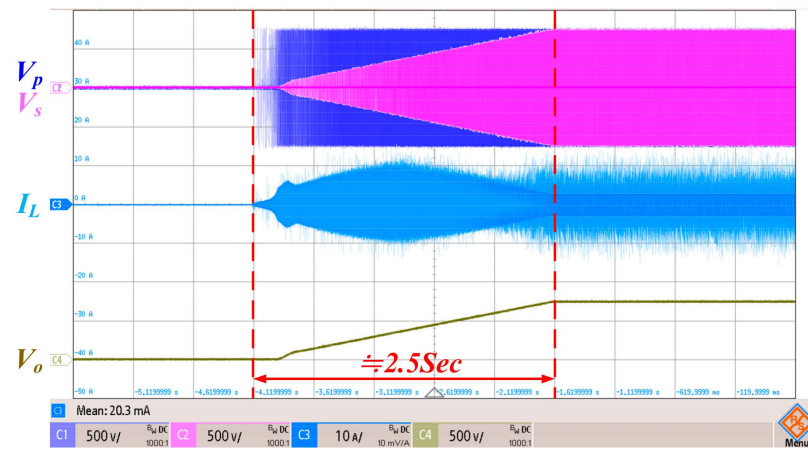
**Figure 13.** Simulation waveform of TPS load variation from 4.5 kW to 7.5 kW ( $V_o = 250$  V) ( $I_L$ : 20 A/div,  $V_o$ : 2 V/div; time: 10 ms/div).



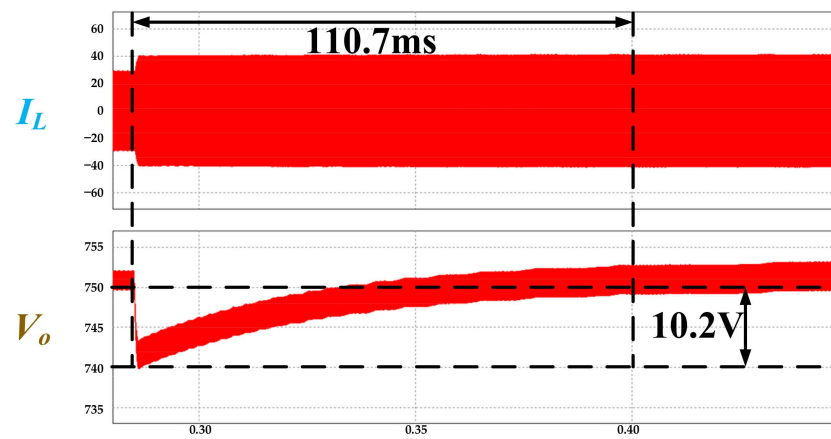
**Figure 14.** Experimental waveform of TPS load variation from 4.5 kW to 7.5 kW ( $V_o = 250$  V) ( $I_L$ : 20 A/div,  $V_o$ : 5 V/div; time: 5 ms/div).



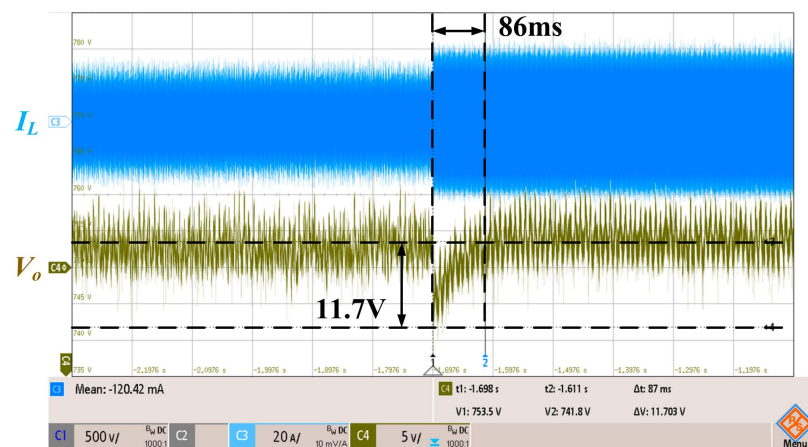
**Figure 15.** Simulation waveform of TPS soft start with  $V_o = 750$  V ( $V_p$ : 500 V/div;  $V_s$ : 100 V/div;  $I_L$ : 5 A/div; time: 500 ms/div).



