## DOCTORAL DISSERTATION

Title of PhD dissertation: Theoretical studies of fragmentation processes of neutral and ionized furan molecule

Title of PhD dissertation (in Polish): Teoretyczne badania procesów rozpadu neutralnej i zjonizowanej czasteczki furanu

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## Preface

Since working on my bachelor's thesis, my academic interests revolved around processes induced by collisions with ions. This curiosity stemmed from my background of physics in medicine, which I studied as a specialization at Gdańsk University of Technology. I find the physics of ion interactions with molecules very interesting mainly due to their advantageous application in radiation therapy. During my PhD studies my efforts focused on exploring the complex dynamics of excited systems with many degrees of freedom. With the increased understanding of topics in molecular physics, I became more interested in effective theoretical methodologies of modelling the molecular rearrangement and fragmentation processes.

My work substantially benefits from the collaboration between research groups initiated through the COST XLIC (XUV /X-ray light and fast ions for ultrafast chemistry) action, namely: the group of Prof. Manuel Alcamí from the Autonomous University of Madrid, Spain, the group of Dr. Paola Bolognesi from Italian National Research Council, Rome, Italy and the group of Dr. Patrick Rousseau from University of Caen, France. The research problem studied in this work formulated during my first Short-Term Scientific Mission at the Autonomous University of Madrid (AUM) in February of 2015, funded by the XLIC program. Subsequently, I was given the opportunity of two more scientific stays at the AUM (in 2016 and 2017) to obtain, review and interpret the theoretical results.

I was engaged in writing the manuscript of this thesis from April 2018 to February 2019. In the meantime, I had the opportunity of visiting ARIBE, the low-energy ion beam facility of GANIL (Grand Accélérateur National d'Ions Lourds) in Caen, France at the time when the experiment of ion collisions with furan molecules has been performed.

I would like to take this opportunity and kindly thank those, who have helped and supported me during the course of my work. To Dr. Marta Łabuda, I am extremely grateful for her guidance, kindness and unwavering support. Without her experience and attention to detail this thesis would not have been possible.

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My time spent in Madrid has always been a great learning experience, so I kindly thank Prof. Manuel Alcamí for hosting me in his group and allowing me to learn from prominent researchers.

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## Chapter 1

## Introduction

Despite the current existence of very accurate quantum chemical methods and rapid increase in the available computer power, full theoretical description of the chemical reactivity remains a difficult problem to study. On the other hand, novel light sources with XUV/X-ray attosecond pulses allow for excellent control of numerous processes and imaging of ultrafast electronic and nuclear dynamics. Still, investigations of molecular fragmentation remain complicated due to the multiplicity of active degrees of freedom. Among all possible fragmentation pathways and products, it is necessary to uncover those that are relevant to understanding the physics of the problem.

The main aim of this thesis is to investigate and understand the fragmentation process of a furan molecule with complementary theoretical methodologies. Depending on the initial charge state, the furan molecule is expected to decompose in a various ways. An additional objective is to propose and test a theoretical procedure that will provide information on the studied process and, at the same time, will be universal if applied to other systems. Moreover, as one of the steps, the present work adopts a statistical method, which is currently being developed. Due to scarce number of its applications, it is crucial to extend the scope of studied systems. Finally, direct quantitative comparison of the theoretically calculated observables with the recently obtained experimental results can provide systematic means of evaluating the accuracy and applicability of the new methodology.

The essence of this work resides in elucidating how the amount and distribution of the internal energy influences the fragmentation yields, regardless of the way it was deposited. It has been previously shown that excitation of the target is much faster than the time scale of the fragmentation. Redistribution of the excitation energy among internal degrees of freedom takes much longer time than the excitation itself. Hence, it is possible to study the fragmentation problem separately from the excitation. Then, comparison with experimental studies using electron beams, synchrotron radiation and ions as primary sources is feasible. So far, experimental measurements of furan interactions with electrons [1], [2] and synchrotron radiation [3] have already been performed. However, to the author's knowledge, this is the first presentation of the ion-induced fragmentation of furan. The newly performed experiments provide great opportunity to asses the chosen theoretical procedure and complement theoretical results.

The furan molecule has been chosen as a target for a few reasons: (1) widespread applications and model structure of the furan molecule (explained later in section 2) make it an interesting research subject; (2) furan comprises of nine atoms, which means that the application of proposed theoretical methods to such system requires sensible computational cost; (3)
the new statistical approach has been previously applied to homo-atomic clusters and heteroatomic linear systems, but has never been used to the investigation of a hetero-atomic ring molecule. Therefore, furan is a good choice for testing and improving the method; and finally (4) an extensive amount of research focused on the decomposition of the neutral furan, however, there are a few studies on the fragmentation of the singly ionized furan and only one on doubly ionized furan (only experimental). In particular, an essential role of few-particle furan cation breakups, not studied before, has been highlighted in a recent paper by Dampc et al [2].

The presented objectives will be achieved by a theoretical procedure comprising of three computational approaches: (1) ab initio Molecular Dynamics simulations describing the evolution of the system following deposition of the energy; (2) exploration of the Potential Energy Surface (PES) comprising of optimized reactants, intermediate and products at high level of theory; (3) statistical calculations employing the Microcanonical Metropolis Monte Carlo ( $\mathrm{M}_{3} \mathrm{C}$ ) method. In other words, considerations of three aspects of the studied process: dynamical, energetic and entropic are expected to create a full picture of the fragmentation mechanism.

The text of this thesis is organized as follows: next subsection of Chapter 1 introduces the physical grounds of the fragmentation process. Chapter 2 explores some general information about the furan molecule and current state of knowledge with regard to the furan fragmentation. Next, in Chapter 3 the theoretical framework applied in this work is presented. Following Chapter 4 contains computational details of the performed calculations. Chapter 5 presents obtained results, discussion and comparison with previous theoretical works and experimental measurements. Finally, Chapter 6 concludes with summary of the results and a forward look on the further research directions.

### 1.1 Fragmentation mechanism

The molecular fragmentation process can be induced in various ways, a few of which will be briefly discussed in this section. In a neutral state, fragmentation of a molecule is possible through a process of pyrolysis, meaning thermal decomposition into smaller fragments carried out at elevated temperatures (generally above $400^{\circ} \mathrm{C}$ ) in the absence of oxygen. Depending on the temperature and residence time, pyrolysis processes are typically classified as slow, moderate or fast. Another way of distinguishing the type of pyrolysis relies on the expected effect. The goal of applied pyrolysis is synthesis of certain compounds through thermal decomposition. Typical chemicals taken as a starting point include fossil fuels, biomass, wastes or polymers. Studies in applied pyrolysis investigate relationships between pyrolysis conditions and product properties, which can be subsequently characterized with such experimental methods like gas chromatography mass spectrometry, Fourier transform infrared spectrometry and nuclear magnetic resonance [4]. On the other hand, the purpose of analytical pyrolysis is characterization of the analyte through thermally induced degradation. This technique investigates chemical compositions and decomposition pathways of different materials. In practice, pyrolysis is used in many industrial applications such as conversion of oils to lighter products in the manufacture of fuels and chemical recycling of waste [5].

Further description of possible physical processes will be limited to the regime of lowenergy interactions, because this energy range is of interest to the present work. As it was mentioned earlier, interaction of ionizing radiation (photons, electron beams, ion beams) with matter can cause variety of possible processes. Gas phase collision experiments help to elucidate the very first steps of this complicated chain of events by providing well-defined laboratory conditions. On the molecular scale, radiation damage results from deposition of the energy during the collision that leads to production of excited and/or ionized states and in the case of sufficient excess energy to fragmentation through different competing pathways. Schematically, typical collisional processes of different projectiles ( $A^{q+}, e^{-}, h \nu$ ) with a molecule represented as $B C$ can be written as

Excitation occurs when deposited energy is distributed among internal degrees of freedom and leads to population of higher rovibrational and/or electronic levels (here denoted with an asterisk *)
ions: $A^{q+}+B C \rightarrow A^{* q+}+B C^{*}$
electrons: $e^{-}\left(E_{i}\right)+B C \rightarrow e^{-}\left(E_{j}\right)+B C^{*}$ where $E_{i}>E_{j}$
photons: $h \nu+B C \rightarrow B C^{*}$
Ionization takes place when absorbed energy exceeds the ionization potential of the molecule. As a results, a molecule looses electron(s), which can interact further in what is known as a secondary process
ions: $A^{q+}+B C \rightarrow A^{* q+}+B C^{*+}+e^{-}$
electrons: $e^{-}+B C \rightarrow 2 e^{-}+B C^{*+}$
photons: $h \nu+B C \rightarrow e^{-}+B C^{*+}$
Charge transfer implies electron capture by the projectile and consequential acquisition of a positive charge by the target molecule
ions: $A^{q+}+B C \rightarrow A^{*(q-r)+}+B C^{* r+}$
Fragmentation takes place when deposited energy is sufficient to break chemical bonds
into two charged species: $B C^{* s+} \rightarrow B^{* u+}+C^{*(s-u)+}$
into one charged and one netral species: $B C^{* s+} \rightarrow B^{* s+}+C^{*}$
If the fragmentation is statistical, its extent depends dramatically on the internal energy of the parent ion [6]. This implies that, prior to fragmentation, the internal excitation is completely randomized among all accessible internal degrees of freedom of the fragmenting ion. A portion of the excess internal energy is released in the relative translation of produced fragments. This energy, named kinetic energy release (KER), provides valuable information about the initial structures of the species involved and the energetics of the reaction. Its values depend on the details of the potential energy surface. The existence of reverse activation barrier, associated with the preceding isomerization, gives large KERs. Moreover, in the case of the fragmentation of multiply charged ions, large KERs result from the Coulomb repulsion between the charged fragments. KER distribution can be observed experimentally in the form of metastable peaks commonly present in mass spectra due ions dissociating in a field-free region of a mass spectrometer.

For a certain type of processes, a quantity that specifies the probability of its occurrence is known as a cross-section. In experimental studies of fragmentation and ionization, their values can be obtained by peak integration of spectra as a function of the projectile's velocity [7]. Based on this approach, theoretical investigation of charge transfer induced by collisions of carbon ions with uracil [8] showed evidence that processes of charge transfer and fragmentation are complementary.

## Chapter 2

## Furan molecule

The aim of this chapter is to present general characteristics of the furan molecule and explore studies that have already investigated fragmentation of the furan molecule. Then, a clear reference in the results section will be possible, allowing for a comprehensible comparison and emphasis on the novelty of results presented in this thesis.

Furan is a five-membered heterocyclic molecule of formula


Figure 2.1 The structural formula of furan with labelling of atoms. $\mathrm{H}_{4} \mathrm{C}_{4} \mathrm{O}$ (see Figure 2.1) with an oxygen atom in the ring. The identification of the carbon atoms bonded with the oxygen by $\alpha$ subscripts and carbons connected only to other carbons by $\beta$ subscripts simplifies the further analysis by the use of symmetry properties. The aromatic character of furan results from one of the oxygen atom's lone pairs of electrons being delocalized into the ring. This leads to $4 n+2$ aromatic system according to the Hückel's rule. Consequently, furan shows planar geometry and high reactivity in the sense of electrophilic substitution.

The geometry of the ground state furan belongs to the $\mathrm{C}_{2 v}$ symmetry point group. Overall, furan molecule contains 36 electrons occupying 18 orbitals. Figure 2.2 shows two of the outermost $\pi$ orbitals: HOMO ( $1 \mathrm{a}_{2}$ ) and HOMO-1 $\left(2 \mathrm{~b}_{1}\right)$. The first ionization energy of furan has been previously determined in the multiphoton ionization experiment as 8.886 eV [9]. The appearance energies of the doubly ionized furan have been measured in the electron impact

## HOMO




Figure 2.2 Two outermost orbitals of furan. Calculated at HF/6-311G(d,p) level of theory. Isosurface value is 0.08 .
experiment at 25.7 eV [10] and in the photoionization experiment at 25.8 eV [11]. Theoretical value of the Vertical Ionization Potential (VIP) can be calculated from the energy difference between the ionized and neutral molecules at the equilibrium geometry of the neutral state. At the B3LYP $/ 6-311++G(d, p)$ level of theory the value of the first VIP is equal to 8.93 eV and the second VIP is 25.82 eV , showing great comparison with the experimental values.

Abundance of research concerning furan stems from its various applications in pharmaceutical industry, organic synthesis and combustion chemistry, among others. Furan and its derivatives display a potential role in the second-generation biofuel production as their energy density is comparable to that of gasoline [12]. Understanding its thermal decomposition plays a role in clean coal combustion due to furan being one of the basic structure units of coal [13]. Moreover, furan and furan analogues are starting points of many reactions. Wide range of applications in the medicinal chemistry results from furan's broad availability and easy functionalization [14]. Finally, major amounts of furan have been found in tobacco smoke [15] and heat treated foods [16], so its cancerogenic and toxic effects have been an objective of numerous studies.

More recently, a renewed interest in the furan molecule is due to its model structure that resembles the building block of the DNA's backbone - deoxyribose sugar. Furan can be seen as a simplified tetrahydrofuran with reduced number of hydrogens. Tetrahydrofuran, on the other hand, is often taken as an analogue of the deoxyribose. Thus, furan is a second step approximation to the DNA chain element. Investigations regarding effects of the ionizing radiation on the biological tissue span over decades of extensive and notable research. Double-strand breaks of the DNA chain play a major role in the cell death because they are exceptionally difficult to repair [17]. Ionizing radiation causes numerous types of damage to the DNA, but double-strand breaks are the most biologically effective [18]. Moreover, it has been recently shown that on the molecular level the source of significant DNA damage is due to secondary particles and not the primary radiation itself [19]. Those particles include mostly low-energy electrons [20], but also radicals [21] as well as singly and multiply charged ions [7], [8]. To this day, numerous theoretical and experimental investigations are devoted to extending our understanding of how radiation modifies a biological system.

### 2.1 Fragmentation of neutral furan

Numerous studies can be found in the literature on the pyrolysis of furan from both the experimental and the theoretical perspectives. The first investigation on the very low pressure furan pyrolysis over the temperatures of 1050-1270 K has been published in 1985 by Grela et al [22]. The only two products that have been measured were CO and $\mathrm{H}_{4} \mathrm{C}_{3}$. A year later, Lifshitz et al [23] applied a single pulse shock tube technique over the temperatures of 1050-1460 K. As a result, they proposed furan pyrolysis to be a two-channel process of decomposition to $\mathrm{CO} / \mathrm{H}_{3} \mathrm{CCCH}$ and $\mathrm{HCCH} / \mathrm{H}_{2} \mathrm{CCO}$. However, they were unable to detect ketene $\left(\mathrm{H}_{2} \mathrm{CCO}\right)$, probably due to its high reactivity toward water that was absored on the walls of the shock tube. Then, in 1991, Organ and Mackie [24] extended the understanding of furan pyrolysis by application of the time-resolved infrared absorption spectrometry together with single pulse
shock tube method over the temperatures of 1100-1700 K. Similarly to Lifshitz et al, they obtained $\mathrm{CO}, \mathrm{H}_{4} \mathrm{C}_{3}, \mathrm{H}_{2} \mathrm{C}_{2}$ as major products, but were able to detect $\mathrm{H}_{2} \mathrm{CCO}$ as well. Additionally, they proposed a third minor channel of furan decomposition to be $\mathrm{HCO} / \mathrm{H}_{3} \mathrm{C}_{3}$. However, this channel has been determined as unlikely by Fulle et al [25] in the combined experiment of the time-of-flight (TOF) and the shock tubes techniques. The absence of the third channel was explained by the high heat of that reaction in comparison with the other two channels. Fulle et al suggested that the observation of HCO and $\mathrm{H}_{3} \mathrm{C}_{3}$ might have resulted from the dissociation of the primary products or impurity initiation. All four groups suggested the rate determining step to be the CO scission and production of the intermediate open-chain biradical, which rapidly fragments to various products.

In 1998, Liu et al [26] published the first quantum chemical study of the unimolecular decomposition of furan. The calculations were carried out using density functional theory (B3LYP) for optimization of the geometries and the QCISD(T) method for the energies. They investigated three decomposition pathways and concluded that CO and $\mathrm{H}_{3} \mathrm{CCCH}$ should be the major products of furan pyrolysis with HCCH and $\mathrm{H}_{2} \mathrm{CCO}$ being distinguishable, but contributing to a minor extend. They proposed that the most favourable mechanism of obtaining channel $\mathrm{CO} / \mathrm{H}_{3} \mathrm{CCCH}$ relies on the $2,1 \mathrm{H}$ shift, ring opening, two more hydrogen transfers and $\mathrm{C}_{\beta}(3)-\mathrm{C}_{\alpha}(4)$ bond cleavage resulting in fragmentation. Production of channel $\mathrm{HCCH} / \mathrm{H}_{2} \mathrm{CCO}$, on the other hand, implies $1,2 \mathrm{H}$ shift and concerted $\mathrm{C}_{\alpha}(1)-\mathrm{O}$ and $\mathrm{C}_{\beta}(2)-\mathrm{C}_{\beta}(3)$ bonds fission.

The first experimental observation of channel $\mathrm{HCO} / \mathrm{H}_{3} \mathrm{C}_{3}$ taking place directly from furan has been published by Sorkhabi et al [27]. By the use of photofragment translational spectroscopy at 196 nm with tunable vacuum ultraviolet probe, they provided evidence of an anisotropic angular distribution, indicating a swift dissociation process characteristic for radical channels such as $\mathrm{HCO} / \mathrm{H}_{3} \mathrm{C}_{3}$. Moreover, they concluded that this channel likely occurs on an electronically excited PES, due to higher energies provided in the photodissociation experiment compared to that of pyrolysis. The mechanism of producing channel $\mathrm{HCO} / \mathrm{H}_{3} \mathrm{C}_{3}$ has been proposed to consist of ring scission, followed by a 2,3 hydrogen transfer and a $\mathrm{C}_{\beta}(3)-\mathrm{C}_{\alpha}(4)$ bond cleavage. The concerted mechanism of obtaining this channel has been identified as unlikely on the basis of measured translational energy of produced fragments.

The most extensive theoretical investigation of furan unimolecular decomposition with high level ab initio quantum chemistry (calculated at CASSCF, CASPT2 and G2-(MP2) levels of theory) and kinetic modelling methods has been performed by Sendt et al [28]. Unlike Liu et al [26], this study contains calculation of rate parameters that allow for a comparison with experimental studies. The crucial conclusion has been made that instead of $\mathrm{C}-\mathrm{O}$ or $\mathrm{C}-\mathrm{H}$ bond cleavages being the first steps, the $1,2-\mathrm{H}$ transfers leading to cyclic carbenes initiate production of the observed species. Their calculations indicate two parallel channels: $\mathrm{CO} / \mathrm{H}_{3} \mathrm{CCCH}$ and $\mathrm{HCCH} / \mathrm{H}_{2} \mathrm{CCO}$, former being the dominant one. Direct ring cleavage, on both singlet and triplet PES, has been found to be much too energetic to contribute appreciably to the furan thermal decomposition. Similarly, the high activation energy required to produce channel $\mathrm{HCO} / \mathrm{H}_{3} \mathrm{C}_{3}$ ruled out this mechanism as a way of obtaining $\mathrm{H}_{3} \mathrm{C}_{3}$. Instead, $\mathrm{H}_{3} \mathrm{C}_{3}$ radicals have been suggested to arise from secondary decomposition of $\mathrm{H}_{4} \mathrm{C}_{3}$.

The first experimental study showing that $\mathrm{H}_{3} \mathrm{C}_{3}$ radicals are produced also in the thermal
decomposition has been published in 2009 by Vasillou et al [29]. There, it has been shown with the use of the high-temperature supersonic nozzle technique combined with IR spectroscopy that these radical species are produced from furan at a higher temperature of $1550 \pm 100 \mathrm{~K}$. The work of Vasillou et al [29] has been complemented by ab initio electronic structure calculations that further confirm that all of the furan fragmentation processes occur after rearrangement to either the $\alpha$-carbene or $\beta$-carbene.

Combustion of furan in premixed furan/oxygen/argon flames has been studied by Tian et al [30] with tunable synchrotron VUV photoionization and molecular-beam mass spectrometry. Consumption of furan under different flames conditions has been investigated. Therein, it has been concluded that in the temperature range characteristic to pyrolysis the model of furan combustion fits best with the predictions of Sendt et al [28]. Moreover, they concluded that the hydrogen abstraction and decomposition of resulting furyl radicals may play a crucial role under high temperatures.

In 2013, Urness et al [31] performed the pyrolysis experiment of furan over the temperatures of 1200-1600 K in a microreactor. To confirm the most probable pathway of unimolecular decomposition, they measured branching ratios of intermediate species as a function of temperature with the tunable synchrotron radiation photoionization mass spectrometry. Specifically, they measured branching ratios of $\beta$-carbene to $\alpha$-carbene and propargyl radical to propyne ( $\left.\left[\mathrm{H}_{2} \mathrm{CCH}\right] /\left[\mathrm{H}_{3} \mathrm{CCCH}\right]\right)$. It has been shown that $80 \%$ to $90 \%$ decomposition of furan proceeds through production of $\beta$-carbene. Moreover, no evidence of propargyl radicals has been found in the temperature range of $1200-1500 \mathrm{~K}$. For higher temperatures, at most $10 \%$ of formyl allene $\left(\mathrm{H}_{2} \mathrm{CCCHCHO}\right)$ fragments to channel $\mathrm{H}_{2} \mathrm{CCH} / \mathrm{CO} / \mathrm{H}$, as most of this intermediate fragments to $\mathrm{CO} / \mathrm{H}_{3} \mathrm{CCCH}$. These results confirmed the skeleton fragmentation to channel $\mathrm{HCO} / \mathrm{H}_{3} \mathrm{C}_{3}$ as an unlikely process.

The most recent study of furan pyrolysis over the temperature range of 1100 to 1600 K has been performed by Cheng et al in 2017 [32]. Their results are consistent with the conclusions of previous pyrolysis studies that furan mainly decomposes to CO and $\mathrm{H}_{3} \mathrm{CCCH}$. Moreover, on the basis of the mole fraction profiles and measured formation temperatures of $\mathrm{H}_{3} \mathrm{C}_{3}$, authors concluded that the mechanism of producing propargyl radicals occurs through secondary fragmentation of propyne. Authors highlighted the importance of understanding the production mechanism of propargyl radicals due to their significant role as precursors of large aromatics formation in the pyrolysis of furan.

Summary of the experimentally observed fragmentation channels is presented in Table 2.1.
TABLE 2.1 Neutral furan fragmentation channels.

|  | $\rightarrow \mathrm{CO}+\mathrm{H}_{4} \mathrm{C}_{3}$ | [22]-[25], [27], [29]-[32] |
| ---: | :--- | :--- |
| Furan | $\rightarrow \mathrm{H}_{2} \mathrm{C}_{2}+\mathrm{H}_{2} \mathrm{C}_{2} \mathrm{O}$ | $[23]-[25],[27],[29]-[32]$ |
|  | $\rightarrow \mathrm{HCO}+\mathrm{H}_{3} \mathrm{C}_{3}$ | $[24],[27],[29]$ |
|  | $\rightarrow \mathrm{H}+\mathrm{CO}+\mathrm{H}_{3} \mathrm{C}_{3}$ | $[31],[32]$ |

### 2.2 Fragmentation of charged furan

Previous studies of ionization and subsequent fragmentation of furan molecules have been studied using various experimental techniques, such as charge-exchange mass spectrometry [33], [34], electron impact [2], [35]-[37], photoelectron-photoion coincidence (PEPICO) spectroscopy [11], [38], [39] and multiphoton mass spectrometry [40], [41].

The first study determining the charge-exchange mass spectra in collisions of furan molecules with wide range of reagent ions has been published in 1971 by Derrick et al [33]. They concluded that for primary ions of $11-12 \mathrm{eV}$ of recombination energy three main channels were $\mathrm{H}_{4} \mathrm{C}_{3}^{+} / \mathrm{CO}, \mathrm{H}_{2} \mathrm{C}_{2} \mathrm{O}^{+} / \mathrm{H}_{2} \mathrm{C}_{2}$ and $\mathrm{H}_{3} \mathrm{C}_{3}^{+} / \mathrm{HCO}$. At higher energies, channels $\mathrm{H}_{3} \mathrm{C}_{4} \mathrm{O}^{+} / \mathrm{H}$ and $\mathrm{HCO}^{+} / \mathrm{H}_{3} \mathrm{C}_{3}$ have been observed as well. Later, in 1980, Tedder et al [34] employed the same experimental technique, and extended the understanding of ionized furan fragmentation by reporting Appearance Energies (AEs) of the three most abundant ions.

The earliest work on decomposition of furan upon electron impact has been performed by Williams et al in 1968 [35]. The mass spectrum of furan has been measured at beam energy of 18 eV and reported three charged fragments: $\mathrm{H}_{3} \mathrm{C}_{3}^{+}, \mathrm{H}_{4} \mathrm{C}_{3}^{+}$and $\mathrm{H}_{2} \mathrm{C}_{2} \mathrm{O}^{+}$. Moreover, mass spectrum of deuterium labeled furan led to the conclusion that either hydrogen randomization does not take place in furan prior to fragmentation, or occurs slowly compared to the rate of fragmentation. Then, in 1979, Holmes and Terlouw [36] reported the 70 eV electron beam Collisional Activation spectrum of furan ions, which consisted of three main peaks corresponding to $\mathrm{H}_{4} \mathrm{C}_{3}^{+}, \mathrm{H}_{3} \mathrm{C}_{3}^{+}$and $\mathrm{H}_{2} \mathrm{C}_{3}^{+}$with Relative Abundances (RA) of $20 \%, 100 \%$ and $29 \%$, respectively. On the basis of the obtained kinetic energy distribution, wide range of kinetic energies released upon CO loss from furan cation was the evidence of substantial energy required to reach the transition state prior to fragmentation. Moreover, the shape of the kinetic energy distribution implied that production of more than one isomer of $\mathrm{H}_{4} \mathrm{C}_{3}^{+}$is possible. Three years later, Burgers et al [37] reported collisional activation mass spectra for various $\mathrm{H}_{4} \mathrm{C}_{4} \mathrm{O}^{+}$ions and wider range of mass over charge ratios. For furan cation fragmentation, additional observation has been made of $\mathrm{HCO}^{+}$and $\mathrm{H}_{4} \mathrm{C}_{3} \mathrm{O}^{+}$fragments, among others. More recently in 2015, ionization and fragmentation of furan has been studied by Dampc et al [2]. Cation mass spectrum at electron energy of 100 eV and absolute total and partial ionization cross sections at energy range of $5-150 \mathrm{eV}$ were measured. With comparable intensity two ionic species dominate the mass spectrum: $\mathrm{H}_{3} \mathrm{C}_{3}^{+}$(Relative Abundance $(R A)=100 \%$ ) and $\mathrm{H}_{4} \mathrm{C}_{4} \mathrm{O}^{+}(\mathrm{RA}=94 \%)$. Intensities of remaining ions did not exceed $15 \%$, highest of which were fragments $\mathrm{H}_{4} \mathrm{C}_{3}^{+}$( $\mathrm{RA}=15 \%$ ) and $\mathrm{HCO}^{+}(\mathrm{RA}=12 \%)$. Authors highlighted the need for ab initio calculations that could provide more insight into such high abundance of $\mathrm{H}_{3} \mathrm{C}_{3}^{+}$. Moreover, Appearance Energies of various charged fragments have been determined. Those values will be later compared with energy barriers calculated in this work. Due to high AEs of some ionic fragments the possibility of multiple-step fragmentation has been pointed out. Moreover, the formation mechanism of the most abundant fragmentation products has been proposed as simultaneous cleavage of two bonds, the $\mathrm{C}_{\alpha}(1)-\mathrm{O}$ and the $\mathrm{C}_{\beta}(3)-\mathrm{C}_{\alpha}(4)$ or $\mathrm{C}_{\beta}(2)-\mathrm{C}_{\beta}(3)$. This statement can be verified by the calculations performed in this work.

In 1980, Willet and Bear were the first to apply threshold PEPICO technique to study the
dissociation of state-selected furan ions [38]. AEs of four fragments: $\mathrm{H}_{4} \mathrm{C}_{3}^{+}, \mathrm{H}_{2} \mathrm{C}_{2} \mathrm{O}^{+}, \mathrm{H}_{3} \mathrm{C}_{3}^{+}$ and $\mathrm{HCO}^{+}$have been reported. Furan ion has been found to be metastable. Identical rates for production of ions $\mathrm{H}_{4} \mathrm{C}_{3}^{+}$and $\mathrm{H}_{2} \mathrm{C}_{2} \mathrm{O}^{+}$indicated that channels producing these fragments have been found to be in competition in the energy range of $11.5-13 \mathrm{eV}$. Moreover, on the basis of rate and kinetic energy release data authors argued that in the near threshold region $\mathrm{H}_{4} \mathrm{C}_{3}^{+}$ ion was the most likely produced in the allene from $\left(\mathrm{H}_{2} \mathrm{CCCH}_{2}^{+}\right)$. Also, it has been suggested that fragmentation to $\mathrm{H}_{2} \mathrm{C}_{2} \mathrm{O}^{+}$and $\mathrm{H}_{3} \mathrm{C}_{3}^{+}$proceeds through one transition state, without additional isomerization. A need for further studies explaining increasing rate of $\mathrm{H}_{3} \mathrm{C}_{3}^{+}$have been expressed in this study. Further investigations of photoabsorption, photoelectron and photoion spectroscopy have been performed in 1998 by Rennie et al [11] and extended in 2001 by threshold-PEPICO measurements [39]. In [11] TOF mass spectrum has been reported at the photon energy of 27.2 eV . Moreover, normalised intensities of sixteen fragment ions as a function of the photon energy have been measured in the photon energy range $12-26 \mathrm{eV}$ and their AEs have been presented. In addition, $a b$ initio calculations have been performed for fragmentation pathways to channels $\mathrm{H}_{2} \mathrm{CCC}_{2}^{+} / \mathrm{CO}$ and $\mathrm{H}_{3} \mathrm{CCCH}^{+} / \mathrm{CO}$, concluding that production of $\mathrm{H}_{4} \mathrm{C}_{3}^{+}$ion in the allene form is more favourable. For higher photon energies, production mechanism of the $\mathrm{H}_{2} \mathrm{C}_{4} \mathrm{O}^{+}$ion has been explained as sequential loss of two hydrogen atoms. Moreover, metastable route of $\mathrm{H}_{3} \mathrm{C}_{3}^{+} \rightarrow \mathrm{H}_{3} \mathrm{C}_{2}^{+} \rightarrow \mathrm{HC}_{3}^{+}$has been suggested. More insight into furan cation fragmentation has been provided by the threshold PEPICO measurement [39]. On the basis of fitting of the RRKM/QET calculations with the experimental data, authors deduced barrier heights for channels $\mathrm{H}_{4} \mathrm{C}_{3}^{+} / \mathrm{CO}, \mathrm{H}_{2} \mathrm{C}_{2} \mathrm{O}^{+} / \mathrm{H}_{2} \mathrm{C}_{2}$ and $\mathrm{H}_{3} \mathrm{C}_{3}^{+} / \mathrm{HCO}$ as 2.75 eV , 2.88 eV and 3.05 eV , respectively. Moreover, measurements of the breakdown curves have been extended to the photon energy of $12-30 \mathrm{eV}$. In the energy range of $14-20 \mathrm{eV} \mathrm{H}_{3} \mathrm{C}_{3}^{+}$has been found to be the most prominent fragment. Their RRKM/QET calculations did not account for sequential process, but authors suggested that this ion could have been produced from $\mathrm{H}_{4} \mathrm{C}_{3}^{+}$, provided it carried sufficient energy for further fragmentation. Ion $\mathrm{H}_{2} \mathrm{C}_{3}^{+}$has been suggested to most likely result from channel $\mathrm{H}_{2} \mathrm{C}_{3}^{+} / \mathrm{H}_{2} \mathrm{CO}$. Authors emphasize possible high values of the kinetic shift in higher energy channels due to the slow onset at threshold.

In a very recent study of unimolecular dissociative photoionization mechanism of furfural (furan-2-carbaldehyde) [42] it has been suggested that the furan breakdown diagram is contained within the one obtained for furfural. Authors calculated potential energy surface of fragmentation of furan cation to three channels: $\mathrm{H}_{4} \mathrm{C}_{3}^{+} / \mathrm{CO}, \mathrm{H}_{2} \mathrm{C}_{2} \mathrm{O}^{+} / \mathrm{H}_{2} \mathrm{C}_{2}$ and $\mathrm{HCO}^{+} / \mathrm{H}_{3} \mathrm{C}_{3}$ at the CBS-QB3 level of theory. However, the presence of $\mathrm{H}_{3} \mathrm{C}_{3}^{+}$ions has been attributed to direct fragmentation of furfural.

Fragmentation of furan cation has been also studied with the infrared multiphoton dissociation technique by Wu et al [40], where intensities of fragments $\mathrm{H}_{4} \mathrm{C}_{3}^{+}$and $\mathrm{H}_{2} \mathrm{C}_{2} \mathrm{O}^{+}$as a function of laser power have been reported. Authors concluded that although it has been previously suggested that these fragments proceed through a common transition state, their results indicate that this is not the case and stepwise photoexcitation leads to prompt fragmentation producing mostly $\mathrm{H}_{4} \mathrm{C}_{3}^{+}$. Moreover, in the study of resonance enhanced multiphoton ionization combined with TOF mass spectrometry by Ridley et al [41] the mass spectra of furan at different laser wavelengths ( $308-363 \mathrm{~nm}$ ) have been reported. Therein, it has been concluded
that the extent of fragmentation has been determined by the laser wavelength reaching or exceeding the ionization potential of the orbitals attributed to the $\mathrm{C}-\mathrm{C}, \mathrm{C}-\mathrm{O}$, and $\mathrm{C}-\mathrm{H}$ bonds and that there should be resonant intermediate states for efficient ionization.

The only investigation available in the literature of furan fragmentation following double ionization has been performed by Pešić et al [3]. This study employed the momentum-resolved coincidence ion spectroscopy and reported the kinetic energy distribution and momentum correlation between coincident ions. The abundance of detected small fragments results from K-shell ionization induced by 548 eV photons. Inner-shell excitations lead to high probability of four- or five-body reactions. Interestingly, authors were able to assign observed fragmentation channels as concerted, secondary decay, or deferred based on the measured momentum correlations and the constructed model. However, comparison between the present study and the results of Pešić et al [3] is inadequate as this work investigates fragmentation channels after valence-shell ionization, which results in larger-mass fragments.

In summary, the abundance of research has already focused on the fragmentation of charged furan, but there still remains a few unclear issues: (1) the high intensity of fragment $\mathrm{H}_{3} \mathrm{C}_{3}^{+}$has not been supported by theory, (2) only two-body fragmentation has been previously theoretically investigated, but already at 13 eV sequential fragmentation can play a role in decomposition of furan cation, (3) no ab initio investigation on the fragmentation of doubly ionized furan has been performed. The comparison only with the results by Rennie et al [11], [39] and Dampc et al [2] will be made in the later chapter due to their recent and detailed quality.

## Chapter 3

## Theoretical methods

Quantum chemistry methods enable investigation of molecular systems by approximating the solution to the fundamental equation of quantum mechanics, the Schrödinger equation. Its exact analytic solution is only possible for small subset of physical systems. In practice, approximations must be applied, which naturally decrease the accuracy of the obtained result. The computational complexity of a selected method often substantially limits the range of possible applications. However, with advances made in development of theoretical methods and increase in availability of supercomputing resources, more and more complex systems are feasible to study with great accuracy.

The goal of this chapter is to formulate essential framework of three theoretical methodologies applied in this work. On the basis of following sections, their complementary character is emphasized as well as their role in describing the process of interest - fragmentation. Firstly, the fundamental approximation of the electronic structure theory: the Born-Oppenheimer approximation is presented. Next section introduces density functional theory as a powerful tool to solve the time-independent Schrödinger equation. Then, as a way elucidating the dynamical evolution of the system, a family of $a b$ initio Molecular Dynamics methods is presented. Final section describes a recently developed, statistical technique based on the Metropolis Monte Carlo algorithm of the microcanonical ensemble.

Theoretical considerations presented in this chapter employ atomic units, i.e. by definition $m_{e}=\hbar=e_{0}=4 \pi \varepsilon_{0}=1$. Such approach is very convenient, especially due to a simple form of the resulting molecular Hamiltonian.

### 3.1 Born-Oppenheimer approximation

The starting point of solving stationary, quantum chemical molecular problems is a time-independent Schrödinger equation given by

$$
\begin{equation*}
\hat{H} \Psi_{k}(\boldsymbol{r}, \boldsymbol{R})=E_{k}^{t o t} \Psi_{k}(\boldsymbol{r}, \boldsymbol{R}), \tag{3.1}
\end{equation*}
$$

where Hamiltonian $\hat{H}$ operates on the wave function $\Psi_{k}$ of the $k$ th eigenstate and produces the total energy eigenvalue $E_{k}^{\text {tot }}$.

A non-relativistic Hamiltonian written in atomic units for a system of $N_{n}$ nuclei (characterized by their position vector $\boldsymbol{R}$, mass $M$ and atomic number $Z$ ) and $N_{e}$ electrons (characterized by their position vector $r$ ) consists of kinetic energy and electrostatic interactions and is given
by

$$
\begin{equation*}
\hat{H}=\sum_{A=1}^{N_{n}}-\frac{1}{2 M_{A}} \nabla_{A}^{2}+\sum_{i=1}^{N_{e}}-\frac{1}{2} \nabla_{i}^{2}-\sum_{A=1}^{N_{n}} \sum_{i=1}^{N_{e}} \frac{Z_{A}}{\left|\boldsymbol{R}_{A}-\boldsymbol{r}_{i}\right|}+\sum_{A<B}^{N_{n}} \frac{Z_{A} Z_{B}}{\left|\boldsymbol{R}_{A}-\boldsymbol{R}_{B}\right|}+\sum_{i<j}^{N_{e}} \frac{1}{\left|\boldsymbol{r}_{i}-\boldsymbol{r}_{j}\right|}, \tag{3.2}
\end{equation*}
$$

where nuclei are numbered by the $A$ subscript and electrons by the $i$ subscript. Eq. 3.2 can be rewritten in a more compact way as

$$
\begin{equation*}
\hat{H}=\hat{T}_{n}(\boldsymbol{R})+\hat{T}_{e}(\boldsymbol{r})+\hat{V}_{e n}(\boldsymbol{r}, \boldsymbol{R})+\hat{V}_{n n}(\boldsymbol{R})+\hat{V}_{e e}(\boldsymbol{r}) \tag{3.3}
\end{equation*}
$$

where $\hat{T}_{n}$ is the operator of nuclear kinetic energy, $\hat{T}_{e}$ is the operator of electronic kinetic energy, $\hat{V}_{e n}$ is the operator of electron-nucleus interaction, $\hat{V}_{n n}$ is the operator of nucleus-nucleus interaction and $\hat{V}_{e e}$ is the operator of electron-electron interaction.

When examining the non-relativistic Hamiltonian, it can be seen that the explicit separation of nuclear and electronic coordinates is prevented by the electron-nucleus interaction $\hat{V}_{e n}(\boldsymbol{r}, \boldsymbol{R})$ that depends on both nuclear and electronic coordinates. In 1927, Born and Oppenheimer introduced a fundamental ansatz for the decomposition of the total wave function [43]. They postulated that decoupling of fast electronic and slow nuclear motions is approximately correct and the total wave function can be separated into electronic and nuclear parts as

$$
\begin{equation*}
\Psi(\boldsymbol{r}, \boldsymbol{R}) \approx \Phi(\boldsymbol{r} ; \boldsymbol{R}) \chi(\boldsymbol{R}), \tag{3.4}
\end{equation*}
$$

where $\Phi$ denotes the electronic wave function and $\chi$ is the nuclear wave function. As a consequence, solving the molecular Schrödinger equation becomes a two step problem. First, the electronic Schrödinger equation

$$
\begin{equation*}
\hat{H}_{e} \Phi_{k}(\boldsymbol{r} ; \boldsymbol{R})=E_{k}(\boldsymbol{R}) \Phi_{k}(\boldsymbol{r} ; \boldsymbol{R}) \tag{3.5}
\end{equation*}
$$

must be solved. Here, $\hat{H}_{e}$ denotes the electronic Hamiltonian given by

$$
\begin{equation*}
\hat{H}_{e}=\hat{T}_{e}+\hat{V}_{e n}+\hat{V}_{n n}+\hat{V}_{e e} . \tag{3.6}
\end{equation*}
$$

As the electronic wave function $\Phi_{k}(\boldsymbol{r} ; \boldsymbol{R})$ only parametrically depends on $\{\boldsymbol{R}\}$, it can be calculated at fixed positions of nuclei. Computing $E_{k}(\boldsymbol{R})$ for a range of nuclear coordinates leads to the potential energy surface (PES) of the $k$ th electronic state.

In the next step, the nuclear Schrödinger equation

$$
\begin{equation*}
\hat{H}_{n} \chi_{j}(\boldsymbol{R})=E_{k}^{t o t} \chi_{k}(\boldsymbol{R}), \tag{3.7}
\end{equation*}
$$

where the nuclear Hamiltonian $\hat{H}_{n}$

$$
\begin{equation*}
\hat{H}_{n}=\hat{T}_{n}+E_{k}(\boldsymbol{R}) \tag{3.8}
\end{equation*}
$$

must be solved for a selected $k$ th electronic state. Such approach indicates that the nuclei move in the field produced by the electrons and nuclei themselves.

In order to show the adequacy of the Born-Oppenheimer approximation, this work follows the derivation shown in [44]. When introducing the postulated product of electronic and nuclear wave functions to the time-independent Schrödinger equation one obtains

$$
\begin{align*}
\hat{H} \Phi \chi & =\left[\hat{T}_{n}+\hat{T}_{e}+\hat{V}_{e n}+\hat{V}_{n n}+\hat{V}_{e e}\right] \Phi \chi=  \tag{3.9}\\
& =\sum_{A=1}^{N_{n}}-\frac{1}{2 M_{A}} \nabla_{A}^{2}[\Phi \chi]+\left[\hat{T}_{e}+\hat{V}_{e n}+\hat{V}_{n n}+\hat{V}_{e e}\right] \Phi \chi . \tag{3.10}
\end{align*}
$$

The laplacian $\nabla_{A}^{2}$ acting on product $\Phi \chi$ gives

$$
\begin{equation*}
\nabla_{A}^{2}[\Phi \chi]=\chi \nabla_{A}^{2} \Phi+2\left(\nabla_{A} \Phi \nabla_{A} \chi\right)+\Phi \nabla_{A}^{2} \chi . \tag{3.11}
\end{equation*}
$$

Hence, eq. 3.10 can be written as

$$
\begin{align*}
\hat{H} \Phi \chi & =\sum_{A=1}^{N_{n}}-\frac{1}{2 M_{A}}\left[\chi \nabla_{A}^{2} \Phi+2\left(\nabla_{A} \Phi \nabla_{A} \chi\right)+\Phi \nabla_{A}^{2} \chi\right]+  \tag{3.12}\\
& +\left[\hat{T}_{e}+\hat{V}_{e n}+\hat{V}_{n n}+\hat{V}_{e e}\right] \Phi \chi .
\end{align*}
$$

If one denotes the sum of terms with derivatives of the electronic wave function $\left(\nabla_{A} \Phi\right)$ as $B$

$$
\begin{equation*}
B=\sum_{A=1}^{N_{n}}-\frac{1}{2 M_{A}}\left[\chi \nabla_{A}^{2} \Phi+2\left(\nabla_{A} \Phi \nabla_{A} \chi\right)\right] \tag{3.13}
\end{equation*}
$$

and takes $\Phi$ out of the remaining sum term, then eq. 3.12 becomes

$$
\begin{equation*}
\hat{H} \Phi \chi=B+\Phi \underbrace{\sum_{A=1}^{N_{n}}-\frac{1}{2 M_{A}} \nabla_{A}^{2} \chi}_{\hat{T}_{N} \chi}+\left[\hat{T}_{e}+\hat{V}_{e n}+\hat{V}_{n n}+\hat{V}_{e e}\right] \Phi \chi \tag{3.14}
\end{equation*}
$$

Introducing $\hat{T}_{N} \chi$ into eq. 3.14 results in

$$
\begin{equation*}
\hat{H} \Phi \chi=B+\Phi \hat{T}_{N} \chi+\underbrace{\left[\hat{T}_{e}+\hat{V}_{e n}+\hat{V}_{n n}+\hat{V}_{e e}\right] \Phi \chi}_{E \Phi} \tag{3.15}
\end{equation*}
$$

Next, substituting the highlighted term in eq. 3.15 with the right hand side of the electronic Schrödinger equation gives

$$
\begin{align*}
\hat{H} \Phi \chi & =B+\Phi \hat{T}_{N} \chi+E \Phi \chi=  \tag{3.16}\\
& =B+\Phi \underbrace{\left[\hat{T}_{N}+E\right] \chi}_{E^{\text {tot }} \chi} . \tag{3.17}
\end{align*}
$$

Lastly, introducing the right hand side of the nuclear Schrödinger equation leads to the final formula

$$
\begin{equation*}
\hat{H} \Phi \chi=B+E^{t o t} \Phi \chi . \tag{3.18}
\end{equation*}
$$

From eq. 3.18 it is clear that the representation of the total wave function as a product of electronic and nuclear functions is not exact, as this approach omits the terms included in the sum $B$. These neglected terms, named non-adiabatic coupling terms, contain derivatives of the electronic wave function with respect to the nuclear positions. Those values are considered relatively small for molecules close to the equilibrium, because they couple different electronic states according to the nuclear motion. If an average value of the non-adiabatic coupling for a selected $k$ th electronic state

$$
\begin{equation*}
\sum_{A=1}^{N_{n}}-\frac{1}{2 M_{A}}\left[\left\langle\Phi_{k}\right| \nabla_{A}^{2}\left|\Phi_{k}\right\rangle+2\left\langle\Phi_{k}\right| \nabla_{A}\left|\Phi_{k}\right\rangle \nabla_{A}\right] \tag{3.19}
\end{equation*}
$$

is added to the nuclear Hamiltonian, then the adiabatic approach is considered.
From a physical perspective, Born-Oppenheimer and adiabatic approximations result from nuclei being several thousand times heavier than the electrons (mass of a proton is $\sim 1836.15$ times larger than mass of an electron [44]). The Born-Oppenheimer approximation implies that the electrons adjust instantaneously to the changes in the nuclear positions. On the other hand, the adiabatic correction depends on the masses of the nuclei and hence, gives different values for different isotopes. This results in a shift of the energies (small when compared to significant isotopic effects on vibrational and rotational energy levels).

Finally, there exist situations when Born-Oppenheimer and adiabatic approximations do not hold. Those include regions of the PES when different electronic states approach each other and produce avoided crossings. It has been shown [43] that the Born-Oppenheimer approximation works until the separation between electronic states is at least two orders greater than the difference between rovibrational energy levels. Nevertheless, present work does consider non-adiabatic phenomena.

### 3.2 Density Functional Theory

In quantum mechanics, finding a physical observable $\hat{O}$ of a system in the $k$ th eigenstate corresponds to calculating its expectation value $O_{k}=\left\langle\Phi_{k}\right| \hat{O}\left|\Phi_{k}\right\rangle$, where the $k$ th wave function is known. The drawback of such approach is that the number of parameters required to accurately approximate the wave function increases exponentially with number of electrons in the studied system. Additionally, the amount of information that the wave function of such system contains often exceeds the complexity of investigated properties (such as single values of energy and dipole moments or functions of a few variables such as one-particle probability density). In this context, Density Functional Theory (DFT) reduces the intricate problem of solving the many body Schrödinger equation by replacing the wave function formalism with the ground state density. The basic framework of DFT significant to the present work is presented in following sections.