**Figure 16.** Experimental waveform of TPS soft start with  $V_o = 750$  V ( $V_p$ : 500 V/div;  $V_s$ : 100 V/div;  $I_L$ : 5 A/div; time: 500 ms/div).



**Figure 17.** Simulation waveform of TPS load variation from 7.5 kW to 15 kW ( $V_o = 750$  V) ( $I_L$ : 20 A/div;  $V_o$ : 5 V/div; time: 50 ms/div).



**Figure 18.** Experimental waveform of TPS load variation from 7.5 kW to 15 kW ( $V_o = 750$  V) ( $I_L$ : 20 A/div;  $V_o$ : 5 V/div; time: 100 ms/div).

### 5.2. Switching Waveform Comparison of SPS and TPS

TPS modulation controls multiple current transitions. For example, for the primary side voltage  $V_p$  from the Lo to Hi state  $t_{1LH}$ , the inductor current must be sufficiently negative to achieve the ZVS of  $Q_1$  and  $Q_2$ . For the secondary side voltage  $V_s$  from the Lo

to Hi state  $t_{2LH}$ , the inductor current must be sufficiently positive to achieve the ZVS of  $Q_5$  and  $Q_6$ . For  $V_p$  from the Hi to Lo state  $t_{1HL}$ , the inductor current must be sufficiently positive to achieve the ZVS of  $Q_3$  and  $Q_4$ , and for  $V_s$  from the Hi to Lo state  $t_{2HL}$ , the inductor current must be sufficiently negative to achieve the ZVS of  $Q_7$  and  $Q_8$ . However, all these operations must be established to realize ZVS. When the output power increase, the Minimum Peak Current control will take over. In Figure 19, the experimental of TPS modulation waveform corresponds to a 250 V output, while Figure 20 represents a 750 V output. Each of these waveforms illustrates the switching current points under light load and heavy load conditions, respectively.

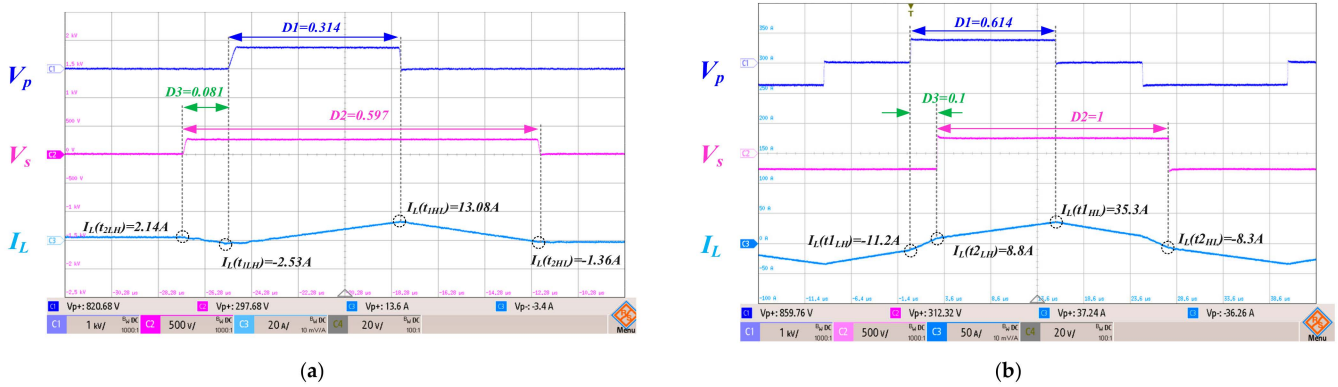


Figure 19. TPS Waveform of  $V_o = 250$  V. (a) 1 kW (Case2, SM1), (b) 7.5 kW (Case2, SM3\*) ( $V_p$ : 1 kV/div;  $V_s$ : 500 V/div;  $I_L$ : 20 A/div in (a),  $I_L$ : 50 A/div in (b), time: 2  $\mu$ s/div).

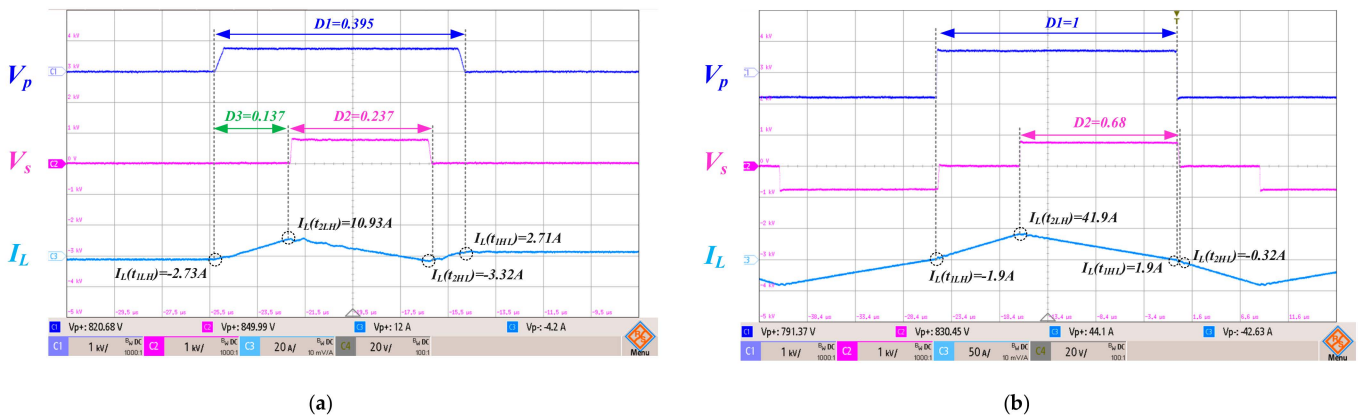
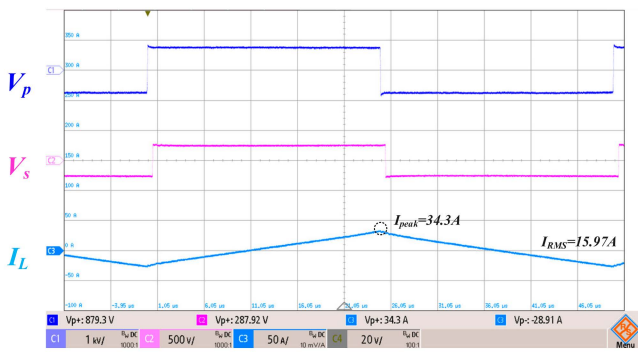


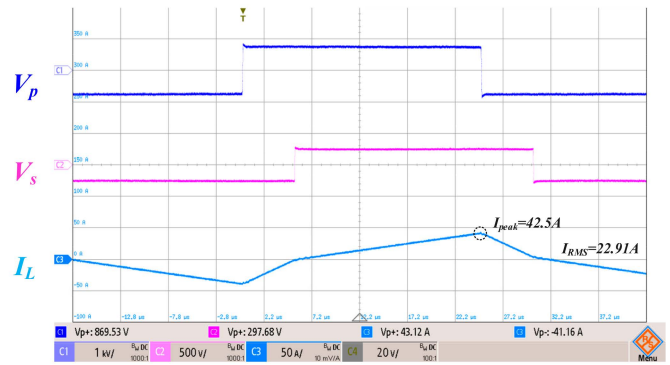
Figure 20. TPS Waveform of  $V_o = 750$  V. (a) 1 kW (Case1, SM1), (b) 15 kW (Case1, SM3\*) ( $V_p/V_s$ : 1 kV/div;  $I_L$ : 20 A/div in (a),  $I_L$ : 50 A/div in (b), time: 2  $\mu$ s/div).

Compared with TPS, SPS modulation only controls the phase shift angle between the primary and secondary sides, which will generate redundant current, thereby causing enormous switching loss at light loads and unnecessary RMS or peak current at heavy loads. In Figure 21, the experimental of SPS modulation waveform corresponds to a 250 V output, while Figure 22 represents a 750 V output. Each of these waveforms illustrates the switching current points under light load and heavy load conditions, respectively.