### 3.2.1 Hohenberg-Kohn theorems

In 1964, Hohenberg and Kohn published the first theoretical considerations giving rise to the nowadays very extensive field of DFT [45]. Therein, authors considered a system of $N$ interacting electrons moving under the influence of an external potential $v(\boldsymbol{r})$ and mutual Coulomb repulsion. In agreement with the Born-Oppenheimer approximation described earlier, positions of nuclei are fixed. Such system is described by the electronic Schrödinger equation (eq. 3.6). For the purpose of clear presentation of the method in this section, one rewrites the electronic Hamiltonian $\hat{H}_{e}$ as a sum of kinetic energy operator $\hat{T}$, potential operator $\hat{V}$ and electronelectron Coulomb interaction operator $\hat{W}$, as follows

$$
\begin{equation*}
\hat{H}_{e}=\hat{T}+\hat{V}+\hat{W}=\sum_{i=1}^{N}-\frac{1}{2} \nabla_{i}^{2}+\sum_{i=1}^{N} v\left(\boldsymbol{r}_{i}\right)+\sum_{i<j}^{N} \frac{1}{\left|\boldsymbol{r}_{i}-\boldsymbol{r}_{j}\right|}, \tag{3.20}
\end{equation*}
$$

where the Coulomb interaction of nuclei is included in the external potential $v\left(\boldsymbol{r}_{i}\right)$. The oneparticle probability density of such system in an electronic ground state is given by

$$
\begin{equation*}
n_{0}(\boldsymbol{r})=N \sum_{\sigma_{1} \ldots \sigma_{N}} \int d \boldsymbol{x}_{2} \ldots \int d \boldsymbol{x}_{N}\left|\Phi_{0}\left(\boldsymbol{r}, \sigma_{1}, \boldsymbol{x}_{2}, \ldots, \boldsymbol{x}_{N}\right)\right|^{2}, \tag{3.21}
\end{equation*}
$$

where variable $\boldsymbol{x}_{i}$ denotes space coordinates and spin state of the $i$ th electron $\left(\boldsymbol{x}_{i} \equiv\left(\boldsymbol{r}_{i}, \sigma_{i}\right)\right.$ ). It can be clearly seen that the ground state density $n_{0}(\boldsymbol{r})$ is a functional of the potential $v(\boldsymbol{r})$ because it is obtained from the wave function governed by the Schrödinger equation. Hohenberg and Kohn showed for the first time that the opposite is also true. The first Hohenberg-Kohn theorem for a nondegenerate system reads:

HK theorem 1 The external potential $v_{0}(\boldsymbol{r})$ of the many-body ground state system (and hence the total ground state energy $E_{0}$ ) is a unique functional of the ground state density $n_{0}(\boldsymbol{r})$.

The proof relies on showing that the opposite assumption leads to a contradictory result, i.e. it is impossible that two different potentials produce the same wave function and by analogy two different ground state wave functions cannot give the same density. As a conclusion, given the ground state density, reconstruction of the molecular Hamiltonian is straightforward and hence all properties of the system can be derived.

Moreover, in [45] Hohenberg and Kohn also presented a way of minimizing the total energy functional

$$
\begin{equation*}
E_{v_{0}}[n]=\langle\Phi[n]| \hat{T}+\hat{V}_{0}+\hat{W}|\Phi[n]\rangle \tag{3.22}
\end{equation*}
$$

when considering the ground state potential operator $\hat{V}_{0}$ following the Rayleigh-Ritz principle. The second Hohenberg-Kohn theorem reads:

HK theorem 2 The ground state energy $E_{v_{0}}[n]$ can be found with the use of ground state density $n_{0}(\boldsymbol{r})$ according to the variational principle:

$$
\begin{align*}
& E_{v_{0}}[n]>E_{0} \text { for } n(\boldsymbol{r}) \neq n_{0}(\boldsymbol{r})  \tag{3.23}\\
& E_{v_{0}}[n]=E_{0} \text { for } n(\boldsymbol{r})=n_{0}(\boldsymbol{r})
\end{align*}
$$

In other words, the density that minimizes the total energy is the exact ground state density. Since the total number of electrons in the system is fixed and can be calculated from

$$
\begin{equation*}
N=\int n(\boldsymbol{r}) d^{3} r, \tag{3.24}
\end{equation*}
$$

such constrained minimization of the energy is possible using the Lagrange multipliers ( $\lambda$ ) method. Given the Lagrangian

$$
\begin{equation*}
\mathcal{L}[n]=E_{v_{0}}[n]-\lambda\left[\int n(\boldsymbol{r}) d^{3} r-N\right], \tag{3.25}
\end{equation*}
$$

according to the principle of stationary action, solving the resulting Euler equation

$$
\begin{equation*}
\frac{\delta \mathcal{L}[n]}{\delta n(\boldsymbol{r})}=\frac{\delta E_{v_{0}}[n]}{\delta n(\boldsymbol{r})}-\lambda=0 \tag{3.26}
\end{equation*}
$$

should give the exact ground state density $n_{0}(\boldsymbol{r})$ without solving the Schrödinger equation. Rewriting equation 3.22 as

$$
\begin{align*}
E_{v_{0}}[n] & =\langle\Phi[n]| \hat{T}+\hat{W}|\Phi[n]\rangle+\int d^{3} r n(\boldsymbol{r}) v_{0}(\boldsymbol{r})=  \tag{3.27}\\
& =F[n]+\int d^{3} r n(\boldsymbol{r}) v_{0}(\boldsymbol{r}) \tag{3.28}
\end{align*}
$$

introduces the universal functional $F[n]$ for the system of $N$ electrons that is irrespective of the external potential. This leads to a new form of eq. 3.26, as follows

$$
\begin{equation*}
\frac{\delta F[n]}{\delta n(\boldsymbol{r})}+v_{0}(\boldsymbol{r})=\lambda \tag{3.29}
\end{equation*}
$$

The biggest advantage of DFT arises from reduction of the dimensionality of the electronic many-body problem. As the wave function formalism refers to $3 N$ variables, electronic density is a function of only three spatial variables. Still, a difficulty remains in finding the appropriate expression for the unknown functional $F[n]$. The following section presents a practical method of finding the ground state density.

### 3.2.2 Kohn-Sham equations

A practical scheme for carrying out DFT calculations analogous to the Hartree-Fock procedure, but containing the effects of exchange and correlation was published in 1965 by Kohn and Sham [46]. It is known that for the systems of $N$ non-interacting particles, the ground state wave function $\Phi_{s}$ takes the form of a single Slater determinant

$$
\Phi_{s}\left(\boldsymbol{x}_{1}, \ldots, \boldsymbol{x}_{N}\right)=\frac{1}{\sqrt{N!}}\left|\begin{array}{cccc}
\phi_{1}\left(\boldsymbol{r}_{1}\right) & \phi_{2}\left(\boldsymbol{r}_{1}\right) & \ldots & \phi_{N}\left(\boldsymbol{r}_{1}\right)  \tag{3.30}\\
\phi_{1}\left(\boldsymbol{r}_{2}\right) & \phi_{2}\left(\boldsymbol{r}_{2}\right) & \ldots & \phi_{N}\left(\boldsymbol{r}_{2}\right) \\
\vdots & \vdots & & \vdots \\
\phi_{1}\left(\boldsymbol{r}_{N}\right) & \phi_{2}\left(\boldsymbol{r}_{N}\right) & \ldots & \phi_{N}\left(\boldsymbol{r}_{N}\right)
\end{array}\right|,
$$

where each one-particle orbital $\phi_{i}(\boldsymbol{r})$ satisfies the Schrödinger equation

$$
\begin{equation*}
\left(-\frac{\nabla^{2}}{2}+v_{s}(\boldsymbol{r})\right) \phi_{i}(\boldsymbol{r})=\varepsilon_{i} \phi_{i}(\boldsymbol{r}) . \tag{3.31}
\end{equation*}
$$

The Hamiltonian in eq. 3.31 consists of the kinetic energy term and the effective potential of a non-interacting system $v_{s}(\boldsymbol{r})$. Acting on the $i$ th orbital $\phi_{i}$ it produces the orbital energy $\varepsilon_{i}$. At the same time, the Euler equation of the non-interacting system is given by

$$
\begin{equation*}
\frac{\delta T_{s}[n]}{\delta n(\boldsymbol{r})}+v_{s}(\boldsymbol{r})=\lambda, \tag{3.32}
\end{equation*}
$$

where $T_{s}$ is the kinetic energy functional in the absence of electron-electron interactions. Kohn and Sham applied the effective one-particle orbital technique, which transformed DFT into a problem feasible to solve. Their approach started with rewriting eq. 3.28 as

$$
\begin{equation*}
E[n]=T_{s}[n]+\int d^{3} r n(\boldsymbol{r}) v(\boldsymbol{r})+\frac{1}{2} \int d^{3} r \int d^{3} r^{\prime} \frac{n(\boldsymbol{r}) n\left(\boldsymbol{r}^{\prime}\right)}{\left|\boldsymbol{r}-\boldsymbol{r}^{\prime}\right|}+E_{x c}[n], \tag{3.33}
\end{equation*}
$$

where $E_{x c}$ is an exchange-correlation ( $x c$ ) energy functional given by

$$
\begin{equation*}
E_{x c}[n]=T[n]-T_{s}[n]+W[n]-\frac{1}{2} \int d^{3} r \int d^{3} r^{\prime} \frac{n(\boldsymbol{r}) n\left(\boldsymbol{r}^{\prime}\right)}{\left|\boldsymbol{r}-\boldsymbol{r}^{\prime}\right|} . \tag{3.34}
\end{equation*}
$$

All terms of eq. 3.33 can be derived explicitly besides the $x c$ energy functional. The corresponding Euler equation with the new form of the total energy functional now becomes

$$
\begin{equation*}
\frac{\delta T_{s}[n]}{\delta n(\boldsymbol{r})}+v(\boldsymbol{r})+\int d^{3} r^{\prime} \frac{n\left(\boldsymbol{r}^{\prime}\right)}{\left|\boldsymbol{r}-\boldsymbol{r}^{\prime}\right|}+\frac{\delta E_{x c}}{\delta n(\boldsymbol{r})}=\lambda . \tag{3.35}
\end{equation*}
$$

Comparing eq. 3.32 and 3.35 leads to conclusion that the mathematical problems are iden-

$$
\begin{equation*}
v_{s}[n](\boldsymbol{r})=v(\boldsymbol{r})+\int d^{3} r^{\prime} \frac{n\left(\boldsymbol{r}^{\prime}\right)}{\left|\boldsymbol{r}-\boldsymbol{r}^{\prime}\right|}+v_{x c}[n](\boldsymbol{r}), \tag{3.36}
\end{equation*}
$$

where $v_{x c}$ denotes the $x c$ potential

$$
\begin{equation*}
v_{x c}(\boldsymbol{r})=\frac{\delta E_{x c}}{\delta n(\boldsymbol{r})} . \tag{3.37}
\end{equation*}
$$

Plugging the new effective potential $v_{s}[n]$ to the Schrödinger equation for the system of non-interacting particles (eq. 3.31) enables finding the ground state density of the interacting system, as follows

$$
\begin{equation*}
\left(-\frac{\nabla^{2}}{2}+v_{s}[n](\boldsymbol{r})\right) \phi_{i}(\boldsymbol{r})=\varepsilon_{i} \phi_{i}(\boldsymbol{r}) . \tag{3.38}
\end{equation*}
$$

Then, the ground state density $n_{0}$ becomes a sum over $N$ non-interacting lowest occupied orbitals

$$
\begin{equation*}
n_{0}(\boldsymbol{r})=\sum_{i=1}^{N}\left|\phi_{i}(\boldsymbol{r})\right|^{2} . \tag{3.39}
\end{equation*}
$$

Equations 3.36-3.39 are labeled as Kohn-Sham (KS) equations. Similarly to the HartreeFock theory, KS equations are solved iteratively until self-consistency is obtained. This technique presents a big advantage over wave function based electron correlation methods, because the KS approach to DFT calculations results in lower computational cost (compared to that of the HF calculations). However, solving the many-body problem is still hindered by the missing expression for the $x c$ energy functional.

### 3.2.3 Approximate functionals

Basing on the former description, DFT can be seen as a formally exact theory if the exact exchange-correlation functional is known. Unfortunately, this is true only for the case of a uniform electron gas, so for the molecular systems approximations must be applied. Although as seen in [47], the $x c$ energy contributes to a minor extend to the total energy, it is relevant when establishing the binding energy of matter. After 50 years of research performed on DFT, abundance of approximate energy functionals can be found in the literature.

## Local Density Approximation

The first approximation, named Local Density Approximation (LDA), was introduced by Kohn and Sham already in 1965 [48]. It relies on the assumption that the $x c$ energy density ( $x c$ energy per unit of volume) of an infinitesimal volume element can be approximated by the $x c$ energy density of a system with uniform density $\bar{n}$. At a position $r$ the value of density $\bar{n}$ is evaluated as the value of the local density $n(\boldsymbol{r})$. Then, for the inhomogeneous system, the $x c$ energy $E_{x c}^{L D A}$ takes the form of an integral over $x c$ energy density in a homogeneous electron gas $e_{x c}^{h}$ that is determined at the local density, as follows

$$
\begin{equation*}
E_{x c}^{L D A}[n]=\left.\int d^{3} r e_{x c}^{h}(\bar{n})\right|_{\bar{n}=n(\boldsymbol{r})} \tag{3.40}
\end{equation*}
$$

Corresponding exchange correlation potential is given by

$$
\begin{equation*}
v_{x c}^{L D A}(\boldsymbol{r})=\left.\frac{d e_{x c}^{h}(\bar{n})}{d \bar{n}}\right|_{\bar{n}=n(\boldsymbol{r})} \tag{3.41}
\end{equation*}
$$

The $x c$ energy density $e_{x c}^{h}(n)$ consists of two terms: one corresponding to the exchange $\left(e_{X}^{h}(n)\right)$ and one to correlation $\left(e_{C}^{h}(n)\right)$. The exchange part can be determined analytically from theory of the homogeneous electron gas, however, there is no exactly known expression for the correlation part. The approximated values come from accurate numerical calculations, such as quantum Monte Carlo simulations [49]. On the basis of such results, high-precision representations of the electron gas correlation energy have been developed [50], [51].

Evidently, LDA succeeds for nonuniform systems with slowly varying density. Hence, for the LDA to hold, the local density variations should satisfy the condition

$$
\begin{equation*}
\frac{|\nabla n(\boldsymbol{r})|}{n(\boldsymbol{r})} \ll k_{F}(n) \tag{3.42}
\end{equation*}
$$

where $k_{F}(n)$ indicates Fermi wave vector. In practice, there are many energetic and structural properties that the LDA approximation is able to reproduce within few percent of the experimental values. Those include total ground state energies (1-5\%), equilibrium distances ( $\sim 3 \%$ ) and vibrational frequencies (few percent) [47]. The main drawback of the LDA approach results from incorrect asymptotic behaviour ( $v_{x c}^{L D A}$ approaches zero too fast). As a result, KS eigenvalues calculated with the LDA approach are too low in magnitude and the highest occupied molecular orbital energies differ significantly from the ionization energies. However, the LDA approximation works well for computing the total energies because underestimation of the correlation is compensated by the overestimation of the exchange effects.

## Gradient Expansion Approximation

Improvement of the LDA approximation is possible through consideration of dependence of the energy density on the gradient of the local density. If condition 3.42 holds, reduced density gradients can be introduced to the energy density as small expansion series. Reduced density gradient takes the form of [47]

$$
\begin{equation*}
s(\boldsymbol{r})=\frac{\nabla n(\boldsymbol{r})}{2 n(\boldsymbol{r}) k_{F}(\boldsymbol{r})} . \tag{3.43}
\end{equation*}
$$

A general formula for the $x c$ energy functional according to Gradient Expansion Approximation (GEA) is given by

$$
\begin{equation*}
E_{x c}^{G E A}[n]=\int d^{3} r\left(e_{x c}^{h}(n(\boldsymbol{r}))+C_{x c}^{2}(n) s^{2}+\ldots\right), \tag{3.44}
\end{equation*}
$$

where $C_{x c}^{2}(n)$ is the second order term of the gradient expansion series. In the last years much effort has been invested in deriving mathematical expressions for higher order terms that reproduce as many of the exact properties as possible. The most widely used Generalized Gradient Approximation (GGA) functionals are the exchange functional of Becke $E_{X}^{B 88}$ [52], the correlation energy functional introduced by Lee, Yang and Parr $E_{c}^{L Y P}$ [53] and PBE functional of Perdew $E^{P E B}$ [54]. Generally, total ground state energies and spectroscopic constants show improvement when calculated with the GGA functionals.

## Hybrid functionals

With the advancements in construction of the GGAs, another idea allowed for surpassing the accuracy of the Gradient Expansion Approximation. The next level of refinement is possible via introduction of portion of exact exchange energy from the Hartree-Fock theory:

$$
\begin{equation*}
E_{X}^{e x a c t}(\boldsymbol{r})=-\sum_{i<j}^{N} \int d^{3} r \int d^{3} r^{\prime} \frac{\phi_{i}^{\star}\left(\boldsymbol{r}^{\prime}\right) \phi_{j}\left(\boldsymbol{r}^{\prime}\right) \phi_{i}(\boldsymbol{r}) \phi_{j}^{\star}(\boldsymbol{r})}{\left|\boldsymbol{r}-\boldsymbol{r}^{\prime}\right|} \tag{3.45}
\end{equation*}
$$

and mixing it with fractions of standard LDA and GGA functionals. Hybrid functionals are generally constructed according to the following formula

$$
\begin{equation*}
E_{x c}^{\text {hybrid }}=a E_{X}^{\text {exact }}+(1-a) E_{X}^{G G A}+E_{C}^{G G A} . \tag{3.46}
\end{equation*}
$$

Nowadays, the most widely used hybrid functional named B3LYP consists of

$$
\begin{equation*}
E_{x c}^{B 3 L Y P}=(1-a) E_{X}^{L D A}+a E_{X}^{e x a c t}+b E_{X}^{B 88}+c E_{C}^{L Y P}+(1-c) E_{C}^{L D A}, \tag{3.47}
\end{equation*}
$$

where $a=0.20, b=0.72$ and $c=0.81$. Other hybrid functionals include PBE0 [55] and B98 [56].
Performance of the B3LYP functional has been extensively studied and according to [47] it has been applied to around $80 \%$ of all studies using DFT. Some benchmark data can be found in [57]-[59]. In [59] it has been shown that the B3LYP functional is an accurate choice for the investigations of oxygen containing organic systems, such as furan, the object of the present work. Particularly, those studies commented on calculating heats of formation and isomerization energies. In combination with basis sets that include dispersion corrections, the B3LYP functional gives mean absolute error values of around $1.9 \mathrm{kcal} / \mathrm{mol}(0.08 \mathrm{eV})$ for determination of the isomerization energies.

With the abundance of available options in the literature, the selection of the correct density functional may seem like a challenge. However, large sets of benchmark calculations provide systematic insight into errors in calculation of several physical properties. Provided their careful examination, making the right choice for the system in question in numerous instances can be easily resolved.

### 3.3 Molecular Potential Energy Surface

Previous sections introduced the concept of a Potential Energy Surface and the method of calculating values of the energy. The potential energy of a non-linear molecular system comprising of $N$ atoms is a multidimensional function of $3 N-6$ internal coordinates. Consequently, visualization of the entire PES is impossible except for systems with one or two internal coordinates. However, in a polyatomic system, it is possible to select certain parts of the PES, such as relationship between the energy and distance between two atoms (1D Potential Energy Curve, Figure 3.1 a)) or energy dependence of simultaneous changes of two internal coordinates (2D Potential Energy Surface, Figure 3.1 b)).

Points on the PES that are especially interesting for understanding the behaviour of molecular systems are stationary points, i.e. minima and saddle points. In a minimum energy configuration the system remains in a stable state, as any change in the geometry results in higher energy. One PES may posses numerous minima with the lowest minimum named global minimum. The relative populations of various equilibrium structures, i.e. thermodynamical properties, can be determined on the basis of the shape of the PES. For example, a broad minimum (point $\mathbf{A}$ in the Figure $3.1 \mathbf{a}$ )) is expected to be more highly populated than a deeper, but more narrow minimum (point $\mathbf{C}$ in the Figure 3.1 a)) due to vibrational energy levels being more spread out and consequently less accessible [60]. Transition from one minimum to another



FIGURE 3.1 Panel a): schematic energy curve. Panel b): surface of a function $f(x, y)=x^{4}+4 x^{2} y^{2}-2 x^{2}+2 y^{2}$ with one saddle point at $(0,0)$ and two minima at $(1,0)$ and $(0,1)$. Adapted from [60].
occurs through a saddle point (point $\mathbf{B}$ in the Figure 3.1 a)), corresponding to a transition structure, which is the highest point on a reaction pathway (a path between two minima). Two adjacent minima can be taken as reactants and products of a specific reaction. Those structures may correspond to many configurations involved in different processes, such as two conformers of a single molecule or two molecules involved in a bimolecular reaction. Then, a transition structure provides information about the changes in geometry and variations in energy during a reaction. Kinetic studies of transition structures provide information about conversion rates from reactants to products. Moreover, during the fragmentation reactions, reverse activation barriers $(\mathrm{E}(\mathbf{B})-\mathrm{E}(\mathbf{C})$ in Figure 3.1 a)) indicate the energy that is converted to relative kinetic energy of produced fragments.

As the first derivatives of the energy function at a stationary point are zero, it is necessary to calculate the second derivatives in order to distinguish between a minimum and a saddle point. Then, a structure with all positive second derivatives is a minimum and a configuration with only one negative eigenvalue in the matrix of second derivatives is a saddle point. Energy minimisation problems of quantum mechanics predominantly use numerical methods that approximate the true minima and saddle points. The default optimization method of the Gaussian software package [61] employed in this work is the Berny algorithm using GEDIIS [62]. The GEDIIS abbreviation stands for Geometry Optimization Using Energy-Represented Direct Inversion in the Iterative Subspace. This algorithm relies on a least-squares minimization scheme and due to enforced interpolation results in enhanced stability and generally smooth convergence behaviour [62].

After determination of a transition structure, it is necessary to make sure that the studied configuration indeed follows a particular reaction pathway. A way to do so relies on the steepest descent minimisation algorithm that produces the Intrinsic Reaction Coordinate (IRC) - the approximation to the minimum energy path that connects a transition structure with the equilibrium geometry. The first steps of reaching each minimum are derived from the eigenvector associated with the imaginary frequency of the transition structure.

### 3.4 Ab initio Molecular Dynamics

Next approach to studying the fragmentation process is a dynamical treatment using ab initio Molecular Dynamics (MD). This methodology unifies first-principle electronic structure theory with the framework of classical dynamics. Contrary to the fully classical MD, where the interatomic potentials are parametrized, predefined functions of the coordinates, ab initio MD methods rely on computing the forces acting on the nuclei "on the fly" from the electronic structure calculations. By that means, the electronic variables are active degrees of freedom as the MD trajectory evolves. Such methodology proves essential in systems where electronic rearrangement causes changes in the nature of bonding and induces chemical reactions, as in the processes under study in this work.

Similarly to the classical MD, ab initio MD employs generalized Lagrangian formulation with a Lagrangian $\mathcal{L}$ defined as the total kinetic energy minus potential energy of the system. Given the Lagrangian of the studied system, corresponding equations of motion are obtained from Euler-Lagrange equations:

$$
\begin{align*}
& \frac{d}{d t} \frac{\partial \mathcal{L}}{\partial \dot{\boldsymbol{R}}_{I}}=\frac{\partial \mathcal{L}}{\partial \boldsymbol{R}_{I}},  \tag{3.48}\\
& \frac{d}{d t} \frac{\delta \mathcal{L}}{\delta\left\langle\dot{\phi}_{i}\right|}=\frac{\delta \mathcal{L}}{\delta\left\langle\phi_{i}\right|}, \tag{3.49}
\end{align*}
$$

for the nuclear coordinates $\boldsymbol{R}_{I}$ (3.48) and the orbitals $\phi_{i}$ (3.49). Here, and in the following discussion, the dot over a variable symbol indicates time derivative. Typically, resulting equations of motion are integrated numerically using gradient-based methods such as velocity Verlet [63] or fourth order Runge-Kutta [64] algorithms. In essence, the type of methods described below relies on solving the time-independent, stationary Schrödinger equation for electrons together with solving the motion of nuclei according to classical mechanics. Methods described in this section only refer to the ground state dynamics and employ DFT as a method of calculating electronic structure.