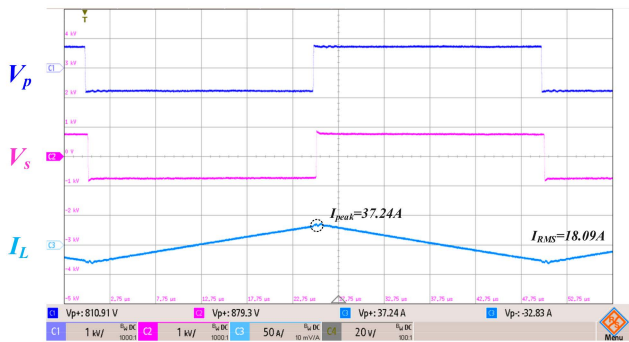


(a)

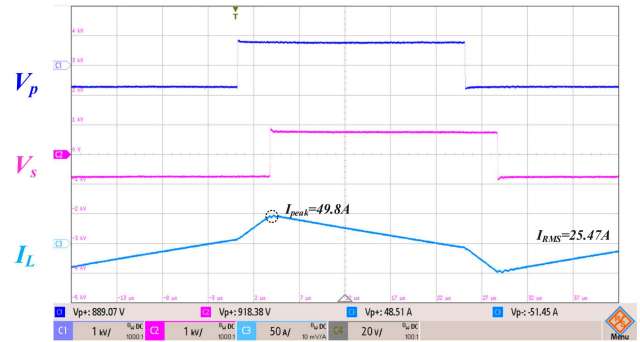


(b)

Figure 21. SPS Waveform of  $V_o = 250$  V. (a) 1 kW, (b) 7.5 kw ( $V_p$ : 1 kV/div;  $V_s$ : 500 V/div;  $I_L$ : 50 A/div; time: 5  $\mu$ s/div).



(a)

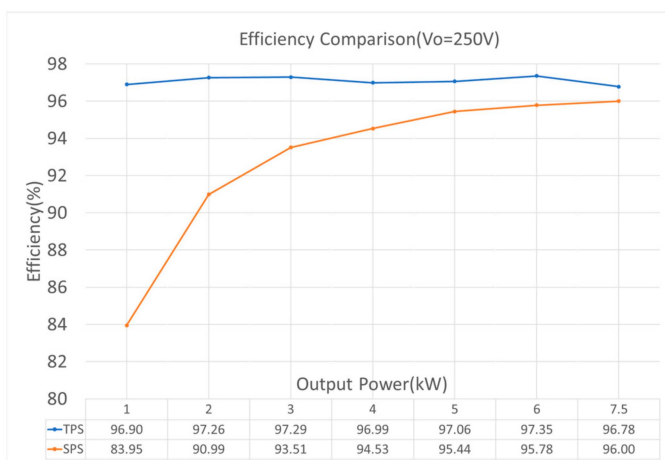


(b)

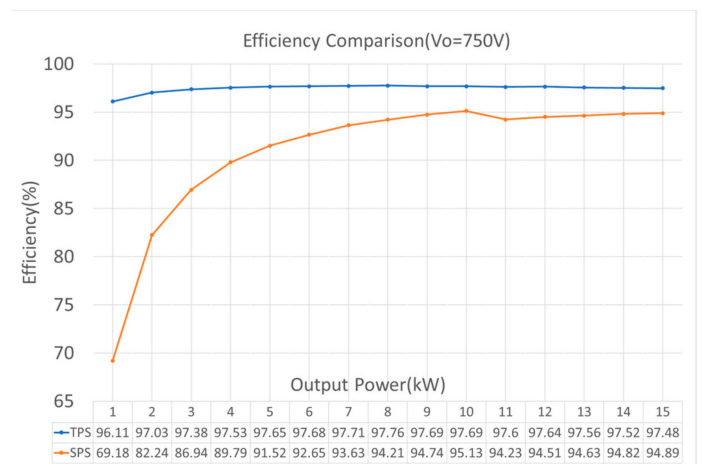
Figure 22. SPS Waveform of  $V_o = 750$  V. (a) 1 kW, (b) 15 kW ( $V_p/V_s$ : 1 kV/div;  $I_L$ : 50 A/div; time: 5  $\mu$ s/div).