### 3.4.1 Born-Oppenheimer Molecular Dynamics

The Born-Oppenheimer approximation of decoupling nuclear and electronic degrees of freedom is also applied to the time dependent problem. According to the Born-Oppenheimer Molecular Dynamics (BOMD), the electronic structure calculations are converged at every time step under the constraint that orbitals are orthonormal, i.e. $\left\langle\phi_{i} \mid \phi_{j}\right\rangle=\delta_{i j}$. Consequently, the Lagrangian is equal to

$$
\begin{equation*}
\mathcal{L}_{B O}=\underbrace{\sum_{I} \frac{1}{2} M_{I} \dot{\boldsymbol{R}}_{I}^{2}}_{\text {kinetic energy }}-\underbrace{\min _{\left.\phi_{i}\right\}}\left\{\left\langle\Phi_{0}\right| H_{e}^{K S}\left|\Phi_{0}\right\rangle\right\}}_{\text {potential energy }}+\underbrace{\sum_{i, j} \Lambda_{i j}\left(\left\langle\phi_{i} \mid \phi_{j}\right\rangle-\delta_{i j}\right)}_{\text {constraint for orthonormality }}, \tag{3.50}
\end{equation*}
$$

where $\Lambda_{i j}$ builds a matrix of Lagrangian multipliers required for the constrained solution. Introducing this Lagrangian to the Euler-Lagrange equations results in the following equations
of motion

$$
\begin{gather*}
M_{I} \ddot{\boldsymbol{R}}_{I}(t)=-\nabla_{I} \min _{\left\{\phi_{i}\right\}}\left\{\left\langle\Phi_{0}\right| \hat{H}_{e}^{K S}\left|\Phi_{0}\right\rangle\right\},  \tag{3.51}\\
0=-H_{e}^{K S} \phi_{i}+\sum_{j} \Lambda_{i j} \phi_{j}, \tag{3.52}
\end{gather*}
$$

for the system in the electronic ground state. Nevertheless, the BOMD scheme is easily applicable to a particular electronic excited state $\Phi_{k}, k>0$. Previously mentioned gradientbased methods are employed to propagate the nuclear degrees of freedom by calculating gradients of the energy, i.e. forces acting on the nuclei. For each nuclear configuration electronic Schrödinger equation is solved. Above equations already imply the Kohn-Sham density functional theory described before by the application of the KS one-particle Hamiltonian $H_{e}^{K S}$ (eq. 3.38).

Such approach to molecular dynamics presents one very significant advantage. Due to the adiabatic separation and minimization of the potential energy at every time step, there exists no constraint on the maximum values of the integration time step coming from the electronic motion. An adequate time step is determined by the nuclear degrees of freedom only. On the other hand, due to the need of converging the wave function at every instance of time, BOMD calculations are computationally expensive (even easily converged system require around 8-12 self-consistent field steps [65]).

### 3.4.2 Extended Lagrangian methods

The high computational cost of self-consistent optimization at every time step of the BOMD limits the feasible size of the studied system and accessible simulation time. As the adopted time step causes small changes in the wave functions, the orbitals might as well be treated by the appropriate equations of motion. In this sense, a more computationally efficient approach to the molecular dynamics calculations was firstly developed by Car and Parinello and published in 1985 [66]. They proposed extending the Lagrangian with kinetic energy of fictitious particles that serve a purpose of the dynamical simulated annealing:

$$
\begin{equation*}
\mathcal{L}_{C P}=\underbrace{\sum_{I} \frac{1}{2} M_{I} \dot{\boldsymbol{R}}_{I}^{2}+\sum_{i} \mu\left\langle\dot{\phi}_{i} \mid \dot{\phi}_{i}\right\rangle}_{\text {kinetic energy }}-\underbrace{\left\langle\Phi_{0}\right| H_{e}^{K S}\left|\Phi_{0}\right\rangle}_{\text {potential energy }}+\underbrace{\sum_{i, j} \Lambda_{i j}\left(\left\langle\phi_{i} \mid \phi_{j}\right\rangle-\delta_{i j}\right)}_{\text {constraint for orthonormality }} \tag{3.53}
\end{equation*}
$$

where again orthonormality of orbitals is imposed by the Lagrange multipliers $\Lambda_{i j}$. The new dynamical variable $\mu$ introduces the fictitious dynamics of the wave function. As a result, both the electronic and nuclear degrees of freedom are propagated at the same time. The resulting CPMD equations of motion are

$$
\begin{align*}
& M_{I} \ddot{\boldsymbol{R}}_{I}(t)=-\nabla_{I}\left\langle\Phi_{0}\right| H_{e}^{K S}\left|\Phi_{0}\right\rangle, \\
& \mu \ddot{\phi}_{i}(t)=-H_{e}^{K S} \phi_{i}+\sum_{j} \Lambda_{i j} \phi_{j} . \tag{3.55}
\end{align*}
$$

Typically to Car-Parinello Molecular Dynamics (CPMD), a plane wave expansion is chosen to represent the orbitals. Such basis allows for an easy calculation of the integrals using fast Fourier transform methods, but shows disadvantages in reproducing the high electron density and cusps near the nuclei. Ultimately, propagation of the orbital coefficients leads to $\mathcal{O}\left(N^{3}\right)$ computational scaling with the system size.

The challenge of the CPMD approach remains in the correct definition of the inertia parameter $\mu$ of the electronic degrees of freedom, so that the electronic subsystem remains "cold", i.e. is close to the associated Born-Oppenheimer PES. Adiabatic separation has been extensively discussed in [67]. Therein, it has been shown that the highest phonon frequency $\omega_{n}^{\max }$ has to be much smaller than the lowest electronic frequency $\omega_{e}^{\min }$ for the correct CPMD simulation. The highest phonon frequency depends entirely on the physics of the system and the lowest electronic frequency $\omega_{e}^{\min }$ is given by

$$
\begin{equation*}
\omega_{e}^{\min } \propto\left(\frac{E_{\text {gap }}}{\mu}\right)^{1 / 2}, \tag{3.56}
\end{equation*}
$$

where $E_{\text {gap }}$ denotes the energy difference between the highest occupied and lowest unoccupied molecular orbitals, which depends on the physical system as well. Hence, it can be seen that the only variable that allows one to control the adiabaticity is the fictitious mass $\mu$. As presented in [67], adequate values of $\mu$ for large-gap systems range from 500 to 1000 a.u., allowing for a time step between 0.1 and 0.25 fs. To summarize, provided that fictitious mass $\mu$ is small enough, CPMD simulations guarantee negligible errors in conservation of the total energy.

In 2001, a modification to the CPMD theory has been introduced by Schlegel et al [68][70]. In the new approach named, Atom-centered Density Matrix Propagation (ADMP), the authors proposed propagating the one-particle density matrix instead of orbital coefficients and using atom-centered Gaussian basis functions rather than plane waves. Generally, to achieve desired accuracy in reproducing the orbitals, a large plane wave basis set is needed. Using Gaussian basis functions presents two significant benefits: it ensures better reproduction of the high electron density regions and, as Gaussians are atom-centered, they adopt to the nuclear motion. Due to transition to the density matrix propagation formalism the following discussion employs the matrix forms for the representation of the phase space $\{\{\boldsymbol{R}, \boldsymbol{M}, \boldsymbol{V}\},\{\boldsymbol{P}, \mu, \boldsymbol{W}\}\}$.

Then, the Lagrangian of the ADMP approach is given by

$$
\begin{equation*}
\mathcal{L}_{A D M P}=\frac{1}{2} \operatorname{Tr}\left[\boldsymbol{V}^{T} \boldsymbol{M} \boldsymbol{V}\right]+\frac{1}{2} \mu \operatorname{Tr}[\boldsymbol{W} \boldsymbol{W}]-E(\boldsymbol{R}, \boldsymbol{P})-\operatorname{Tr}[\boldsymbol{\Lambda}(\boldsymbol{P} \boldsymbol{P}-\boldsymbol{P})] \tag{3.57}
\end{equation*}
$$

where $\boldsymbol{R}, \boldsymbol{M}$ and $\boldsymbol{V}$ are the nuclear positions, masses and velocities, respectively. The electronic degrees of freedom are described by the one-particle density matrix $\boldsymbol{P}$ (defined as $\left.\sum_{i=1}^{N_{e}}\left|\phi_{i}\right\rangle\left\langle\phi_{i}\right|\right)$, density matrix velocity $\boldsymbol{W}$ and fictitious mass $\mu$. Here, Lagrangian multiplier matrix introduces a constraint on the idempotency of the density matrix (resulting from description of a pure state) and on the total number of electrons. Applying Lagrangian $\mathcal{L}_{A D M P}$ to the EulerLagrange equations leads to the following ADMP equations of motion

$$
\begin{equation*}
\boldsymbol{M} \frac{d^{2} \boldsymbol{R}}{d t^{2}}=-\left.\frac{\partial E(\boldsymbol{R}, \boldsymbol{P})}{\partial \boldsymbol{R}}\right|_{\boldsymbol{P}} \tag{3.58}
\end{equation*}
$$

$$
\begin{equation*}
\mu \frac{d^{2} \boldsymbol{P}}{d t^{2}}=-\left[\left.\frac{\partial E(\boldsymbol{R}, \boldsymbol{P})}{\partial \boldsymbol{P}}\right|_{\boldsymbol{R}}+\boldsymbol{\Lambda} \boldsymbol{P}+\boldsymbol{P} \boldsymbol{\Lambda}-\boldsymbol{\Lambda}\right], \tag{3.59}
\end{equation*}
$$

for the nuclear and electronic degrees of freedom, respectively. Solution of eq. 3.59 gives dynamics of the one-particle density matrix in the orthonormal basis. In practice, the forces acting on the nuclei and density matrices are derived using the McWeeny density matrix purification transformation [71] in the expression for the energy.

As in the case of CPMD simulations, the fictitious mass $\mu$ should act as a parameter of the adiabatic control. Analysis of its influence on the adiabaticity has been investigated in [72]. This study relied on assessment of the commutator of Fock and density matrices, which in the BOMD approach is equal to zero. The authors concluded that, indeed, as the fictitious mass is proportional to the mentioned commutator, its magnitude determines the lower limit for deviations from the Born-Oppenheimer PES.

In summary, alterations introduced by the ADMP method decrease significantly the computational cost of the dynamical calculations by ensuring linear scaling of computational time with the increasing system size.

### 3.4.3 Time integration algorithm

After establishing the equations of motion the next step of solving a dynamical problem is to decide on the method of their numerical integration. Present work employs the ADMP technique, so the integration algorithm implemented for this method will be presented in the following section, namely the velocity Verlet algorithm [63]. This method relies on expanding position $r$ of a particle of mass $m$ around time $t$ in a Taylor series as

$$
\begin{equation*}
r(t+\Delta t)=r(t)+V(t) \Delta t+\frac{f(t)}{2 m} \Delta t^{2}+\mathcal{O}\left(\Delta t^{4}\right) \tag{3.60}
\end{equation*}
$$

where $V$ and $f$ denote velocity and force, respectively. Expanding the velocity in the same manner and applying the expansion of the force gives the following formula for the velocity at time $t+\Delta t$

$$
\begin{equation*}
V(t+\Delta t)=V(t)+\frac{f(t)+f(t+\Delta t)}{2 m} \Delta t . \tag{3.61}
\end{equation*}
$$

This variant of the Verlet algorithm leads to convenient expressions for positions and velocities computed at equal times. In this form, obtaining new velocities requires preceding calculations of positions and forces at times $t$ and $t+\Delta t$. However, the most commonly used iterative procedure of the velocity Verlet algorithm avoids storing forces at two instances of time [73]. It comprises of following steps:

1. Given $V(t)$ and $f(t)$, computing velocity at half-time step as $V\left(t+\frac{1}{2} \Delta t\right)=V(t)+\frac{f(t)}{2 m} \Delta t$.
2. Computing position at time $t+\Delta t$ as $r(t+\Delta t)=r(t)+V\left(t+\frac{1}{2} \Delta t\right) \Delta t$.
3. Evaluating force at time $t+\Delta t$ from the interaction potential with the use of $r(t+\Delta t)$.
4. Computing velocity at time $t+\Delta t$ as $V(t+\Delta t)=V\left(t+\frac{1}{2} \Delta t\right)+\frac{f(t+\Delta t)}{2 m} \Delta t$.

The velocity Verlet algorithm is preferable for iterations of constrained dynamics, such as ADMP. Applying above approach to the ADMP equations of motion leads to the following formula for propagation of the density matrix

$$
\begin{equation*}
\boldsymbol{P}_{(t+\Delta t)}=\boldsymbol{P}_{(t)}+\boldsymbol{W}_{(t)} \Delta t-\frac{\Delta t^{2}}{2 \mu}\left[\left.\frac{\partial E\left(\boldsymbol{R}_{(t)}, \boldsymbol{P}_{(t)}\right)}{\partial \boldsymbol{P}_{(t)}}\right|_{\boldsymbol{R}_{(t)}}+\boldsymbol{\Lambda}_{(t)} \boldsymbol{P}_{(t)}+\boldsymbol{P}_{(t)} \boldsymbol{\Lambda}_{(t)}-\boldsymbol{\Lambda}_{(t)}\right] \tag{3.62}
\end{equation*}
$$

Density matrix velocities are calculated using

$$
\begin{align*}
\boldsymbol{W}_{\left(t+\frac{1}{2} \Delta t\right)} & =\boldsymbol{W}_{(t)}-\frac{\Delta t}{2 \mu}\left[\left.\frac{\partial E\left(\boldsymbol{R}_{(t)}, \boldsymbol{P}_{(t)}\right)}{\partial \boldsymbol{P}_{(t)}}\right|_{\boldsymbol{R}_{(t)}}+\boldsymbol{\Lambda}_{(t)} \boldsymbol{P}_{(t)}+\boldsymbol{P}_{(t)} \boldsymbol{\Lambda}_{(t)}-\boldsymbol{\Lambda}_{(t)}\right]  \tag{3.63}\\
& =\frac{\boldsymbol{P}_{(t+\Delta t)}-\boldsymbol{P}_{(t)}}{\Delta t} \tag{3.64}
\end{align*}
$$

and

$$
\begin{align*}
& \boldsymbol{W}_{(t+\Delta t)}=\boldsymbol{W}_{\left(t+\frac{1}{2} \Delta t\right)}-\frac{\Delta t}{2 \mu}\left[\left.\frac{\partial E\left(\boldsymbol{R}_{(t+\Delta t)}, \boldsymbol{P}_{(t+\Delta t)}\right)}{\partial \boldsymbol{P}_{(t+\Delta t)}}\right|_{\boldsymbol{R}_{(t+\Delta t)}}\right. \\
&\left.+\boldsymbol{\Lambda}_{(t+\Delta t)} \boldsymbol{P}_{(t+\Delta t)}+\boldsymbol{P}_{(t+\Delta t)} \boldsymbol{\Lambda}_{(t+\Delta t)}-\boldsymbol{\Lambda}_{(t+\Delta t)}\right] . \tag{3.65}
\end{align*}
$$

Aforementioned propagation of the density matrix requires computation of the Lagrange multipliers matrix at each time step. The ADMP method works under the idempotency constraint $\boldsymbol{P}^{2}=\boldsymbol{P}$ and the time derivative of the idempotency constraint $\boldsymbol{W} \boldsymbol{P}+\boldsymbol{P} \boldsymbol{W}=\boldsymbol{W}$. According to these conditions, given the density matrix at time step $t\left(\boldsymbol{P}_{(t)}\right)$, idempotent $\boldsymbol{P}_{(t+\Delta t)}$ is obtained by iteratively solving for the idempotency constraint. Then, given values of $\boldsymbol{P}_{(t)}$, $\boldsymbol{P}_{(t+\Delta t)}, \boldsymbol{W}_{(t)}$ and $\boldsymbol{W}_{\left(t+\frac{1}{2} \Delta t\right)}$, idempotent density matrix velocity $\boldsymbol{W}_{(t+\Delta t)}$ can be found by iteratively solving for the time derivative of the idempotency constraint.

Similarly to the propagation of the electronic degrees of freedom, for the nuclear positions one obtains

$$
\begin{equation*}
\boldsymbol{R}_{(t+\Delta t)}=\boldsymbol{R}_{(t)}+\boldsymbol{V}_{(t)} \Delta t-\frac{\Delta t^{2}}{2} \boldsymbol{M}^{-1}\left[\left.\frac{\partial E\left(\boldsymbol{R}_{(t)}, \boldsymbol{P}_{(t)}\right)}{\partial \boldsymbol{R}_{(t)}}\right|_{\boldsymbol{P}_{(t)}}\right] \tag{3.66}
\end{equation*}
$$

and for the nuclear velocities

$$
\begin{align*}
\boldsymbol{V}_{\left(t+\frac{1}{2} \Delta t\right)} & =\boldsymbol{V}_{(t)}-\frac{\Delta t}{2} \boldsymbol{M}^{-1}\left[\left.\frac{\partial E\left(\boldsymbol{R}_{(t)}, \boldsymbol{P}_{(t)}\right)}{\partial \boldsymbol{R}_{(t)}}\right|_{\boldsymbol{P}_{(t)}}\right]  \tag{3.67}\\
& =\frac{\boldsymbol{R}_{(t+\Delta t)}-\boldsymbol{R}_{(t)}}{\Delta t}, \tag{3.68}
\end{align*}
$$

and

$$
\begin{equation*}
\boldsymbol{V}_{(t+\Delta t)}=\boldsymbol{V}_{\left(t+\frac{1}{2} \Delta t\right)}-\frac{\Delta t}{2} \boldsymbol{M}^{-1}\left[\left.\frac{\partial E\left(\boldsymbol{R}_{(t+\Delta t)}, \boldsymbol{P}_{(t+\Delta t)}\right)}{\partial \boldsymbol{R}_{(t+\Delta t)}}\right|_{\boldsymbol{P}_{(t+\Delta t)}}\right] . \tag{3.69}
\end{equation*}
$$

There are no constraints for the nuclear motion, as the idempotency depends only on the electronic coordinates.

In practice, initial configurations of $\boldsymbol{R}_{(0)}, \boldsymbol{V}_{(0)}$ and $\boldsymbol{W}_{(0)}$ are known. At each time step the
density matrix is calculated with a cost equivalent to a one cycle of the self-consistent field approach. As previously described, values at consecutive time steps are derived from analytical gradients of energy and idempotency constraints.

Correct choice of the time step size ensures total energy conservation in the ADMP calculations. The requirement for small oscillations of the ADMP energy around the BO PES does not allow for as large time steps as the BOMD method. Good energy conservation of the ADMP method ( $\sim 10^{-5}$ Hartree) has been found to result from time steps two times smaller when comparing to the BOMD [65]. Finally, according to [65], ADMP trajectories can be obtained 3-4 times faster than when using the BOMD approach.

### 3.5 Microcanonical Metropolis Monte Carlo

Third approach to studying the fragmentation process is a statistical treatment based on the assumption of the internal thermodynamic equilibrium. The method, named Microcanonical Metropolis Monte Carlo $\left(\mathrm{M}_{3} \mathrm{C}\right)$, has been previously applied to several systems, such as: atomic metal clusters [74], neutral and singly charged carbon clusters [75]-[78] as well as singly charged acetylene [78]. The present work is the first attempt at investigation of decomposition of a heterocyclic molecule in a neutral and singly charged state using $\mathrm{M}_{3} \mathrm{C}$. In essence, the goal of the $\mathrm{M}_{3} \mathrm{C}$ method is to describe the fragmentation process with a lower computational cost than required by the ab initio Molecular Dynamics without significant loss in accuracy.

In the following sections, a theoretical basis of the $\mathrm{M}_{3} \mathrm{C}$ technique is presented, including general foundations of the method, interpretation of the final expression for the Density of States (DOS) and explanation of the stochastic sampling technique. Recently, a detailed theoretical description of the method has been published [78], presenting some improvements to the theory derived in [74] and [76]. The following is significantly based on these three studies.

### 3.5.1 Microcanonical ensemble

In statistical mechanics, a system can belong to a certain ensemble depending on the quantities defining it. Particularly, a system with fixed total energy belongs to a microcanonical ensemble. According to the Boltzmann's formula, the entropy $S$ of such isolated system at equilibrium is given by:

$$
\begin{equation*}
S=k_{B} \ln \Omega(E), \tag{3.70}
\end{equation*}
$$

where $k_{B}$ is the Boltzmann's constant and $\Omega(E)$ is the total DOS. The value of $\Omega(E)$ defines a number of accessible microstates with energy $E$ that, according to the Laplace principle of indifference, are equally probable. In a microcanonical ensemble with conserved total linear $P_{0}$ and angular $J_{0}$ momenta, the formula for the Density of States is given by

$$
\begin{equation*}
\Omega\left(E, P_{0}, J_{0}\right)=\int d \boldsymbol{\Gamma} \delta[\mathcal{H}(\boldsymbol{\Gamma})-E] \delta\left[\mathcal{J}(\boldsymbol{\Gamma})-\mathcal{J}_{0}\right] \delta\left[\mathcal{P}(\boldsymbol{\Gamma})-\mathcal{P}_{0}\right], \tag{3.71}
\end{equation*}
$$

where $\int d \boldsymbol{\Gamma}$ is the integral over the phase space $\boldsymbol{\Gamma}$ (values of all possible position and momentum variables), $\delta$ denotes Dirac's delta function and $\mathcal{H}(\boldsymbol{\Gamma})$ is the Hamiltonian of the system.

Considering the second law of thermodynamics, thermodynamic equilibrium is obtained by reaching the state of maximum entropy. Hence, an accurate description of the DOS is the most significant step of the $\mathrm{M}_{3} \mathrm{C}$ technique.

### 3.5.2 Approximation of the Density Of States

The $\mathrm{M}_{3} \mathrm{C}$ method relies on factorization of the DOS into a product of several, easily integrable components. The system of coordinates is defined in a laboratory frame, in which $\boldsymbol{\mathcal { R }}_{i}$ denotes the center of mass position of the $i$ th fragment and $\boldsymbol{\theta}_{i}$ is the orientation of the fragment $i$ with respect to its body-fix frame. Let $n$ denote number of atoms in the studied system and $N_{c}$ number of possible fragmentation channels. Firstly, through a convenient phase space channel decomposition, a $\left(3 n \times N_{c}\right)$-dimensional problem becomes $N_{c}$ uncoupled problems. The double well potential, taken as the pairwise interaction potential between fragments, allows for partition of the phase space into three regions according to the position of its local maximum and the asymptotic limit. Different interaction potentials are applied to channels that belong to either of the subspaces. As a result, the total DOS is given by a sum over possible channels such as

$$
\begin{equation*}
\Omega(E)=\sum_{j=1}^{N_{c}} \Omega_{e}\left(\boldsymbol{c}_{j}\right) \Omega_{n}\left(\boldsymbol{c}_{j}\right) \Omega_{c_{j}}(E), \tag{3.72}
\end{equation*}
$$

where $\Omega_{e}\left(\boldsymbol{c}_{j}\right)$ represents the electronic DOS, $\Omega_{n}\left(\boldsymbol{c}_{j}\right)$ denotes the combinatorial DOS and $\Omega_{\boldsymbol{c}_{j}}(E)$ is associated with the $\boldsymbol{c}_{j}$-th channel with the energy $E$. The electronic DOS introduces the electronic state degeneracy. If $N_{f}^{(j)}$ denotes number of fragments in channel $\boldsymbol{c}_{j}$ and $s_{i}^{(j)}$ is the $i$-th fragment in channel $\boldsymbol{c}_{j}$, then

$$
\begin{equation*}
\Omega_{e}\left(\boldsymbol{c}_{j}\right)=\prod_{i=1}^{N_{f}^{(j)}} \Omega_{e}\left(s_{i}^{(j)}\right) \tag{3.73}
\end{equation*}
$$

represents the total electronic DOS. The number of accessible microstates is calculated using the symmetry of the electronic wave function of each fragment as follows:

$$
\Omega_{e}(s)= \begin{cases}(2 S+1)(2 L+1), & \text { if } s \text { is an atom }  \tag{3.74}\\ (2 S+1), & \text { if } s \text { is a linear molecule }\left(M_{L}=0\right) \\ (2 S+1) 2\left|M_{L}\right|, & \text { if } s \text { is a linear molecule }\left(M_{L} \neq 0\right) \\ (2 S+1) 2 D, & \text { if } s \text { is not a linear molecule }\end{cases}
$$

Total spin $S$ and total orbital angular momentum $L$ quantum numbers specify values of $\Omega_{e}(s)$ for atoms. In the case of linear molecules, values of $\Omega_{e}(s)$ depend on the total spin and the component of $L$ along the molecular axis: $M_{L}$. For nonlinear molecules, $\Omega_{e}(s)$ is calculated using the degeneracy of irreducible representation: $D$, which equals to 1 for states A and B , and 2,3,4,5 for states E,F,G,H, respectively.