### 5.3. Efficiency Comparison

Figure 23 shows the measured efficiency curves at output voltage conditions of 250 and 750 V. High efficiency performance can be achieved at a wide range of output voltages.



(a)



(b)

Figure 23. Measured efficiency curves at (a) 250 V and (b) 750 V output voltage conditions.

## 6. Conclusions

In this paper, we present a high-efficiency dual-active-bridge converter with an optimal control method using triple-phase-shift (TPS) modulation for the battery charger of electric vehicles. This approach eliminates switching losses through an ALL-ZVS mode under light loads and improves conduction losses through Minimum Peak Current mode once the load current is sufficient to allow all switches to enter ZVS. Additionally, we address and propose Ambiguous mode to resolve issues arising at the boundary between these two modes. Based on the above, this research simplifies controller's calculations and reduces analysis workload by offering a convergent approach to determine the number of TPS operation modes (*Case 1 SM1*, *Case 1 SM3\**, *Case 2 SM1* and *Case 2 SM3\**) that necessitate analysis within the small-signal model. It also ensures the circuit's stability when operating under these selected modes, that it is accurately modeled by GAM, and that the derived results are verified through simulation and experiment. Finally, a 15 kW test platform is used to validate the design. The soft-start function, transient response, and TPS and SPS modulation efficiency comparison are presented. Finally, this platform achieves 97.71% and 97.76% efficiencies at 250 V/7.5 kW and 750 V/8 kW, respectively, which obtained 26.93% and 2.59% efficiency improvement at 750 V/1 kW and 750 V/15 kW through the All-ZVS mode and the Minimum Peak Current mode, respectively.

**Author Contributions:** Conceptualization, S.-h.K.; Methodology, T.-W.H.; Software, C.-W.C.; Investigation, C.-W.C.; Data curation, S.-h.K. and Y.-C.C.; Writing—original draft, S.-h.K. and Y.-C.C.; Writing—review & editing, S.-h.K., H.-J.C., S.B., S.P., M.J. and M.T.; Visualization, S.B., S.P., M.J. and M.T.; Supervision, H.-J.C., T.-W.H. and Y.-C.C.; Project administration, H.-J.C. and T.-W.H. All authors have read and agreed to the published version of the manuscript.

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**Conflicts of Interest:** The authors declare no conflict of interest.

## Appendix A

The detailed small-signal coefficient terms of the variables in each Equations (15)–(19) have been arranged to correspond to (A1) to (A5) for matrices  $A$ ,  $B$ ,  $C$  and  $D$ .

$$\begin{aligned} \frac{d}{dt} \Delta i_{L_{1R}} = & \Delta i_{L_{1R}} \times \frac{-R_t}{L_t} \\ & + \Delta i_{L_{1I}} \times \omega_s \\ & + \Delta v_{in_0} \times \frac{\sin(2\pi D_1)}{\pi L_t} \\ & + \Delta v_{o_0} \times \frac{-N}{\pi L_t} [\sin[\pi(D_1 + D_2 + 2D_\varphi)] - \sin[\pi(D_1 - D_2 + 2D_\varphi)]] \\ & + \Delta d_1 \times \frac{1}{L_t} \left[ \begin{aligned} & 2 \cos(2\pi D_1) \times V_{in_0} \\ & - NV_{o_0} \times [\cos[\pi(D_1 + D_2 + 2D_\varphi)] - \cos[\pi(D_1 - D_2 + 2D_\varphi)]] \end{aligned} \right] \\ & + \Delta d_2 \times \frac{-N}{L_t} [V_{o_0} \times [\cos[\pi(D_1 + D_2 + 2D_\varphi)] + \cos[\pi(D_1 - D_2 + 2D_\varphi)]]] \\ & + \Delta d_\varphi \times \frac{-N}{L_t} [2V_{o_0} \times [\cos[\pi(D_1 + D_2 + 2D_\varphi)] - \cos[\pi(D_1 - D_2 + 2D_\varphi)]]] \end{aligned} \quad (A1)$$