Second component of the total DOS, named combinatorial DOS, introduces the Gibbs' correction factor for the possibility of identical fragments in channel $\boldsymbol{c}_{j}$ :

$$
\begin{equation*}
\Omega_{n}\left(\boldsymbol{c}_{j}\right)=\frac{1}{\prod_{k} \boldsymbol{m}\left(\boldsymbol{s}_{k}^{(j)}\right)!} \delta\left\{\sum_{i=1}^{N_{f}^{(j)}} s_{i}^{(j)}-s_{0}\right\} \delta\left\{\sum_{i=1}^{N_{f}^{(j)}} z_{i}^{(j)}-z_{0}\right\}, \tag{3.75}
\end{equation*}
$$

where $\boldsymbol{m}\left(s_{k}^{(j)}\right)$ denotes the number of times $k$ th fragment appears in channel $\boldsymbol{c}_{j}$. Moreover, by including the Dirac's delta functions with the initial fragment identity $s_{0}$ and the initial charge $z_{0}$, the composition and charge conservation rules are satisfied.

The remaining component of the total DOS in eq. $3.72-\Omega_{c_{j}}(E)$ - represents the DOS of a fragmentation channel $\boldsymbol{c}_{j}$ with the energy $E$. The Hamiltonian model for a fragmentation channel is obtained by omitting the ro-vibrational couplings and consequently the vibrational contribution of each fragment can be integrated out from the total DOS, leading to

$$
\begin{equation*}
\Omega_{\boldsymbol{c}}(E)=\int \prod_{\mu=1}^{N_{f}} d E_{\nu \mu} \Omega_{\nu \mu}\left(\boldsymbol{c}, E_{\nu \mu}\right) \Lambda\left(\boldsymbol{c}, E-E_{\nu}\right), \tag{3.76}
\end{equation*}
$$

where $\Omega_{\nu \mu}\left(\boldsymbol{c}, E_{\nu \mu}\right)$ is the vibrational DOS of $\mu$ th fragment and $\Lambda(\boldsymbol{c}, E)$ denotes the combined translational and rotational contributions to the density of states. Next, by assuming a classical harmonic approximation of the fragment's internal degrees of freedom, the vibrational DOS takes the form of the density of states for $f_{\nu \mu}$-dimensional harmonic oscillator, given by

$$
\begin{equation*}
\Omega_{\nu \mu}(\boldsymbol{c}, E)=\frac{E^{f_{\nu \mu}-1}}{\hbar_{\nu \mu} \Gamma\left(f_{\nu \mu}\right)} \prod_{k=1}^{f_{\nu \mu}} \omega_{\mu k}^{-1} \tag{3.77}
\end{equation*}
$$

where $\Gamma$ denotes Euler's gamma function, $f_{\nu \mu}$ is the number of internal vibrational degrees of freedom of $\mu$ th fragment and $\omega_{\mu k}$ is the frequency of its $k$ th vibrational mode.

The final component $\Lambda(\boldsymbol{c}, E)$ comprises integration of the rotational motion, which is hindered by the coupling of the system's angular momentum with the fragments' orbital rotation. Firstly, definition of the linear momenta of constituent fragments in the center of mass laboratory-oriented system enables fixing $\mathcal{P}_{0}=0$ and the constraint for the linear momentum in eq. 3.71 can be integrated out. However, this approach can not be applied to the constraint for the angular momentum. The $\mathrm{M}_{3} \mathrm{C}$ method employs a technique proposed by Jellinek and Ly [79], which is based on representing the overall rotation of a nonrigid system as a rotation of a changing rigid body. This means that the tensor of inertia is adapted to the instantaneous position of fragments and the overall rotation and internal displacements can exchange energy. Consequently, the density of states for the translational and rotational motion takes the form of

$$
\begin{align*}
\Lambda(\boldsymbol{c}, E)= & \frac{(2 \pi)^{s / 2}}{\Gamma(s / 2)}\left(\frac{1}{M} \prod_{\mu=1}^{N_{f}} m_{\mu}\right)^{3 / 2} \int \frac{d^{f_{t}} \boldsymbol{\mathcal { R }}}{(2 \pi \hbar)^{f_{t}}} \frac{d^{f_{r}} \boldsymbol{\theta}}{(2 \pi \hbar)^{f_{r}}}  \tag{3.78}\\
& \times \operatorname{det} \boldsymbol{B}(\boldsymbol{\mathcal { R }}, \boldsymbol{\theta})^{1 / 2}\left[E-U(\boldsymbol{\mathcal { R }})-E_{\mathcal{J}_{0}}(\boldsymbol{\mathcal { R }})\right]^{s / 2-1},
\end{align*}
$$

where $s$ is the total number of translational and rotational degrees of freedom ( $s=f_{t}+f_{r}$ ), $m_{\mu}$ and $M$ are the mass of $\mu$ th fragment and total mass, respectively. Equation 3.78 includes the term $\boldsymbol{B}$, which results from integration of the angular momenta. Matrix $\boldsymbol{B}$ denotes the diagonal representation of the coupling matrix of inertia tensor, which initially includes effective inertia tensors for the $\mu$ th fragment (diagonal terms) and the strength of interaction between different fragments (off-diagonal terms). The integrals in eq. 3.78 represent the spatial occupation and the angular part of the eigenrotation of the fragments. The complexity of these integrals requires application of a method of approximation for the calculation of the total DOS. The approach employed by the $\mathrm{M}_{3} \mathrm{C}$ method is described in the following subsection.

### 3.5.3 Metropolis Monte Carlo Sampling

In practice, the Metropolis Monte Carlo procedure is used to integrate the configurational space in eq. 3.78 and sample the vibrational energy in eq. 3.77. In contrast to the regular Monte Carlo technique, the accessible states are not sampled uniformly, but the values of $\Omega(E)$ are the weighting factors leading to the most important parts of the phase space (here, region of maximum entropy). The $\mathrm{M}_{3} \mathrm{C}$ method employs the Metropolis algorithm [80], which allows one to find this region through the following procedure:

Step 1 A random configuration of the state vector $\chi_{i}$ for the given internal energy is chosen and corresponding $\operatorname{DOS} \Omega^{\prime}\left(\chi_{i}\right)$ is calculated.

Step 2 A new state vector $\chi_{i+1}$ is obtained through a small, random modification of the state variables and the new $\operatorname{DOS} \Omega^{\prime}\left(\chi_{i+1}\right)$ is computed.

Step 3 The acceptance ratio of the new configuration is obtained as

$$
\begin{equation*}
p\left(\chi_{i} \longrightarrow \chi_{i+1}\right)=\min \left(1, \frac{\Omega^{\prime}\left(\chi_{i+1}\right)}{\Omega^{\prime}\left(\boldsymbol{\chi}_{i}\right)}\right) \tag{3.79}
\end{equation*}
$$

Step 4 A random number $U_{(0,1)}$ is sampled from the uniform distribution.
Step 5 The new state vector is either accepted or rejected depending on the comparison with $U_{(0,1)}$. If $U_{(0,1)} \leq p$, the state $\boldsymbol{\chi}_{i+1}$ is accepted. Otherwise, the system returns to the initial state $\chi_{i}$.

Steps 2-5 are repeated until the accepted modifications constitute 30-50\% of all trials. Each transformation is followed by adjustment of the kinetic energy so that the total energy is conserved.

In the $\mathrm{M}_{3} \mathrm{C}$ method, the abstract objects which modify the state vectors are called reactors. The system's state vector $\chi$ denotes a phase space configuration determined by four variables: composition of the system $\boldsymbol{c}$ (includes number of fragments, their charge, geometry, electronic configuration and spin multiplicity), vibrational energy $\boldsymbol{E}_{\nu}$, Cartesian coordinates of the fragments' centres of mass $\boldsymbol{R}$ and their orientation in space $\boldsymbol{\theta}$. Following operations enable exploration of the state vectors space:

Vibrational reactor $(V)$ relies on random sampling of the vibrational energy. The maximum possible value is limited by the lowest dissociation energy of involved fragments. Consequently, the vibrational $\operatorname{DOS} \Omega_{\nu}(\boldsymbol{c}, E)$ is recalculated.

Rotational reactor $(R)$ denotes random sampling of the fragments' orientation from the uniform distribution. This operation modifies the angular momentum couplings between different fragments and the inertia tensors.

Translational reactor ( $T$ ) randomly samples new positions of each fragment, so that they fit in the reaction volume and do not overlap. As a result, the interacting potential between fragments is recomputed.

Structure reactor $\left(S_{n}\right)$ changes the system's composition according to a random search tree of all fragments from the database. Possible values of $n$ include $n=-1,0,1$, where $n$ determines the change in number of fragments. This reactor requires recomputation of all quantities.

The resulting sequence of accepted state vectors is called the Markov Chain. In general, a sequence of several thousand reactors guarantees a sufficient exploration of the phase space and can be written in a following way: $\boldsymbol{\chi}_{0} \xrightarrow{V} \boldsymbol{\chi}_{1} \xrightarrow{R} \boldsymbol{\chi}_{2} \xrightarrow{T} \boldsymbol{\chi}_{3} \xrightarrow{S_{1}} \boldsymbol{\chi}_{4} \xrightarrow{V} \ldots$

Eventually, the statistical expectation value of an observable $f$ is approximated as an arithmetic average

$$
\begin{equation*}
\langle f\rangle=\frac{1}{N} \sum_{i=1}^{N} f\left(\chi_{i}\right), \tag{3.80}
\end{equation*}
$$

where $N$ denotes total number of proposed changes of the state vector (both accepted and rejected). In order to account for the equilibration period of the system, the first $10 \%$ of generated state vectors is removed from the averaging procedure. This average is true within the ergodic hypothesis that the $\mathrm{M}_{3} \mathrm{C}$ method assumes. The ergodic theorem states that when the system has infinite time to evolve, the statistical time average of a certain property becomes a space average. This approach is widely used in studies of stochastic processes and the entropy of dynamical systems [81]. For a specific internal energy, the obtained observables include fragmentation channel probabilities, components of the total energy and different contributions to the total DOS.

## Chapter 4

## Computational details

The approach applied in the present work consists of three theoretical methodologies, previously detailed in Chapter 3. These three methods have been chosen due to the fact that they provide complementary information about the fragmentation process. Following section specifies the technical aspects of the applied theoretical techniques.

### 4.1 Ab initio Molecular Dynamics

Firstly, ab initio Molecular Dynamics simulations enabled the identification of the most probable reaction mechanisms occurring for different internal energies. The calculations were carried out using the ADMP method with the B3LYP functional and $6-31 \mathrm{G}(\mathrm{d}, \mathrm{p})$ basis set implemented in the Gaussian09 package [61]. The propagation time of the simulations has been limited to $t_{\max }=500 \mathrm{fs}$ for neutral and singly ionized furan and to $t_{\max }=300 \mathrm{fs}$ in the case of furan dication. Such duration of the simulations proved to be sufficient in observation of the separated fragmentation products. A time step of $\Delta t=0.1 \mathrm{fs}$ ensured good separation between electronic and nuclear degrees of freedom. Moreover, fictitious mass of $\mu_{e}=0.1 \mathrm{amu}$ has been chosen to guarantee conservation of the total energy. Modelling the experimental conditions of collision induced fragmentation is possible through taking the molecule optimized in the neutral state as input geometry in the dynamical simulations of ionized furan. This is in accordance with the Franck-Condon principle, stating that positions of the nuclei in the molecule experience no significant change under an electronic transition, such as ionization [82]. Therefore, either one or two electrons from the highest occupied molecular orbital were extracted and the excitation energy, varying from 5 to 30 eV in steps of 1 eV , was introduced into the system. Random distribution of the internal energy over all vibrational degrees of freedom and multiple simulations starting from the same structure made it possible to perform a statistical analysis of the fragmentation mechanism. For each internal energy of every charge state 150 calculations were run, leading to 3900 trajectories in total for each charge state. Dynamical calculations have been performed at the Centre of Informatics - Tricity Academic Supercomputer \& networK (CI TASK). The CPU time of the simulations varied significantly depending on the initial distribution of velocities, however, on average, single trajectory of 500 fs run for about 48 hours (the average taken over 150 trajectories of 15 eV deposited to singly ionized furan).

The large amount of obtained data imposes the use of external programs, which efficiently parse the output files. A convenient choice are bash scripts that work quickly with the outputs stored at the computing servers. The data analysis was based on the following:

Step 1 Extraction of geometries and charge distributions from the last step of the Gaussian output files,

Step 2 Determination of the exit channel of every trajectory by assuming bonds to be broken when distance between atoms exceeded $R=2.5 \AA$,

Step 3 Counting and classification of final exit channels depending on the number of produced fragments for more comprehensible interpretation.

All MD output files were treated with the described procedure, which only provided the information about the final step of the simulation. It is equally important to have an idea of the mechanisms taking place during the simulations, so some trajectories were viewed using the MOLDEN visualization package [83]. Additionally, trajectories of the most abundant processes were treated with a script extracting geometries at consecutive time steps. As a consequence, intermediate processes were explored. In summary, the features that have been extracted from the MD include structures and charge distribution of fragments at a final time step, channels probabilities, type of observed processes and their average times and sequence of events in a specific group of processes.

### 4.2 Exploration of the Potential Energy Surface

As the lifetime of some reactions might be longer than 500 fs , it is necessary to carry out an investigation of structural and energetic features of the species participating in the observed processes. Hence, as a second step, exploration of the Potential Energy Surface has been performed. For this purpose, quantum chemistry calculations of reactants, intermediates, transition states and products were carried out. Geometry optimizations have been performed at the B3LYP/6-311++G(3df,2p) level of theory for the neutral molecule and B3LYP/6-311++G(d,p) for charged furan. This level of theory has been extensively applied to studies of hydrocarbons [84], [85] and heterocyclic molecules [86], [87] and proves to be an adequate choice for molecular and electronic structure calculations of furan. The harmonic vibrational frequencies and zero point energy corrections were predicted using the same level of theory. All minima are characterized by having positive harmonic vibrational frequencies and all transition states present only one imaginary frequency. In search for the geometries of transition states three approaches were interchangeably applied:

- optimization of the trial geometry,
- relaxed scans along the reaction coordinate,
- the Synchronous Transit-Guided Quasi-Newton method that requires reactants and products as input.

The first and the second method were used with similar frequency, however, QST2 procedure failed most of the time. To check the correct connections of the critical points on the Potential Energy Surface, Intrinsic Reaction Coordinate (IRC) calculations have been performed for
successfully optimized transition states. Again, all quantum chemical calculations were carried out using Gaussian09 package [61] and computing resources provided by the Wrocław Centre for Networking and Supercomputing (WCSS) and CI TASK. The graphical interface used for visualization of molecular geometries was GaussView version 5.0 .8 [88].

### 4.3 Microcanonical Metropolis Monte Carlo

Finally, simulations of the Microcanonical Metropolis Monte Carlo technique have been performed. Results presented in this work were obtained with the 2.0 version of the $\mathrm{M}_{3} \mathrm{C}$ program. The source files were provided by Néstor F. Aguirre, the first author of [78], and installed on the computing cluster of CI TASK, Tryton. The $\mathrm{M}_{3} \mathrm{C}$ method was employed to study fragmentation of only neutral and singly ionized furan, because it is not yet applicable to investigation of multiply charged molecules.

### 4.3.1 Input information

First, a database of all possible fragmentation products is necessary to perform the $\mathrm{M}_{3} \mathrm{C}$ simulations. The $\mathrm{M}_{3} \mathrm{C}$ interface with the Gaussian package allows for a stochastic search of isomers by optimization of fixed number of trial geometries. Consequently, 226 neutral and 243 singly ionized isomers were successfully optimized at the B3LYP $/ 6-311++G(d, p)$ level of theory. All obtained geometries are presented in Appendix A. In a complete fragment database every isomer is characterized by: electronic energy, geometry in an xyz format, vibrational frequencies, symmetry of the wave function and molecular symmetry. All this information is required as an input of the $\mathrm{M}_{3} \mathrm{C}$ simulation. Moreover, it is necessary to establish the lowest energy dissociation channel of every fragment in the database. This is done automatically through a tool implemented in the $\mathrm{M}_{3} \mathrm{C}$ package, which samples the feasible dissociation channels and finishes with the one with the lowest energy.

### 4.3.2 Convergence search

Before performing any Monte Carlo calculation it is important to check the influence of the simulation parameters on the obtained results. Therefore, performance of the following parameters has been tested:

- system radius - $R_{\text {sys }}$ - specifies the radius (in $\AA$ ) of the available reaction volume,
- Markov Chain sequence - $M C_{\text {seq }}$ - indicates the sequence of events acting on the studied system,
- number of events - $N_{e v}$ - defines number of steps in the sampling procedure leading to the maximum entropy region. Single modification of the state vector by a reactor corresponds to one event,
- number of experiments - $N_{\text {exp }}$ - number of performed Monte Carlo simulations. Each experiment starts with a randomly selected initial state vector $\chi_{0}$. Final fragmentation
probabilities are averaged over all experiments and errors are calculated as standard deviations from the mean values.

In this section, the search for convergence of the $\mathrm{M}_{3} \mathrm{C}$ simulations is described. To minimize the computational time of the trial simulations, the fragments database was limited to only the most important species. The adopted criteria of a successful simulation were the error values, calculated as a standard deviation from the mean value of a channel probability. Typically, a good Monte Carlo calculation is characterized by errors below $10 \%$. In order to have a single criterion assessing the simulation's accuracy, the errors in channels were averaged according to the following formula

$$
\begin{equation*}
\sigma_{\text {sim }}=\frac{1}{J} \sum_{j=1}^{J} \sum_{c_{j}=1}^{C_{j}} \frac{\sigma_{c_{j}}}{C_{j}}, \tag{4.1}
\end{equation*}
$$

where $\sigma_{c_{j}}$ is the error in channel $c$ for the $j$ th energy scan. The value of $C_{j}$ denotes total number of channels for the $j$ th energy scan and $J$ total number of performed energy scans (here 21).

Firstly, the $R_{\text {sys }}$ parameter has been tested. The essential requirement is that the parent molecule and dissociation products should fit into the volume $V_{R}=\frac{4}{3} \pi R_{\text {sys }}^{3}$. In the previous $\mathrm{M}_{3} \mathrm{C}$ application to investigation of fragmentation of carbon clusters [76] the authors suggested that $R_{\text {sys }}=N_{T} \cdot 1 \AA$ and $R_{s y s}=N_{T} \cdot 2 \AA$ ( $N_{T}$ denotes total number of carbon atoms) provided practically the same results. As furan molecule consists of nine atoms, the values of $R_{\text {sys }}=$ $\{10 \AA, 13 \AA, 15 \AA, 20 \AA\}$ have been tested and as in [76] no significant changes have been observed. Consequently, the $R_{\text {sys }}=13 \AA$ has been chosen for the future simulations. Optimization of the rest of simulation parameters is discussed separately for the neutral and ionized case.

For the neutral furan, the Markov Chain sequence and number of events were tested simultaneously while number of experiments was kept constant ( $N_{\text {exp }}=5$ ). Figure 4.1 shows the averaged error as a function of the number of events for different Markov Chain sequences. The notation used in the figure denotes following sequences:

| $\mathrm{MC}_{1 / 5 S}$ | $5 \times(\mathrm{V}, \mathrm{T}, \mathrm{R}) \mathrm{S}: 0,5 \times(\mathrm{V}, \mathrm{T}, \mathrm{R}), \mathrm{S}:-1: 1$ |
| :--- | :--- |
| $\mathrm{MC}_{1 S}$ | $\mathrm{~V}, \mathrm{~T}, \mathrm{R}, \mathrm{S}: 0, \mathrm{~V}, \mathrm{~T}, \mathrm{R}, \mathrm{S}: 1:-1$ |
| $\mathrm{MC}_{5 S}$ | $\mathrm{~V}, \mathrm{~T}, \mathrm{R}, 5 \times \mathrm{S}: 0, \mathrm{~V}, \mathrm{~T}, \mathrm{R}, 5 \times \mathrm{S}: 1:-1$ |
| $\mathrm{MC}_{5,5 S}$ | $5 \times \mathrm{S}: 0, \mathrm{~V}, \mathrm{~T}, \mathrm{R}, 5 * \mathrm{~S}: 0, \mathrm{~V}, \mathrm{~T}, \mathrm{R}, 10 \times \mathrm{S}: 1:-1$ |
| $\mathrm{MC}_{10 S}$ | $\mathrm{~V}, \mathrm{~T}, \mathrm{R}, 10 \times \mathrm{S}: 0, \mathrm{~V}, \mathrm{~T}, \mathrm{R}, 10 \times \mathrm{S}: 1:-1$ |
| $\mathrm{MC}_{20 S}$ | $\mathrm{~V}, \mathrm{~T}, \mathrm{R}, 20 \times \mathrm{S}: 0, \mathrm{~V}, \mathrm{~T}, \mathrm{R}, 20 \times \mathrm{S}: 1:-1$ |

The definition of each reactor is described in the section 3.5.3. The main difference between tested sequences is the amount and order of the $S$ reactors (which have the highest computational cost). From Figure 4.1 it can be seen that with increasing number of $S$ reactors the averaged error decreases until reaching 5 reactors in the MC sequence. Then, the simulation's accuracy stabilizes and does not substantially improve when more $S$ reactors are added. Moreover, with the increasing number of events the averaged error reaches a plateau starting from around 800000 events. Consequently, the values chosen for the next step of the convergence


FIGURE 4.1 Results of optimization of the MC sequence and number of events of the $\mathrm{M}_{3} \mathrm{C}$ simulation of neutral furan with $N_{\text {exp }}=5$.


FIGURE 4.2 Panel a): results of the optimization of the number of experiments of the $\mathrm{M}_{3} \mathrm{C}$ simulation of neutral furan with $M C_{5 S}$ and $N_{e v}=800000$. Panel b): computational time of the respective simulations.
search are: $M C_{\text {seq }}=V, T, R, 5 \times S: 0, V, T, R, 5 \times S: 1:-1$ and $N_{e v}=800000$. Finally, the optimum number of experiments was tested. Figure 4.2 presents averaged errors as a function of the number of experiments together with the CPU times of the corresponding simulations. The number of experiments chosen for the final calculation was $N_{\text {exp }}=50$. At this point, the averaged error value stabilizes at around $1.2 \%$ (highlighted with a blue circle in Figure 4.2) and the computational cost is justifiable.