$$\begin{aligned} \frac{d}{dt} \Delta i_{L_{1I}} = & \Delta i_{L_{1R}} \times (-\omega_s) \\ & + \Delta i_{L_{1I}} \times \frac{-R_t}{L_t} \\ & + \Delta v_{in_0} \times \frac{\cos(2\pi D_1) - 1}{\pi L_t} \\ & + \Delta v_{o_0} \times \frac{-N}{\pi L_t} [\cos[\pi(D_1 + D_2 + 2D_\varphi)] - \cos[\pi(D_1 - D_2 + 2D_\varphi)]] \\ & + \Delta d_1 \times \frac{-1}{L_t} \left[ \begin{aligned} & 2 \sin(2\pi D_1) \times V_{in_0} \\ & + NV_{o_0} \times [\sin[\pi(D_1 - D_2 + 2D_\varphi)] - \sin[\pi(D_1 + D_2 + 2D_\varphi)]] \end{aligned} \right] \\ & + \Delta d_2 \times \frac{-N}{L_t} [V_{o_0} \times [-\sin[\pi(D_1 + D_2 + 2D_\varphi)] - \sin[\pi(D_1 - D_2 + 2D_\varphi)]]] \\ & + \Delta d_\varphi \times \frac{-N}{L_t} [2V_{o_0} \times [\sin[\pi(D_1 - D_2 + 2D_\varphi)] - \sin[\pi(D_1 + D_2 + 2D_\varphi)]]] \end{aligned} \quad (A2)$$

$$\begin{aligned}
\frac{d}{dt} \Delta v_{c_0} = & \Delta i_{N_0} \times \frac{-R}{C_o(R+r_c)} \\
& + \Delta v_{c_0} \times \frac{-1}{C_o(R+r_c)} \\
& + \Delta i_{L_{1R}} \times \frac{2NR}{\pi C_o(R+r_c)} [\sin[\pi(D_1 + D_2 + 2D_\varphi)] - \sin[\pi(D_1 - D_2 + 2D_\varphi)]] \\
& + \Delta i_{L_{1I}} \times \frac{2NR}{\pi C_o(R+r_c)} [\cos[\pi(D_1 + D_2 + 2D_\varphi)] - \cos[\pi(D_1 - D_2 + 2D_\varphi)]] \\
& + \Delta d_1 \times \frac{2NR}{C_o(R+r_c)} \left[ \begin{array}{l} I_{L_{1R}} \times [\cos[\pi(D_1 + D_2 + 2D_\varphi)] - \cos[\pi(D_1 - D_2 + 2D_\varphi)]] \\ + I_{L_{1I}} \times [\sin[\pi(D_1 - D_2 + 2D_\varphi)] - \sin[\pi(D_1 + D_2 + 2D_\varphi)]] \end{array} \right] \\
& + \Delta d_2 \times \frac{2NR}{C_o(R+r_c)} \left[ \begin{array}{l} I_{L_{1R}} \times [\cos[\pi(D_1 + D_2 + 2D_\varphi)] + \cos[\pi(D_1 - D_2 + 2D_\varphi)]] \\ - I_{L_{1I}} \times [\sin[\pi(D_1 + D_2 + 2D_\varphi)] + \sin[\pi(D_1 - D_2 + 2D_\varphi)]] \end{array} \right] \\
& + \Delta d_\varphi \times \frac{2NR}{C_o(R+r_c)} \left[ \begin{array}{l} 2I_{L_{1R}} \times [\cos[\pi(D_1 + D_2 + 2D_\varphi)] - \cos[\pi(D_1 - D_2 + 2D_\varphi)]] \\ + 2I_{L_{1I}} \times [\sin[\pi(D_1 - D_2 + 2D_\varphi)] - \sin[\pi(D_1 + D_2 + 2D_\varphi)]] \end{array} \right]
\end{aligned} \tag{A3}$$