The $\mathrm{M}_{3} \mathrm{C}$ simulations of the singly ionized furan include an improvement to the phase space sampling method. The new technique, named SEQUENTIAL, differs from the RANDOM sampling in allowed transitions as steps in the Markov Chain sequence. SEQUENTIAL sampling removes $S$ reactors that in a way are "unphysical". This modification works under the assumption that if the system has already lost a light fragment, it is unlikely that it will reattach to the
parent molecule and then recombine. As an example, a forbidden reaction under the SEQUENTIAL sampling method would be the second transition in sequence: $\mathrm{H}_{4} \mathrm{C}_{4} \mathrm{O}^{+} \rightarrow \mathrm{H}+\mathrm{H}_{3} \mathrm{C}_{4} \mathrm{O}^{+}$ $\rightarrow \mathrm{C}+\mathrm{H}_{4} \mathrm{C}_{3} \mathrm{O}^{+}$. Consequently, the configurational space is sampled more efficiently and the computational cost of calculations decreases. Again, the first step of the convergence search was the simultaneous optimization of the Markov Chain sequence and number of events, while number of experiments was kept constant ( $N_{\text {exp }}=100$ ). Figure 4.3 demonstrates decrease of the averaged error until around $N_{e v}=250000$. As a compromise between computational cost and accuracy, $\mathrm{MC}_{1 S}$ and $\mathrm{MC}_{5 S}$ sequences with 200000 number of events were chosen for subsequent testing of the number of experiments. According to the results presented in Figure 4.4, the optimum value of experiments for the $\mathrm{M}_{3} \mathrm{C}$ simulation of singly ionized furan is $N_{\text {exp }}=500$ with $\mathrm{MC}_{5 S}$ (highlighted with a blue circle).


Figure 4.3 Panel a): Results of optimization of the MC sequence and number of events of the $\mathrm{M}_{3} \mathrm{C}$ simulation of singly ionized furan. Panel b): computational time of the respective simulations.


FIGURE 4.4 Panel a): results of the optimization of the number of experiments of the $\mathrm{M}_{3} \mathrm{C}$ simulation of singly ionized furan with $N_{e v}=200000$. Panel b): computational time of the respective simulations.

In summary, parameters chosen for the final calculations are presented in Table 4.1. Both in the neutral and singly ionized case the energy was scanned up to 20 eV every 0.5 eV . As a result of the performed simulations, similarly to the ADMP method, a statistical distribution of all possible fragmentation channels as a function of the internal energy is obtained. Additional output information include possible reactions and the correlation between pairs of energy components.

TABLE 4.1 Final parameters of the $\mathrm{M}_{3} \mathrm{C}$ simulations

| Parameter | $\mathbf{H}_{4} \mathrm{C}_{4} \mathbf{O}$ | $\mathrm{H}_{4} \mathrm{C}_{4} \mathbf{O}^{+}$ |
| :--- | :---: | :---: |
| System Radius |  |  |
| Markov chain sequence | $\mathrm{V}, \mathrm{T}, \mathrm{R}, 5 \times \mathrm{S}: 0, \mathrm{~V}, \mathrm{~T}, \mathrm{R}, 5 \times \mathrm{S}: 1:-1$ |  |
| Number of experiments | 50 | 500 |
| Number of events | 800000 | 200000 |
| Sampling method | RANDOM | SEQUENTIAL |

### 4.3.3 Fitting of the energy distribution function

As an output, the $\mathrm{M}_{3} \mathrm{C}$ method provides fragmentation probabilities as a function of the internal energy. Direct comparison of the theoretical and experimental results is possible if the distribution of energy deposited during the collision is known. Such functions have been previously reported only for several systems. Those procedures relied either on coincidence measurement of the scattered negative ion and the fragmentation products [89] or combination of photon and ion experiments [90]. Theoretical determination of energy transfer is also possible by calculating the nuclear and electronic stopping powers [91] or evaluating the calculated transition amplitudes [92], [93]. However, basing on the semiempirical arguments, distribution of the deposited energy might as well result from fitting of an analytical function so that the errors between theoretical and measured branching ratios are minimized. This last approach is implemented in the $\mathrm{M}_{3} \mathrm{C}$ software package and was applied in the present work. The employed fitting procedure is described below.

A branching ratio $R_{i}$ of a channel $i$ in a microcanonical ensemble is given by

$$
\begin{equation*}
R_{i}=\int_{0}^{\infty} f(E) P_{i}(E) d E \quad \text { for } \quad i=1,2, \ldots, I \tag{4.2}
\end{equation*}
$$

where $f(E)$ is the normalized energy distribution function and $P_{i}(E)$ is the fragmentation probability of a channel $i$. The form of function $f(E)$ has been chosen so that it represent a Boltzmann distribution at higher temperatures. A Slater-type basis set ensures the required features of a one-maximum distribution and exponential decay at long range. Hence, the energy distribution function takes the form of

$$
\begin{equation*}
f(E)=\sum_{k=1}^{K} c_{k} B_{k}(E), \quad \text { where } \quad B_{k}(E)=B_{\left\{n_{k}, l_{k}\right\}}(E)=\frac{1}{l_{k}!}\left(\frac{1}{n_{k}}\right)^{l_{k}+1} E^{l_{k}} e^{-E / n_{k}} . \tag{4.3}
\end{equation*}
$$

The normalization of the $f(E)$ function is satisfied by the constrains on the $c_{k}$ coefficients: $\sum_{k=1}^{K} c_{k}=1$ and basis set elements $B_{k}(E): \int_{0}^{\infty} B_{k}(E) d E=1$. Effectively, determination of the parameters $c_{k}, n_{k}$ and $l_{k}$ is the goal of the fitting procedure. The new form of the branching ratio $R_{i}$ now reads

$$
\begin{align*}
R_{i} & =\sum_{k=1}^{K} c_{k} A_{i k}, \quad \text { where }  \tag{4.4}\\
A_{i k} & =\int_{0}^{\infty} B_{k}(E) P_{i}(E) d E \quad \text { for } \quad i=1,2, \ldots, I \quad \text { and } \quad k=1,2, \ldots, K \tag{4.5}
\end{align*}
$$

This set of equations can not be uniquely solved, as it describes an overdetermined system (number of channels $I$ is larger than the number of basis set elements $K$ ). Hence, a least squares method has been applied in order to minimize the sum of squared differences between theoretical $R_{i}$ and experimental $R_{i}^{\text {exp }}$ branching ratios, which reads

$$
\begin{equation*}
S=\sum_{i=1}^{I}\left[\sum_{k=1}^{K} c_{k} A_{i k}-R_{i}^{e x p}\right]^{2}, \tag{4.6}
\end{equation*}
$$

in a matrix form:

$$
\begin{equation*}
S=\operatorname{Tr}\left[\left(\mathbf{A} \mathbf{c}-\mathbf{R}^{e x p}\right)^{T}\left(\mathbf{A c}-\mathbf{R}^{e x p}\right)\right] \tag{4.7}
\end{equation*}
$$

If $\hat{\mathbf{c}}$ denotes the values of $\mathbf{c}$ that minimize the $S$, then

$$
\begin{equation*}
\left.\frac{d S}{d \mathbf{c}}\right|_{\mathbf{c}=\hat{\mathbf{c}}}=2 \mathbf{A}^{T}\left(\mathbf{A} \hat{\mathbf{c}}-\mathbf{R}^{e x p}\right)=0 \tag{4.8}
\end{equation*}
$$

Finally, the problem simplifies to the solution of

$$
\begin{equation*}
\mathbf{A} \hat{\mathbf{c}}=\mathbf{R}^{e x p}, \quad \text { where } \quad \hat{\mathbf{c}} \geq \mathbf{0} \quad \text { and } \quad \hat{\mathbf{c}}^{T} \hat{\mathbf{c}}=1 \tag{4.9}
\end{equation*}
$$

In practice, equation 4.9 is transformed to

$$
\left[\left(\begin{array}{cc}
\mathbf{I} & \mathbf{0}  \tag{4.10}\\
\mathbf{0} & \eta
\end{array}\right)\binom{\mathbf{A}}{1}\right]\binom{\hat{\mathbf{c}}}{0}=\left(\begin{array}{cc}
\mathbf{I} & \mathbf{0} \\
\mathbf{0} & \eta
\end{array}\right)\binom{\mathbf{R}^{e x p}}{1},
$$

where $\mathbf{I}$ is the identity matrix of size $I \times K$ and $\eta$ is a real number that is set to $10^{8}$ in this particular calculation. The transformation to eq. 4.10 allows one to apply the standard Lawson and Hanson's algorithm [94] for solution of the least square problems.

As an example of the fitting procedure, Figure 4.5 presents the fitted energy distribution functions for collision of $\mathrm{Ar}^{11+}$ ions ( panel a) ) and electrons (panel b) ) with singly ionized furan. Their interpretation and convolution with species probabilities are provided in the Chapter 5. Here, a difference can be noticed in the shape of obtained functions through inclusion of several basis set elements. The total energy distribution function of collision with $\mathrm{Ar}^{11+}$ exhibits a maximum at approx. 1 eV and a second node at 6 eV . However, the total energy distribution function of collision with electrons is a single maximum distribution with the peak
centred at approx. 4 eV . These results show that the applied fitting procedure is adequate for reproducing the experimental branching ratios of various kinds of collisional systems.



FIGURE 4.5 Results of the fitting to the experimental branching ratios measured for the collsion of singly ionized furan with a) $\mathrm{Ar}^{11+}$ ions and $\mathbf{b}$ ) electrons.

## Chapter 5

## Results and discussion

### 5.1 Neutral furan

### 5.1.1 Molecular Dynamics

Results of the dynamical simulations of neutral furan are presented in Figures 5.1-5.3. Statistical analysis of the obtained trajectories ( 3900 overall) allowed to identify the most abundant processes presented in Figure 5.1 a). The following description of the observed processes is divided into four groups of possible mechanisms: (1) isomerization, (2) fragmentation, (3) H/ $\mathrm{H}_{2}$


FIGURE 5.1 Results of the ADMP simulations of neutral furan: total occurrence of a) observed processes b) number of fragments as a function of internal energy.
loss + isomerization and (4) H/ $\mathrm{H}_{2}$ loss + fragmentation. The first process to appear is isomerization at 9 eV and it remains a dominant process until the energy of 16 eV . Secondly, we can observe skeleton fragmentation starting at 10 eV and becoming a dominant process between the energies of 17 and 23 eV . Channels that include H and $\mathrm{H}_{2}$ loss followed by isomerization both start at the energy of 13 eV and reach maximum probability at 24 eV and 19 eV , respectively. Finally, since the energy of $22 \mathrm{eV} \mathrm{H} / \mathrm{H}_{2}$ loss followed by fragmentation become the dominant processes. Figure 5.1 b) presents produced number of fragments depending on the energy applied to the system. It can be noticed that, as expected, for lowest energies furan molecule does not decompose. Two-body fragmentation is the dominant process for the energy range $17-23 \mathrm{eV}$. Afterwards, three-body fragmentation channels prevails.
a) Isomerization

b) Fragmentation

c) $\mathrm{H} \operatorname{loss}$


FIGURE 5.2 Results of the ADMP simulations of neutral furan: snapshots of the most significant trajectories.

In the case of furan, an isomerization process can indicate either ring opening, hydrogen transfer to neighbouring atom or rotation of the dihedral angle and breaking of the planar symmetry of the molecule. The panel a) in Figure 5.2 presents five furan isomers that dominate the MD and how they evolve in time. Their order corresponds to how abundant they were throughout the entire energy range, from the most (panel 1)) to least (panel 5)) observed. These exemplifying snapshots show that the required rearrangements take place late in the


FIGURE 5.3 Results of the ADMP simulations of neutral furan: Most important channels as a function of internal energy. Only channels that appeared at least $10 \%$ at a certain point in the energy range are presented. Numbers in brackets of the panel a) indicate numbering of isomers in the Potential Energy Surface exploration.
dynamics and if the system was given more simulation time it could potentially evolve until fragmentation. As it is shown in Figure 5.3 a), the most prevalent furan isomer corresponds to formyl-allene structure that can be achieved by 1,2 hydrogen transfer $\left(\mathrm{H}_{2} \mathrm{C}=\mathrm{C}=\mathrm{CH}-\mathrm{CHO}, 177\right.$ trajectories in total). Next most abundant isomer - alkyne-alcohol - is produced by H transfer to the oxygen atom ( $\mathrm{HC} \equiv \mathrm{C}-\mathrm{CH}-\mathrm{CH}-\mathrm{OH}, 110$ trajectories). Third most populated isomerization channel can be seen as cyclopropene substituted by a CHO group (67 trajectories). This isomer does not include hydrogen transfer, but relies on ring opening and cyclization of three carbon atoms. The following isomers are a formyl-alkyne ( $\mathrm{HC} \equiv \mathrm{C}-\mathrm{CH}_{2}-\mathrm{CHO}, 36$ trajectories), achieved by $2,3 \mathrm{H}$ transfer and a structure $\mathrm{H}_{2} \mathrm{C}=\mathrm{CH}-\mathrm{CH}=\mathrm{C}=\mathrm{O}$ ( 28 trajectories), achieved by two subsequent hydrogen transfers. It is worth pointing out that decreasing probability of isomerization at higher energies does not reflect reduced relevance of the isomerization process.

This mechanism remains valid, but simply occurs earlier in the dynamics and at $t=500$ fs is already followed by fragmentation.

Channels marked as skeleton fragmentation involve cleavage of $\mathrm{C}-\mathrm{O}$ and $\mathrm{C}-\mathrm{C}$ bonds, usually after prior isomerization, but does not allow $\mathrm{H} / \mathrm{H}_{2}$ loss. In significant majority of considered trajectories $\mathrm{C}-\mathrm{O}$ bond is the first to break. The panel b) in Figure 5.2 presents illustrative time evolution of two most populated fragmentation channels: $\mathrm{HCCH}+\mathrm{H}_{2} \mathrm{CCO}(\mathbf{1})$ ) and CO $+\mathrm{H}_{4} \mathrm{C}_{3}$ (2)-4)). Production of exit channel $\mathrm{HCCH}+\mathrm{H}_{2} \mathrm{CCO}$ starts with $\mathrm{C}-\mathrm{O}$ bond break and is followed by simultaneous $1,2 \mathrm{H}$ transfer and C-C break. As it can be noticed from panel b) of Figure 5.3, fragmentation into acetylene $(\mathrm{HCCH})$ and ethenone $\left(\mathrm{H}_{2} \mathrm{CCO}\right)$ appears first in the dynamical simulations and is the most abundant mechanism of furan decomposition into two fragments. Channel $\mathrm{CO}+\mathrm{H}_{4} \mathrm{C}_{3}$ can be obtained in a few different ways, depending on the final isomer of $\mathrm{H}_{4} \mathrm{C}_{3}$. The most populated channels comprise either two $2,1 \mathrm{H}$ transfers leading to allene $\left(\mathrm{H}_{2} \mathrm{CCCH}_{2}\right)$ or 3,2 and $1,2 \mathrm{H}$ transfer leading to propyne $\left(\mathrm{H}_{3} \mathrm{CCCH}\right)$. Least populated channel produces cyclopropene $\left(\mathrm{H}_{2} \mathrm{CCHCH}\right)$ and requires cyclization and one H transfer. The total numbers of trajectories producing mentioned isomers of $\mathrm{H}_{4} \mathrm{C}_{3}$ are 96,44 and 35 , respectively.

Third observed process was found to be $\mathbf{H} / \mathbf{H}_{2}$ loss followed by isomerization. As presented in panel c) of Figure 5.3, single H loss and subsequent isomerization appears early in the energy range, however, it has to be stressed again that the remaining $\mathrm{H}_{3} \mathrm{C}_{4} \mathrm{O}$ species might fragment, given more time to evolve. A competition between $\mathrm{H}_{\alpha}$ and $\mathrm{H}_{\beta}$ elimination can be noticed, however, majority of the cases of single hydrogen loss occurs from $\alpha$ position ( 91 vs 73 trajectories, respectively). Channels of $\mathrm{H}_{2}$ loss are also highly observed. Particularly, significant prevalence of $\mathrm{H}_{2}$ loss from $\alpha$ and $\beta$ positions of one side of the furan ring can be noticed. The frequency of $\mathrm{H}_{2}$ loss in a decreasing order is: adjacent $\mathrm{H}_{\alpha}$ and $\mathrm{H}_{\beta}(64 \%)>$ opposite $\mathrm{H}_{\alpha}$ and $\mathrm{H}_{\beta}(15 \%)>$ two $\mathrm{H}_{\alpha}(11 \%)>$ two $\mathrm{H}_{\beta}(10 \%)$.

The most abundant three-body fragmentation channel has been found to produce fragments $\mathrm{H}_{2} \mathrm{C}_{3}, \mathrm{CO}$ and $\mathrm{H}_{2}$ and at the same time to exhibit second highest total occurrence throughout all energies. $\mathrm{H}_{2}$ loss from adjacent $\alpha$ and $\beta$ positions remains the most abundant configuration of molecular hydrogen loss with the total occurrence being: adjacent $\mathrm{H}_{\alpha}$ and $\mathrm{H}_{\beta}(61 \%)>$ two $\mathrm{H}_{\alpha}(18 \%)>$ opposite $\mathrm{H}_{\alpha}$ and $\mathrm{H}_{\beta}(13 \%)>$ two $\mathrm{H}_{\beta}(8 \%)$. The most important channels of H loss appear after the channel of $\mathrm{H}_{2}$ loss, first at 15 eV producing $\mathrm{H}_{2} \mathrm{C}_{3}, \mathrm{CO}$ and H and later at 20 eV producing $\mathrm{HC}_{2} \mathrm{O}, \mathrm{H}_{2} \mathrm{C}_{2}$ and H . Snapshots of mentioned channels in panel c) of Figure 5.2 show that H loss takes place at around 20-40 fs. Subsequently, it can be followed by H transfer (decomposition to $\mathrm{H}_{3} \mathrm{C}_{3} / \mathrm{CO} / \mathrm{H}$ ) or can directly fragment (decomposition to $\mathrm{HC}_{2} \mathrm{O} / \mathrm{H}_{2} \mathrm{C}_{2} / \mathrm{H}$ ). Alike in the process of H loss followed by isomerization, hydrogen is mainly eliminated from $\alpha$ position ( $66 \%$ of trajectories).

### 5.1.2 Potential Energy Surface

Complementary information on relative stability of structures obtained in the MD and their reaction pathways are required to understand production yields of important exit channels.

Moreover, exploration of Potential Energy Surface enables extending the dynamical simulations of trajectories that could still undergo some processes, but were limited by the simulation time. Calculated pathways, presenting minima and transition structures optimized at the B3LYP/6-311++G(3df,2p) level of theory, are displayed in Figures 5.4-5.7. Correspondingly to the discussion of MD results, description of PES follows a similar scheme. Isomerization of the system prior to the fragmentation is considered first, followed by explanation of the skeleton fragmentation, H loss and finally $\mathrm{H}_{2}$ loss. Previous theoretical studies [26], [28] focused on isomerization and fragmentation processes, however, hydrogen elimination as well as multifragmentation have never been studied before.

Search for possible furan isomers was mainly based on the mechanisms observed in the Molecular Dynamics simulations. Depending on the first step of the process, five isomerization pathways (p1-p5), shown in Figure 5.4, can be distinguished. The lowest energy barrier is associated with $1,2 \mathrm{H}$ migration to form cyclic $\alpha$-carbene (1) - a structure with two unshared electrons localized on the same $\mathrm{C}_{\alpha}$ atom. Second pathway - p2 - corresponds to $2,1 \mathrm{H}$ transfer to form $\beta$-carbene (2). It is worth pointing out that no carbene structures were found at the end of MD simulations, the reason being the known short lived and highly reactive character of carbenes. Structure $\mathbf{2}$ can further isomerize to formyl-allene ( $\mathbf{3}$ and $\mathbf{4}$ ) through elongation of the C-O bond. This molecule can also be obtained directly from furan by concerted H transfer and ring opening ( $\mathrm{p}^{\prime}$ ), but requires overcoming a higher energy barrier. Low barrier for obtaining formyl-allene is consistent with high abundance of this isomer in MD calculations (177 trajectories).

Further hydrogen migration from $\mathrm{C}_{\alpha}(4)$ to oxygen atom with a transition structure located at 2.66 eV gives structure 5, the second most populated isomer in MD simulations ( 110 trajectories). Alternatively, from formyl-allene (4) a higher energy barrier of 3.14 eV was found for $1,4 \mathrm{H}$ transfer leading to stable structures $\mathbf{9}$ and $\mathbf{1 0}$, the lowest populated isomers in MD.

Third pathway - p3 - connects furan and structures 7 and 8 by 2,3 H transfer through the highest energy barrier computed for direct transition from furan, viz. 3.74 eV . On the other hand, structure 8 can be also obtained from formyl-allene (4), however the energy barrier for such isomerization is higher $(3.83 \mathrm{eV})$ and more steps of rearrangement are required. The fourth pathway - p4 - is associated with the ring opening by cleavage of the C-O bond and implies energy barrier of 3.52 eV . Obtained minima 13 and 14 correspond to isomers of the third most populated channel ( 67 trajectories). Pathway p5 also starts with cleavage of the $\mathrm{C}-\mathrm{O}$ bond, but the calculated transition structure is located 0.08 eV higher than the first TS of p4 and yields unstable isomers, not found in the MD.


Figure 5.4 Potential Energy Surface for the isomerization process. Energies calculated at B3LYP/6-311++G(3df,2p) level of theory are given in eV relative to furan. Zero point energy (ZPE) corrections are included. Transition structures are named with regard to the minima they connect. The total number of trajectories obtained in the MD is indicated for five families of isomers.

TABLE 5.1 Comparison of ADMP and PES exploration results for the isomerization process.

| Isomer | Total number <br> of trajectories | Structure | Energy <br> barrier <br> $[\mathbf{e V}]$ | Number <br> of TS | Energy <br> barrier <br> $[\mathrm{VV}][28]$ |
| :--- | :--- | :--- | :--- | :--- | :--- |
| $\mathrm{H}_{2} \mathrm{C}=\mathrm{C}=\mathrm{CH}-\mathrm{CHO}$ | 177 | $\mathbf{3}$ and $\mathbf{4}$ | 3.03 | 2 | 2.99 |
| $\mathrm{HC} \equiv \mathrm{C}-\mathrm{CH}-\mathrm{CH}-\mathrm{OH}$ | 110 | $\mathbf{5}$ and $\mathbf{6}$ | 3.03 | 3 | - |
| $\mathrm{cyc}(\mathrm{HC}=\mathrm{CH}-\mathrm{CH})-\mathrm{CHO}$ | 67 | $\mathbf{1 3}$ and $\mathbf{1 4}$ | 3.52 | 1 | - |
| $\mathrm{HC} \equiv \mathrm{C}-\mathrm{CH}_{2}-\mathrm{CHO}$ | 36 | $\mathbf{7}$ and $\mathbf{8}$ | 3.74 | 1 | 3.69 |
| $\mathrm{H}_{2} \mathrm{C}=\mathrm{CH}-\mathrm{CH}=\mathrm{C}=\mathrm{O}$ | 28 | $\mathbf{9}$ and $\mathbf{1 0}$ | 3.14 | 4 | $4.41^{a}$ |

${ }^{a}$ different path to obtain this isomer

As an isomerization summary and a link between dynamical results and exploration of PES for this process, Table 5.1 presents total occurrence in MD, lowest energy barrier and number of steps (transitions states) required to reach the most important furan isomers. It can be seen that the lowest energy barrier is associated with the highest number of trajectories. Moreover, although producing structures $\mathbf{9}$ and $\mathbf{1 0}$ requires overcoming second lowest energy barrier, their occurrence in MD is least abundant because of several steps required to reach these isomers.

Figure 5.5 demonstrates possible pathways of fragmentation into two channels: $\mathrm{HCCH}+$ $\mathrm{H}_{2} \mathrm{CCO}$ and $\mathrm{CO}+\mathrm{H}_{4} \mathrm{C}_{3}$. From $\alpha$-carbene (1) exist two possibilities of fragmentation by either concerted $\mathrm{C}-\mathrm{O}$ and $\mathrm{C}_{\beta}-\mathrm{C}_{\beta}$ or $\mathrm{C}-\mathrm{O}$ and $\mathrm{C}_{\alpha}-\mathrm{C}_{\beta}$ bond cleavages. Barriers calculated for these reactions are 3.55 and 4.40 eV , respectively. The same channels can be obtained by $\mathrm{C}_{\alpha}-\mathrm{C}_{\beta}$ or $\mathrm{C}_{\beta^{-}}$ $C_{\beta}$ bond cleavage of more stable structure 7 , however these mechanisms show higher energy barriers of 4.30 and 6.55 eV , respectively. Third possibility of fragmentation was found from structure 4 by either direct decomposition to $\mathrm{CO}+\mathrm{H}_{2} \mathrm{CCCH}_{2}$ or two-step hydrogen migration and $\mathrm{C}_{\alpha}-\mathrm{C}_{\beta}$ bond cleavage to $\mathrm{CO}+\mathrm{H}_{3} \mathrm{CCCH}$. As presented in Figure $5.5 \mathbf{b}$ ), fragmentation can also occur from cyclic isomer $\operatorname{cyc}(\mathrm{HC}=\mathrm{CH}-\mathrm{CH})-\mathrm{CHO}(13)$. Single bond cleavage, but higher barrier ( 5.51 eV ) was found to produce of $\mathrm{H}_{4} \mathrm{C}_{3}$ in a cyclic form (cyclopropene). Second cyclic isomer of $\mathrm{H}_{4} \mathrm{C}_{3}$ (cyclopropylidene) can be obtained by more steps, but presents lower energy barrier ( 4.52 eV ).


Figure 5.5 Potential Energy Surface for the skeleton fragmentation. Energies calculated at B3LYP/6$311++\mathrm{G}(3 \mathrm{df}, 2 \mathrm{p})$ level of theory are given in eV relative to furan. Zero point energy corrections are included.

TABLE 5.2 Comparison of ADMP and PES exploration results for the fragmentation process.

| Fragmentation channel | Total number <br> of trajectories | Energy of the <br> exit channel | Energy <br> barrier | Number <br> of TS |
| :--- | :--- | :--- | :--- | :--- |
| $\mathrm{HCCH}+\mathrm{H}_{2} \mathrm{CCO}$ | 198 | 1.89 | 3.55 | 2 |
| $\mathrm{CO}+\mathrm{H}_{2} \mathrm{CCCH}_{2}$ | 96 | 0.95 | 4.16 | $3 / 4$ |
| $\mathrm{CO}+\mathrm{H}_{3} \mathrm{CCCH}$ | 44 | 1.05 | 3.14 | 6 |
| $\mathrm{CO}+\mathrm{cyc}\left(\mathrm{HCCHCH}_{2}\right)$ | 35 | 2.09 | 5.51 | 2 |
| $\mathrm{CO}+\mathrm{cyc}\left(\mathrm{H}_{2} \mathrm{CCCH}_{2}\right)$ | - | 3.95 | 4.52 | 4 |

From the Table 5.2, summarizing results of the fragmentation process, it can clearly be seen that channel $\mathrm{HCCH}+\mathrm{H}_{2} \mathrm{CCO}$ presents the optimum combination of the second lowest energy barrier and only two steps of rearrangement required before decomposition. However, absolute abundance of channel $\mathrm{CO}+\mathrm{H}_{4} \mathrm{C}_{3}$ closely follows that of channel $\mathrm{HCCH}+\mathrm{H}_{2} \mathrm{CCO}$ with total occurrence of 175 . As discussed in the section of MD results, three isomeric forms of $\mathrm{H}_{4} \mathrm{C}_{3}$ have been distinguished. Their relative stability follows an adequate order as the one obtained by ADMP method and not the one determined by the exploration of reaction paths and energy barriers. It is worth pointing out that with enough internal energy to overcome the barriers, statistical distribution of products should prevail over the differences in energy barriers, meaning that MD should present more quantitatively reliable results.


Figure 5.6 Potential Energy Surface for the hydrogen loss. Energies calculated at B3LYP/6-311++G(3df,2p) level of theory are given in eV relative to furan. ZPE corrections are included.

As shown in Figure 5.6, energy barriers for hydrogen elimination from both positions are of equal height ( 5.07 eV ). Resulting $\alpha$-furyl and $\beta$-furyl structures ( 23 and 19) present practically unchanged geometry to that of furan. The maximum variation in geometrical parameters appeared after $\mathrm{H}_{\alpha}$ loss and led to decrease of $\mathrm{C}_{\alpha}-\mathrm{O}$ bond length by $0.03 \AA$ as well as decrease in $\mathrm{C}_{\alpha}-\mathrm{C}_{\beta}-\mathrm{C}_{\beta}$ angle and increase in $\mathrm{O}-\mathrm{C}_{\alpha}-\mathrm{C}_{\beta}$ angle by approx. $3^{\circ}$. The unpaired electron of these radicals occupies a $\pi$ type orbital. Further isomerization after H loss can either proceed
through cleavage of the $\mathrm{C}_{\alpha}(4)$ - O bond of the $\alpha$-furyl or $\mathrm{C}_{\alpha}(1)$-O of the $\beta$-furyl concerted with H transfer to the carbon from which hydrogen was previously eliminated, leading to structures 24 and 20. Then, subsequent isomerization from structure 20 by $2,1 \mathrm{H}$ transfer gives structure 21 and rotation of the dihedral angle $\mathrm{O}-\mathrm{C}_{\alpha}-\mathrm{C}_{\beta}-\mathrm{C}_{\beta}$ leads to structure 22.

Following H loss, two possible fragmentation channels: $\mathrm{H}+\mathrm{HCCH}+\mathrm{HCCO}$ and $\mathrm{H}+\mathrm{CO}$ $+\mathrm{H}_{2} \mathrm{CCCH}$ were found, latter being more stable. CO and $\mathrm{H}_{2} \mathrm{CCCH}$ can be obtained after both $\mathrm{H}_{\alpha}$ or $\mathrm{H}_{\beta}$ loss by either 1,2 hydrogen transfer of structure 24 or elongation of the $\mathrm{C}_{\alpha}(4)-\mathrm{C}_{\beta}(3)$ bond of structure 22. Energy barriers calculated for these mechanism are 8.03 eV and 7.79 eV , respectively. Break of the planar geometry of structure 20 by rotation around $\mathrm{C}_{\beta}-\mathrm{C}_{\beta}$ bond can lead to products HCCH and HCCO. Following $\mathrm{H}_{\beta}$ elimination first step of H migration was found to be rate determining. The system will, however, more probably relax to channel $\mathrm{H}+$ $\mathrm{HCCH}+\mathrm{HCCO}$.


Figure 5.7 Potential Energy Surface for the molecular hydrogen loss from two $\alpha$, two $\beta$ and opposite $\alpha$ and $\beta$ positions. Energies calculated at B3LYP/6-311++G(3df,2p) level of theory are given in eV relative to furan. ZPE corrections are included.

During exploration of Potential Energy Surface all possible positions of $\mathbf{H}_{2}$ loss have been studied. Figures 5.7 and 5.8 present pathways for this process. Although the energy barrier for emission of $\mathrm{H}_{2}$ from two $\beta$ positions is the lowest $(5.86 \mathrm{eV})$, such low occurrence of this channel in the dynamical simulations can be explained by deterring properties of the stable structure 7. Reaching the transition structure for the loss of two $\beta$ hydrogens from structure 7 would additionally require closing of the furan ring. Second and third lowest energy barriers were found for the loss of two adjacent hydrogens in $\alpha$ and $\beta$ positions. These pathways imply either production of $\beta$-carbene (2) and $\mathrm{H}_{2}$ loss from $\mathrm{C}_{\alpha}(4)$ or production of $\alpha$-carbene (1) and $\mathrm{H}_{2}$ loss from $\mathrm{C}_{\beta}(3)$, with barriers of 6.17 eV and 6.30 eV , respectively, both leading to structure 25. From there, subsequent ring opening gives structure 26. Common mechanism, exhibiting the highest energy barrier of 7.23 eV , was found for the elimination of $\mathrm{H}_{2}$ from opposite sides of the furan ring and two $\alpha$ positions giving structure 31. Further stabilization of the system can additionally occur after ring opening to structure 32.

Reaction pathways following $\mathrm{H}_{2}$ loss present a lower energy barrier than any channel of decomposition observed after H loss. The only three-body fragmentation followed by $\mathbf{H}_{2}$
loss observed in the dynamical simulation produced CO and $\mathrm{H}_{2} \mathrm{C}_{3}$. Consequently, this single process was investigated. The most energetically favorable fragmentation takes place after the elimination of two $\mathrm{H}_{\beta}$ with barrier of 6.39 eV , but as it was previously pointed out, such reaction can be stopped at stable structure 7 and requires succeeding ring formation. Thus, the most probable mechanism of fragmentation takes place after loss of adjacent hydrogens from $\alpha$ and $\beta$ positions due to low energy barrier ( 6.79 eV ) and few steps of rearrangement. Such conclusion is consistent with the ADMP results.


Figure 5.8 Potential Energy Surface for the molecular hydrogen loss from the adjacent $\alpha$ and $\beta$ positions. Energies calculated at B3LYP / $6-311++\mathrm{G}(3 \mathrm{df}, 2 \mathrm{p})$ level of theory are given in eV relative to furan.

### 5.1.3 Statistical method

A complementary information about the fragmentation process can be provided by the $\mathrm{M}_{3} \mathrm{C}$ methodology. The database of possible fragments included 226 isomers corresponding to 44 different chemical formulas. Their geometries are presented in Annex 1. The final parameters used to obtain the results discussed in this section are given in Table 5.3.

Table 5.3 Parameters of the $\mathrm{M}_{3} \mathrm{C}$ simulation of neutral furan

| System Radius | $13 \AA$ |
| :--- | :--- |
| Markov chain sequence | $\mathrm{V}, \mathrm{T}, \mathrm{R}, 5 \times \mathrm{S}: 0, \mathrm{~V}, \mathrm{~T}, \mathrm{R}, 5 \times \mathrm{S}: 1:-1$ |
| Number of experiments | 50 |
| Number of events | 800000 |
| Sampling method | RANDOM |



FIGURE 5.9 Results of $\mathrm{M}_{3} \mathrm{C}$ calculations of neutral furan: a) channels and b) species probabilities as a function of the internal energy.

Figure 5.9 presents results obtained with the $\mathrm{M}_{3} \mathrm{C}$ method, channels (panel a)) and species (panel b)) distributions as a function of the internal energy. The first channel that can be observed is $\mathrm{CO} / \mathrm{H}_{4} \mathrm{C}_{3}$. For the energy range between 1 and 4.5 eV , it is the only fragmentation channel with probability of $100 \%$. A second channel $\mathrm{H}_{2} \mathrm{C}_{2} / \mathrm{H}_{2} \mathrm{C}_{2} \mathrm{O}$ appears at 5 eV and reaches maximum probability of $30 \%$ at 6.5 eV . Both channels are dominant in the dynamical simulations at intermediate energies, but the $\mathrm{H}_{2} \mathrm{C}_{2} / \mathrm{H}_{2} \mathrm{C}_{2} \mathrm{O}$ presents higher total occurrence. No direct comparison of the probabilities for specific internal energies can be made due to each method's consideration of time. The ADMP method allows to investigate the very first steps of the fragmentation process and in the $\mathrm{M}_{3} \mathrm{C}$ complete redistribution of the excitation energy over all fragments is assumed in the infinite time limit. Hence, it can be expected that longer simulation times of ADMP calculations would lead to enhanced probability of the $\mathrm{CO} / \mathrm{H}_{4} \mathrm{C}_{3}$ channel. Figure 5.9 b) shows that the main fragment observed throughout all energies is CO. This species is a product of all but one presented fragmentation channels, which is coherent with the exploration of PES, showing that exit channels are more stable when CO is produced.

The first three-body channel to appear in the energy range was found to be $\mathrm{CO} / \mathrm{H}_{2} \mathrm{C}_{3} / \mathrm{H}_{2}$. It dominates since 6.5 until 11 eV with a maximum at 8.5 eV . Moreover, the fact that the total energy of products: $\mathrm{H}_{2} \mathrm{C}_{3}, \mathrm{CO}$ and $\mathrm{H}_{2}$ is lower than any channel of single H loss can explain minor significance of this process in two- and three-body fragmentation channels obtained by the $\mathrm{M}_{3} \mathrm{C}$ method. At higher energies also four- and five-body channels involving either atomic and molecular hydrogen loss can be noticed. The dominant ones are: $\mathrm{CO} / \mathrm{HC}_{3} / \mathrm{H}_{2} / \mathrm{H}$, $\mathrm{CO} / \mathrm{C}_{3} / \mathrm{H}_{2} / \mathrm{H}_{2}$, and $\mathrm{CO} / \mathrm{C}_{3} / \mathrm{H}_{2} / \mathrm{H} / \mathrm{H}$. These channels, although highly stable and entropically favorable, do not appear in the ADMP simulations since not enough energy is deposited into the system and time evolution is not enough to observe such mechanisms. They were also
not considered in our previous discussion of the PES since they present high-energy barriers (at least of 10 eV ).

### 5.1.4 Comparison with thermal decomposition experiments

Previously discussed importance of two-body fragmentation channels: $\mathrm{CO} / \mathrm{H}_{4} \mathrm{C}_{3}$ and $\mathrm{H}_{2} \mathrm{C}_{2} / \mathrm{H}_{2} \mathrm{C}_{2} \mathrm{O}$ is consistent with the experimental measurements of furan pyrolysis [22]-[25], [27], [29]-[32], [95], where it has been shown that these are the most observed unimolecular decomposition reactions. The most probable mechanisms of obtaining these products occur through the formation of highly reactive carbenes, as it was confirmed in this work. Multifragmentation processes have not been an objective of any experimental study. However, in a theoretical investigation by Sendt et al [28] it was proposed that H loss from propyne $\left(\mathrm{H}_{3} \mathrm{CCCH}\right)$ is a mechanism producing channel $\mathrm{CO} / \mathrm{H}_{3} \mathrm{C}_{3} / \mathrm{H}$. Propargyl radicals $\left(\mathrm{H}_{3} \mathrm{C}_{3}\right)$ were observed as a thermal decomposition products by Sorkhabi et al [27] and Vasiliou et al [29], where it was indicated that these species are direct products of furan decomposition. However, none of the methods applied in this work pointed out to such reaction. The $\mathrm{H}_{3} \mathrm{C}_{3}$ fragment is rather produced in channel $\mathrm{CO} / \mathrm{H}_{3} \mathrm{C}_{3} / \mathrm{H}$. Contrary to the conclusion of Sendt, the mechanism of producing this channel relies on H loss taking place directly from furan rather than from propyne. Moreover, present results show that $\mathrm{H}_{2}$ loss and subsequent fragmentation to CO and $\mathrm{H}_{2} \mathrm{C}_{3}$ should be a highly observed three-body fragmentation channel for higher energies applied into the system.

### 5.2 Singly ionized furan

### 5.2.1 Molecular Dynamics

Results of the dynamical simulations of singly ionized furan are presented in Figures 5.10-5.14. As in the case of the neutral molecule, four types of processes can be distinguished. The amount of internal energy required to observe them is shifted to lower values in comparison with the neutral furan. As it is shown in Figure 5.10 a), furan cation remains intact until the energy of 8 eV . Since then, the first isomerization takes place and can be ultimately observed at the energy of 25 eV . Skeleton fragmentation occurs for all energies starting from 9 eV and dominates for the energy range between 16 and 20 eV . Next, $\mathrm{H} / \mathrm{H}_{2}$ loss followed by isomerization starts at 13 eV . The major process since 20 eV was found to be $\mathrm{H} / \mathrm{H}_{2}$ loss followed by fragmentation. Figure $5.10 \mathbf{b}$ ) presents number of fragments produced at different internal energies. It can be noticed that two body fragmentation dominates for midrange energies from 16 to 21 eV and three body fragmentation is the most abundant for higher energies between 22 and 28 eV . Decomposition to four fragments starts at 19 eV and is the most frequent at 29 eV . Finally, the calculations show that five body fragmentation is a minor process with maximum occurrence of $7 \%$ at 30 eV .


FIGURE 5.10 Results of the ADMP simulations of singly ionized furan: total occurrence of a) observed processes b) number of fragments as a function of the internal energy.


FIGURE 5.11 Results of the ADMP simulations of singly ionized furan: a) total occurrence of isomerization channels b) snapshots of trajectories leading to channels from the left panel.

Starting with the isomerization process, only three distinctive structures were found at the final step of the simulations. The panel a) of Figure 5.11 shows their abundances and panel b) exemplifies their evolution in time. The first isomerization channel corresponds to $2,1 \mathrm{H}$ transfer to form $\mathrm{H}_{2} \mathrm{C}=\mathrm{C}=\mathrm{CH}-\mathrm{CHO}^{+}$( 145 trajectories in total). The second most populated channel, with 43 trajectories overall, implies opening of the furan ring and break of the planar symmetry of the molecule without any hydrogen transfer. Lastly, hydrogen migration to the oxygen atom was observed 36 times. The panel a) of Figure 5.11 shows distinct prevalence of $2,1 \mathrm{H}$ migration until the energy of 21 eV , when hydrogen transfer to oxygen becomes more abundant.


FIGURE 5.12 Results of the ADMP simulations of singly ionized furan: a) total occurrence of fragmentation channels b) snapshots of trajectories leading to channels from the left panel. Only channels that appeared at least $5 \%$ at a certain point in the energy range are presented.

Compared to the neutral molecule, dynamical simulations of singly ionized furan produced more variations of skeleton fragmentation, as four major channels were found: $\mathrm{H}_{3} \mathrm{C}_{3}^{+} / \mathrm{HCO}$, $\mathrm{HCO}^{+} / \mathrm{H}_{3} \mathrm{C}_{3}, \mathrm{H}_{4} \mathrm{C}_{3}^{+} / \mathrm{CO}$ and $\mathrm{H}_{2} \mathrm{C}_{2} \mathrm{O}^{+} / \mathrm{H}_{2} \mathrm{C}_{2}$, listing from the most to the least populated. The panel b) of Figure 5.12 shows that the first and the most abundant fragmentation mechanism does not impose hydrogen migration, but follows ring opening and later cyclization of three carbon atoms, producing cyclopropenium cation $\mathrm{c}-\mathrm{H}_{3} \mathrm{C}_{3}^{+}$. The second most populated channel produces the same species, but charge is located on the $\mathrm{HCO}^{+}$fragment and $\mathrm{H}_{3} \mathrm{C}_{3}$ is formed in a linear configuration. In this mechanism, $2,3 \mathrm{H}$ transfer takes place as a first step, followed by $\mathrm{C}-\mathrm{O}$ and $\mathrm{C}_{\alpha}-\mathrm{C}_{\beta}$ bond cleavages. In the third channel of skeleton fragmentation, species $\mathrm{H}_{4} \mathrm{C}_{3}^{+}$can be obtained in four possible isomers. To find out which configuration of $\mathrm{H}_{4} \mathrm{C}_{3}^{+}$is the most abundant, 98 trajectories producing channel $\mathrm{H}_{4} \mathrm{C}_{3}^{+}+\mathrm{CO}$ were examined. The total occurrence of mentioned species was found to be: allene $\left(\mathrm{H}_{2} \mathrm{CCCH}_{2}^{+}\right)-59$ trajectories, cyclopropene $\left(\mathrm{c}-\mathrm{H}_{2} \mathrm{CCHCH}^{+}\right)-28$ trajectories, vinylmethylene $\left(\mathrm{H}_{2} \mathrm{CCHCH}^{+}\right)-6$ trajectories and propyne $\left(\mathrm{H}_{3} \mathrm{CCCH}^{+}\right)$- 5 trajectories. Lastly, production of $\mathrm{H}_{2} \mathrm{C}_{2} \mathrm{O}^{+}$and $\mathrm{H}_{2} \mathrm{C}_{2}$ proceeds through ring opening, $1,2 \mathrm{H}$ transfer and $\mathrm{C}_{\beta}-\mathrm{C}_{\beta}$ bond cleavage. From panel a) of Figure 5.12 it can be noticed that channel $\mathrm{H}_{3} \mathrm{C}_{3}^{+} / \mathrm{HCO}$, besides being the most abundant among skeleton fragmentation, is also the first to appear in the energy range. Channels $\mathrm{HCO}^{+} / \mathrm{H}_{3} \mathrm{C}_{3}$ and $\mathrm{H}_{4} \mathrm{C}_{3}^{+} / \mathrm{CO}$ present similar character, but maximum value of producing $\mathrm{H}_{4} \mathrm{C}_{3}^{+}$is shifted by 1 eV to higher energies.


FIGURE 5.13 Results of the ADMP simulations of singly ionized furan: a) total occurrence of H loss channels $\mathbf{b}$ ) snapshots of trajectories leading to channels from the left panel. Only channels that appeared at least $5 \%$ at a certain point in the energy range are presented.

Third process that can be observed is $\mathbf{H}$ loss. Firstly, ejection of the hydrogen atom can be followed by isomerization. Position of the eliminated hydrogen(s) was again subject of the statistical analysis. It was found that $\mathrm{H}_{\alpha}$ was lost in $56 \%$ of the considered trajectories giving H and $\mathrm{H}_{3} \mathrm{C}_{4} \mathrm{O}^{+}$. As it can be seen in panel a) of Figure 5.13, this channel is dominant until the energy of 20 eV . Since then, decomposition of the remaining fragment after H loss starts to


FIGURE 5.14 Average time scales of sequential events leading to a) $\mathrm{H}_{3} \mathrm{C}_{3}^{+} / \mathrm{CO} / \mathrm{H}$ and $\left.\mathbf{b}\right) \mathrm{H}_{2} \mathrm{C}_{3}^{+} / \mathrm{CO} / \mathrm{H} / \mathrm{H}$. Borders of bars represent when, for different energies, on average either H loss or fragmentation take place. Inset plots show abundance of different processes.
prevail. First panel of Figure 5.13 c) shows the most abundant mechanism leading to production of fragments $\mathrm{H}_{3} \mathrm{C}_{3}^{+}, \mathrm{CO}$ and H by $\mathrm{H}_{\alpha}$ loss and subsequent ring rupture. This mechanism relies on H loss from $\alpha$ position in substantial majority of trajectories ( $82 \%$ ). As shown in Figure 5.13 a), $\mathrm{H}_{3} \mathrm{C}_{3}^{+} / \mathrm{CO} / \mathrm{H}$ is the most abundant channel for the middle energy range ( $20-$ 25 eV ). The sequence of events ( H loss $\rightarrow$ fragmentation or fragmentation $\rightarrow \mathrm{H}$ loss) has been studied in order to recognize the most probable mechanism. From Figure 5.14 a) it can be seen that hydrogen atom is mainly ejected from $\mathrm{H}_{4} \mathrm{C}_{4} \mathrm{O}^{+}$and not from the previously fragmented species. Moreover, the width of blue bars, representing the average time the system requires to decompose after initial H loss, decreases with increasing energy. Fragmentation before H loss was a minor process with only 25 occurrences in total (in comparison with 272 for H loss $\rightarrow$ fragmentation). However, if the fragmentation occurred as a first step, the intermediate channel was mainly found to be $\mathrm{H}_{3} \mathrm{C}_{3}^{+} / \mathrm{HCO}$ ( 17 trajectories) and the least frequent was $\mathrm{H}_{4} \mathrm{C}_{3}^{+} / \mathrm{CO}$ (8 trajectories).