$$\begin{aligned}
\frac{d}{dt} \Delta v_{o_0} = & \Delta i_{N_0} \times \frac{-R \times r_c}{R+r_c} \\
& + \Delta v_{c_0} \times \frac{R}{R+r_c} \\
& + \Delta i_{L_{1R}} \times \frac{2NRr_c}{\pi(R+r_c)} [\sin[\pi(D_1 + D_2 + 2D_\varphi)] - \sin[\pi(D_1 - D_2 + 2D_\varphi)]] \\
& + \Delta i_{L_{1I}} \times \frac{2NRr_c}{\pi(R+r_c)} [\cos[\pi(D_1 + D_2 + 2D_\varphi)] - \cos[\pi(D_1 - D_2 + 2D_\varphi)]] \\
& + \Delta d_1 \times \frac{2NRr_c}{R+r_c} \left[ \begin{array}{l} I_{L_{1R}} \times [\cos[\pi(D_1 + D_2 + 2D_\varphi)] - \cos[\pi(D_1 - D_2 + 2D_\varphi)]] \\ + I_{L_{1I}} \times [\sin[\pi(D_1 - D_2 + 2D_\varphi)] - \sin[\pi(D_1 + D_2 + 2D_\varphi)]] \end{array} \right] \\
& + \Delta d_2 \times \frac{2NRr_c}{R+r_c} \left[ \begin{array}{l} I_{L_{1R}} \times [\cos[\pi(D_1 + D_2 + 2D_\varphi)] + \cos[\pi(D_1 - D_2 + 2D_\varphi)]] \\ - I_{L_{1I}} \times [\sin[\pi(D_1 + D_2 + 2D_\varphi)] + \sin[\pi(D_1 - D_2 + 2D_\varphi)]] \end{array} \right] \\
& + \Delta d_\varphi \times \frac{2NRr_c}{R+r_c} \left[ \begin{array}{l} 2I_{L_{1R}} \times [\cos[\pi(D_1 + D_2 + 2D_\varphi)] - \cos[\pi(D_1 - D_2 + 2D_\varphi)]] \\ + 2I_{L_{1I}} \times [\sin[\pi(D_1 - D_2 + 2D_\varphi)] - \sin[\pi(D_1 + D_2 + 2D_\varphi)]] \end{array} \right]
\end{aligned} \tag{A4}$$

$$\begin{aligned}
\frac{d}{dt} \Delta i_{o_0} = & \Delta i_{N_0} \times \frac{R}{R+r_c} \\
& + \Delta v_{c_0} \times \frac{1}{R+r_c} \\
& + \Delta i_{L_{1R}} \times \frac{2Nr_c}{\pi(R+r_c)} [\sin[\pi(D_1 + D_2 + 2D_\varphi)] - \sin[\pi(D_1 - D_2 + 2D_\varphi)]] \\
& + \Delta i_{L_{1I}} \times \frac{2Nr_c}{\pi(R+r_c)} [\cos[\pi(D_1 + D_2 + 2D_\varphi)] - \cos[\pi(D_1 - D_2 + 2D_\varphi)]] \\
& + \Delta d_1 \times \frac{2Nr_c}{R+r_c} \left[ \begin{array}{l} I_{L_{1R}} \times [\cos[\pi(D_1 + D_2 + 2D_\varphi)] - \cos[\pi(D_1 - D_2 + 2D_\varphi)]] \\ + I_{L_{1I}} \times [\sin[\pi(D_1 - D_2 + 2D_\varphi)] - \sin[\pi(D_1 + D_2 + 2D_\varphi)]] \end{array} \right] \\
& + \Delta d_2 \times \frac{2Nr_c}{R+r_c} \left[ \begin{array}{l} I_{L_{1R}} \times [\cos[\pi(D_1 + D_2 + 2D_\varphi)] + \cos[\pi(D_1 - D_2 + 2D_\varphi)]] \\ - I_{L_{1I}} \times [\sin[\pi(D_1 + D_2 + 2D_\varphi)] + \sin[\pi(D_1 - D_2 + 2D_\varphi)]] \end{array} \right] \\
& + \Delta d_\varphi \times \frac{2Nr_c}{R+r_c} \left[ \begin{array}{l} 2I_{L_{1R}} \times [\cos[\pi(D_1 + D_2 + 2D_\varphi)] - \cos[\pi(D_1 - D_2 + 2D_\varphi)]] \\ + 2I_{L_{1I}} \times [\sin[\pi(D_1 - D_2 + 2D_\varphi)] - \sin[\pi(D_1 + D_2 + 2D_\varphi)]] \end{array} \right]
\end{aligned} \tag{A5}$$

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