The final major process was found to be the $\mathbf{H}_{2} / \mathbf{2 H}$ loss. As shown in panel a) of Figure 5.15, the elimination of two hydrogen atoms appears first at the energy of 16 eV and slowly increases until reaching maximum probability of $12 \%$ for the energy of 27 eV . The frequency of 2 H loss in a decreasing order is: adjacent $\mathrm{H}_{\alpha}$ and $\mathrm{H}_{\beta}(34 \%)>$ opposite $\mathrm{H}_{\alpha}$ and $\mathrm{H}_{\beta}(33 \%)>$ two $\mathrm{H}_{\alpha}(26 \%)>$ two $\mathrm{H}_{\beta}(7 \%)$. Subsequently, the $\mathbf{H}_{2} / 2 \mathbf{H}$ loss followed by fragmentation can be observed. This mechanism is complex and a lot of different channels of this character were found. However, one channel of the highest importance can be clearly distinguished. The first panel of Figure 5.15 b) shows the most abundant mechanism of obtaining fragments $\mathrm{H}_{2} \mathrm{C}_{3}^{+}$, CO and 2 H by opposite $\mathrm{H}_{\alpha}$ and $\mathrm{H}_{\beta}$ loss and subsequent $\mathrm{C}_{\alpha}-\mathrm{C}_{\beta}$ bond cleavage. The frequency of 2 H loss in this channel in a decreasing order is: opposite $\mathrm{H}_{\alpha}$ and $\mathrm{H}_{\beta}(44 \%)>$ two $\mathrm{H}_{\alpha}(27 \%)$ $>$ adjacent $\mathrm{H}_{\alpha}$ and $\mathrm{H}_{\beta}(25 \%)$ > two $\mathrm{H}_{\beta}(4 \%)$. Panel a) of Figure 5.15 shows that production of $\mathrm{H}_{2} \mathrm{C}_{3}^{+}$, CO and 2 H is the most numerous for the highest considered energies ( $26-30 \mathrm{eV}$ ). Again, time scale of this process and its transitional steps, presented in Figure 5.14 b), can help to elucidate actual production mechanism of this channel. It can be seen that sequence of


FIGURE 5.15 Results of the ADMP simulations of singly ionized furan: a) total occurrence of $\mathrm{H}_{2} / 2 \mathrm{H}$ loss channels b) snapshots of trajectories leading to channels from the left panel. Only channels that appeared at least $5 \%$ at a certain point in the energy range are presented.
events producing channel $\mathrm{H}_{2} \mathrm{C}_{3}^{+} / \mathrm{CO} / \mathrm{H} / \mathrm{H}$ is mainly $1^{\text {st }} \mathrm{H}$ loss $\rightarrow 2^{\text {nd }} \mathrm{H}$ loss $\rightarrow$ fragmentation although on average it takes more time for this channel to be produced. Decomposition to this channel always starts with ejection of the first hydrogen in the time interval between 10 and 50 fs . Subsequently, in most cases second hydrogen is eliminated and the remaining structure breaks. Conversely, when fragmentation takes place right after the first H loss intermediate channels of $\mathrm{H}_{3} \mathrm{C}_{3}^{+} / \mathrm{CO} / \mathrm{H}$ (21 trajectories) or $\mathrm{H}_{2} \mathrm{C}_{3}^{+} / \mathrm{HCO} / \mathrm{H}$ (19 trajectories) are produced. Less populated channels of discussed type never exceed the total occurrence of $10 \%$, so their contribution to the fragmentation process of singly ionized furan are minor.

### 5.2.2 Potential Energy Surface

Further understanding of the fragmentation process is provided by the exploration of the Potential Energy Surface. Scheme 5.16 shows all calculated fragmentation pathways of furan cation and clarifies steps of obtaining three and four body fragmentation channels. Obtained energy profiles, presenting minima and transition structures optimized at B3LYP/6$311++G(d, p)$ level of theory, are presented in Figures 5.17-5.21. For the reasons of clarity and further comparison with the experimental results, exploration of PES of singly ionized furan is divided into sections, investigating production of specific species.


FIGURE 5.16 Calculated fragmentation pathways corresponding to channels obtained by Molecular Dynamics.


Figure 5.17 Potential Energy Surface for production of $\mathrm{H}_{4} \mathrm{C}_{3}^{+}$. Energies calculated at B3LYP/6-311++G(d,p) level of theory are given in eV relative to furan. ZPE corrections are included. Panel a) shows fragmentation occurring directly from furan. Dashed lines indicate barrierless processes. Panel b) shows possible isomerization pathways of $\mathrm{H}_{4} \mathrm{C}_{3}^{+}$. Dashed line indicate that only the transition structure of the highest energy is presented.

The formation of the $\mathrm{H}_{4} \mathrm{C}_{3}^{+}$ion has been explored with consideration of four possible structures for this species, previously mentioned in the MD results. Resulting Potential Energy Surface is presented in panel a) of Figure 5.17. The lowest energy barrier, equal to 11.52 eV , has been found for production of allene $\left(\mathrm{H}_{2} \mathrm{CCCH}_{2}^{+}\right)$by consecutive $2,1 \mathrm{H}$ transfer, ring opening, rotation around $\mathrm{C}_{\alpha}-\mathrm{C}_{\beta}$ bond and $1,2 \mathrm{H}$ transfer concerted with $\mathrm{C}_{\alpha}-\mathrm{C}_{\beta}$ bond cleavage (ts1 $\rightarrow \mathbf{t s} \mathbf{2} \rightarrow \mathbf{t s} \mathbf{3} \rightarrow \mathbf{t s} \mathbf{4}$ ). A different pathway results in production of propyne $\left(\mathrm{H}_{3} \mathrm{CCCH}^{+}\right)$, with energy barrier of 11.69 eV , when $1,4 \mathrm{H}$ transfer (ts5) occurs instead of ts4. Fragmentation to allene through barrier higher than ts $\mathbf{1}$ only by $0.04 \mathrm{eV}(11.56 \mathrm{eV}-\mathrm{ts} 6)$ can also take place when sequence of hydrogen migration is reversed, i.e. when $1,2 \mathrm{H}$ transfer, ring opening, $2,1 \mathrm{H}$ transfer and $\mathrm{C}_{\alpha}-\mathrm{C}_{\beta}$ bond cleavage (ts6 $\rightarrow \mathbf{t s} 7 \rightarrow \mathbf{t s} 8 \rightarrow \mathbf{t s} 9$ ) occur in succession. If ring opening is concerted with $1,2 \mathrm{H}$ transfer as a first step of this reaction, then the transition structure (ts10) is located at higher energy of 12.22 eV . Production of vinylmethylene $\left(\mathrm{H}_{2} \mathrm{CCHCH}^{+}\right)$is possible when a barrierless $\mathrm{C}_{\alpha}-\mathrm{C}_{\beta}$ bond fission takes place from $\min 7$. No pathway was found to produce cyclopropene ( $\mathrm{c}-\mathrm{H}_{2} \mathrm{CCHCH}^{+}$) directly from furan cation. However, if $\mathrm{H}_{4} \mathrm{C}_{3}^{+}$species posses enough internal energy, they can interconvert after primary fragmentation. The isomerization of $\mathrm{H}_{4} \mathrm{C}_{3}^{+}$is presented in the panel $\mathbf{b}$ ) of Figure 5.17. It can be seen that vinylmethylene and cyclopropene might be sequentially obtained from allene through energy barriers of 11.73 and 11.59 eV , respectively. Consequently, cyclopropene ion can also be a product of furan cation fragmentation. On the other hand, isomerization from allene to propyne presents higher energy barrier $(12.10 \mathrm{eV})$ than for direct fragmentation to propyne from furan cation $(11.69 \mathrm{eV})$, which can be another reason for such low observation of this isomer in the MD simulations.


Figure 5.18 Potential Energy Surface for production of $\mathrm{H}_{3} \mathrm{C}_{3}^{+}$. Energies calculated at B3LYP/6-311++G(d,p) level of theory are given in eV relative to furan. ZPE corrections are included. Dashed line indicate barrierless transitions.

Possible ways of obtaining the $\mathrm{H}_{3} \mathrm{C}_{3}^{+}$ion are presented in Figure 5.18. The cyclic isomer of $\mathrm{H}_{3} \mathrm{C}_{3}^{+}$- cyclopropenium cation $\left(\mathrm{c}-\mathrm{H}_{3} \mathrm{C}_{3}^{+}\right)$- requires the least amount of rearrangement to be produced. No hydrogen transfer is needed to obtain channel c- $\mathrm{H}_{3} \mathrm{C}_{3}^{+} / \mathrm{HCO}$, only furan ring opening through a transition structure located at 11.78 eV (ts11). The mechanism follows a few steps, as fragmentation proceeds through formation of an ion-molecule complex in which the $\mathrm{C}_{\alpha} \cdots \mathrm{C}_{\beta}$ distance is equal to $1.68 \AA(\min 9)$. The $\mathrm{H}_{3} \mathrm{C}_{3}^{+}$ion can also be produced through channels involving H loss. As it was previously stated in the discussion of the MD results, the mechanism of producing channel $\mathrm{H}_{3} \mathrm{C}_{3}^{+} / \mathrm{CO} / \mathrm{H}$ is based mainly on H loss $\rightarrow$ fragmentation sequence of events. Production of $\mathrm{H}_{3} \mathrm{C}_{3}^{+}$through H loss exhibits higher energy barriers than the one for skeleton fragmentation, but the dynamical simulations show prevalence of this process for middle energies. $\mathrm{H}_{\alpha}$ can be ejected directly from furan cation or from an isomer of furan cation. The least amount of energy ( $\mathbf{t s 1 2}-12.44 \mathrm{eV}$ ) is required to eliminate hydrogen from min9. Subsequent $\mathrm{C}_{\alpha}-\mathrm{C}_{\beta}$ bond cleavage proceeds through the lowest energy barrier for formation of channel c- $\mathrm{H}_{3} \mathrm{C}_{3}^{+} / \mathrm{CO} / \mathrm{H}$, located at 12.91 eV . Barriers for $\mathrm{H}_{\alpha}$ and $\mathrm{H}_{\beta}$ elimination directly from furan cation were calculated to be 14.60 and 14.71 eV , respectively. Lower barrier for elimination of hydrogen from $\alpha$ position, resulting in production of $\alpha$-furyl cation (min10), is consistent with majority of $\mathrm{H}_{\alpha}$ loss observed in the MD calculations. Only one transition structure ( $\mathbf{t s 1 3}-16.28 \mathrm{eV}$ ) is required to obtain fragmentation channel c- $\mathrm{H}_{3} \mathrm{C}_{3}^{+} / \mathrm{CO} / \mathrm{H}$ from $\min 10$. Although production of $\mathrm{c}-\mathrm{H}_{3} \mathrm{C}_{3}^{+}$from $\beta$-furyl cation (min12) presents a lower reaction barrier (ts15-16.00 eV), this mechanism is less probable because of several steps of isomerization are required to reach fragmentation. A linear configuration of $\mathrm{H}_{3} \mathrm{C}_{3}^{+}$- a propargyl cation $\left(\mathrm{H}_{2} \mathrm{CCCH}^{+}\right)$- might be formed in two steps after concerted C-O bond fission and $2,1 \mathrm{H}$ transfer of $\alpha$-furyl cation (ts14-14.99 eV) and consecutive, barrierless $\mathrm{C}_{\alpha}-\mathrm{C}_{\beta}$ bond cleavage of min11. This mechanism leads to the most energetically favourable pathway of obtaining $\mathrm{H}_{2} \mathrm{CCCH}^{+}$ ion. This isomer can be also obtained after $\mathrm{H}_{\beta}$ elimination through two different mechanisms, but their energy barriers are higher ( 16.81 or 15.56 eV ) than the one calculated for fragmentation of $\alpha$-furyl cation ( 14.99 eV ).

The fragmentation pathways leading to formation of $\mathrm{H}_{2} \mathrm{C}_{3}^{+}$ion are presented in Figure 5.19. This species can be produced in two isomeric forms: cyclic or linear, former being more stable by 0.09 eV . Two-body fragmentation implies the energy barrier of 13.43 eV and the series of $2,1 \mathrm{H}$ transfer, $2,3 \mathrm{H}$ transfer $\mathrm{C}_{\alpha}-\mathrm{C}_{\beta}$ bond cleavage and finally barrierless C-O bond fission ( $\mathbf{t s} \mathbf{1} \rightarrow \mathbf{t s} \mathbf{2 4} \rightarrow \mathbf{t s} \mathbf{2 5}$ ). This mechanism is unlikely to occur because of as many as four steps and after reaching $\min 2$ the system is expected to follow reaction path of $\mathrm{H}_{4} \mathrm{C}_{3}^{+} / \mathrm{CO}$. Next, the energy barrier of 15.99 eV was calculated for $\mathrm{H}_{2}$ loss from min2. Depending on which $\mathrm{C}-\mathrm{O}$ bond cleaves, either $\min 23$ or very stable $\min 22$ are obtained. From $\min 23$ a c- $\mathrm{H}_{2} \mathrm{C}_{3}^{+}$ion is produced by $\mathrm{C}_{\alpha}-\mathrm{C}_{\beta}$ bond fission. Fragmentation to $\mathrm{HCCCH}^{+}$proceeds without barrier from min22. A cyclic isomer of $\mathrm{H}_{2} \mathrm{C}_{3}^{+}$can be also formed from $\min 22$ by $\mathrm{C}_{\alpha}-\mathrm{C}_{\beta}$ bond cleavage. The first step of obtaining channel $\mathrm{H}_{2} \mathrm{C}_{3}^{+} / \mathrm{CO} / \mathrm{H}_{2}(\mathbf{t s 2 6})$ is common for production of both $\mathrm{H}_{2} \mathrm{C}_{3}^{+}$isomers. Stability of $\min 22$ indicate which species will be more populated. From this structure the lowest energy path leads to linear isomer of $\mathrm{H}_{2} \mathrm{C}_{3}^{+}$. A channel that presents significant occurrence for the highest considered energies of the dynamical simulation was four-body fragmentation channel: $\mathrm{H}_{2} \mathrm{C}_{3}^{+} / \mathrm{CO} / 2 \mathrm{H}$. Previous analysis of the MD results specified the preferable sequence


FIGURE 5.19 Potential Energy Surface for production of $\mathrm{H}_{2} \mathrm{C}_{3}^{+}$. Energies calculated at B3LYP/6-311++G(d,p) level of theory are given in eV relative to furan. ZPE corrections are included. Panel a) shows two- and three-body fragmentation channels. Panel b) shows four-body fragmentation channels. Dashed lines indicate barrierless transitions.
of events to be: $1^{\text {st }} \mathrm{H}$ loss $\rightarrow 2^{\text {nd }} \mathrm{H}$ loss $\rightarrow$ fragmentation. Reaction pathways following this scheme are depicted in panel b) of Figure 5.19. It can be seen that, as expected, the least amount of energy is required to emit hydrogens first from $\min 9\left(\mathrm{H}_{\alpha}\right)$ and then from $\min 15\left(\mathrm{H}_{\beta}\right)$ rather than directly from furan cation. If $\mathrm{H}_{\beta}$ is emitted first from $\min 9$ the system proceeds through higher energy barrier with a transition structure at 19.39 eV (ts39). Elimination of hydrogens
from furan cation and later from furyl cations proceeds without barriers. The position of emitted hydrogens influences the stability of obtained structures. The least energy is required to eliminate two hydrogens from $\beta$ position ( $\min 24-19.03 \mathrm{eV}$ ). Subsequent C-O bond fission and concerted $\mathrm{C}_{\alpha}-\mathrm{C}_{\beta}$ bond cleavage with $1,2 \mathrm{H}$ transfer lead to channel $\mathrm{HCCCH}^{+} / \mathrm{CO} / 2 \mathrm{H}$. Next lowest isomer of $\mathrm{H}_{2} \mathrm{C}_{4} \mathrm{O}^{+}$was obtained after opposite $\mathrm{H}_{\alpha}$ and $\mathrm{H}_{\beta} \operatorname{loss}$ ( $\boldsymbol{\operatorname { m i n } 2 6 - 1 9 . 2 4 \mathrm { eV } \text { ). From }}$ there, by ring opening and H transfer, both isomers of $\mathrm{H}_{2} \mathrm{C}_{3}^{+}$can be produced. Emission of two hydrogens from two $\alpha$ positions ( $\min 28-19.29 \mathrm{eV}$ ) gave the third lowest geometry of $\mathrm{H}_{2} \mathrm{C}_{4} \mathrm{O}^{+}$. Consecutive ring opening leads to fragmentation through a barrier of 19.81 eV . The least stable isomer of $\mathrm{H}_{2} \mathrm{C}_{4} \mathrm{O}^{+}$was found after loss of adjacent $\mathrm{H}_{\alpha}$ and $\mathrm{H}_{\beta}$ ( $\min 30-19.32 \mathrm{eV}$ ). The ring opening of $\min 30$ implies 20.04 eV of energy for decomposition to $\mathrm{c}-\mathrm{H}_{2} \mathrm{C}_{3}^{+} / \mathrm{CO} / 2 \mathrm{H}$. The preferable position of emitted hydrogens concluded from dynamical simulations was found to be opposite $\mathrm{H}_{\alpha}$ and $\mathrm{H}_{\beta}$. This observation together with the lowest calculated reaction pathway indicate $\mathbf{t s} \mathbf{1 1} \rightarrow \boldsymbol{\operatorname { m i n }} \mathbf{9} \rightarrow \boldsymbol{t s} \mathbf{1 2} \rightarrow \boldsymbol{\operatorname { m i n }} \mathbf{1 5} \rightarrow \boldsymbol{\operatorname { m i n }} \mathbf{2 7}$ to be the most probable mechanism of producing $\mathrm{H}_{2} \mathrm{C}_{3}^{+}$ions through a four-body fragmentation. Moreover, energy barrier for channel involving loss of molecular hydrogen is lower than for loss of two single hydrogen atoms. However, the reason for such low occurrence of this channel in the MD might be difficult spatial distribution for forming ts26.


FIGURE 5.20 Potential Energy Surface for production of $\mathrm{HC}_{3}^{+}$. Energies calculated at B3LYP/6-311++G(d,p) level of theory are given in eV relative to furan. ZPE corrections are included. Dashed lines indicate barrierless transitions.

The only channel observed in the dynamical simulations producing ion $\mathrm{HC}_{3}^{+}$was found to be four body fragmentation to $\mathrm{HC}_{3}^{+} / \mathrm{CO} / \mathrm{H} / \mathrm{H}_{2}$. Figure 5.20 presents two calculated reaction pathways leading to formation of $\mathrm{HC}_{3}^{+}$. As concluded from the MD, with comparable probability the sequence of events of producing this channel can either be H loss $\rightarrow \mathrm{H}_{2}$ loss $\rightarrow$ fragmentation or $\mathrm{H}_{2}$ loss $\rightarrow \mathrm{H}$ loss $\rightarrow$ fragmentation. This channel was observed only in 31 trajectories of the dynamical simulations, so exploration of Potential Energy Surface is vital for identifying the most probable mechanism. The lowest energy pathway was found to start
with H loss from $\min 9$ as a first step. Further hydrogen migration produces min33, from which a transition structure for $\mathrm{H}_{2}$ elimination was calculated at 17.15 eV . Cleavage of $\mathrm{C}_{\alpha}-\mathrm{C}_{\beta}$ bond leads to the highest transition structure for this mechanism located at 17.54 eV . As previously mentioned in the section of fragmentation to $\mathrm{H}_{2} \mathrm{C}_{3}^{+}$, hydrogen molecule can be ejected after previous isomerization to min2. Subsequent barrierless H loss from min21 produces unstable min35, which under ring opening and $\mathrm{C}_{\alpha}-\mathrm{C}_{\beta}$ bond fission leads to the fragmentation through an energy barrier of 19.89 eV . Therefore, most probable mechanism of obtaining ion $\mathrm{HC}_{3}^{+}$proceeds through H loss, followed by $\mathrm{H}_{2}$ loss and finally fragmentation of the $\mathrm{HC}_{4} \mathrm{O}^{+}$ion.


FIGURE 5.21 Potential Energy Surface for production of $\mathrm{HCO}^{+}, \mathrm{H}_{2} \mathrm{C}_{2} \mathrm{O}^{+}$and $\mathrm{H}_{2} \mathrm{C}^{+}$. Energies calculated at B3LYP/6-311++G(d,p) level of theory are given in eV relative to furan. ZPE corrections are included. Dashed lines indicate barrierless transitions or that only the transition structure of the highest energy is presented.

Potential Energy Surface producing remaining significant ions are presented in Figure 5.21. A species that can only be obtained by skeleton fragmentation was found to be ketene cation $\left(\mathrm{H}_{2} \mathrm{C}_{2} \mathrm{O}^{+}\right)$. Mechanism of decomposition to $\mathrm{H}_{2} \mathrm{C}_{2} \mathrm{O}^{+}$proceeds through 1,2 hydrogen transfer and concerted fission of $\mathrm{C}-\mathrm{O}$ and $\mathrm{C}_{\beta}-\mathrm{C}_{\beta}$ bonds. The calculated energy barrier was located at 12.03 eV (ts48). A fragment that was not observed in the dynamical simulations, but was identified by previous experimental studies [2], [11], [39] is methylene ion $\left(\mathrm{H}_{2} \mathrm{C}^{+}\right)$. Possible mechanisms of producing $\mathrm{H}_{2} \mathrm{C}^{+}$involve further decomposition of ketene cation, requiring 13.72 eV of energy or decomposition of allene cation, leading to higher energy barrier for production of $\mathrm{H}_{2} \mathrm{C}^{+}$located at 17.50 eV . The last identified species, highly observed in the dynamical simulations coming from two- and three-body fragmentation channels, is formyl cation $\left(\mathrm{HCO}^{+}\right)$. Firstly, $2,3 \mathrm{H}$ transfer and consecutive ring rupture lead to formation of $\mathrm{HCO}^{+}$and propargyl radical as a neutral species. The highest transition structure for this mechanism was located at 12.78 eV (ts46). Formyl cation might as well be produced after H loss from min9 and subsequent $\mathrm{C}_{\alpha}-\mathrm{C}_{\beta}$ bond cleavage of min14. This three-body fragmentation channel requires 16.21 eV of deposited energy to occur.

To summarize, possible furan cation fragmentation pathways to nine charged species have been proposed. Exploration of PES enabled identification of the most probable decomposition mechanisms. Based on the obtained fragmentation pathways, the most abundant charged fragment is expected to be $\mathrm{H}_{3} \mathrm{C}_{3}^{+}$due to low energy barriers, a simple production mechanism and numerous plausible channels forming this species. The $\mathrm{H}_{4} \mathrm{C}_{3}^{+}$fragment is expected to be produced mostly in the allene isomeric form. For higher energies, a $\mathrm{H}_{2} \mathrm{C}_{3}^{+}$ion can be produced as a results of four-body fragmentation involving elimination of two atomic hydrogens. Loss of hydrogen was found to be an important process. Interestingly, hydrogen elimination occurs from the $\mathrm{H}_{4} \mathrm{C}_{4} \mathrm{O}^{+}$molecule rather than from the already fragmented species.

### 5.2.3 Statistical method

More insight into the fragmentation of the furan cation can be provided by the Microcanonical Metropolis Monte Carlo method. The database of neutral fragments used for the $\mathrm{M}_{3} \mathrm{C}$ calculations of the neutral furan consisted of 226 neutral isomers. In order to perform the $\mathrm{M}_{3} \mathrm{C}$ calculation of the furan cation, 243 singly ionized isomers have been added to the data set. Appendix 1 presents their geometries. A different sampling method, named SEQUENTIAL, has been applied in the case of the ionized molecule. Again, detailed benchmark of the input parameters have been performed (Chapter 4.3.2 Convergence search). Table 5.4 summarizes the final parameters used to obtain results presented in Figures 5.22-5.27.

Table 5.4 Parameters of the $\mathrm{M}_{3} \mathrm{C}$ simulation of singly ionized furan

| System Radius | $13 \AA$ |
| :--- | :--- |
| Markov chain sequence | $\mathrm{V}, \mathrm{T}, \mathrm{R}, 5 \times \mathrm{S}: 0, \mathrm{~V}, \mathrm{~T}, \mathrm{R}, 5 \times \mathrm{S}: 1:-1$ |
| Number of experiments | 500 |
| Number of events | 200000 |
| Sampling method | SEQUENTIAL |

As it can be seen in Figure 5.22, using SEQUENTIAL sampling method results in more channels being observed in comparison with the fragmentation of neutral molecule. Decomposition of the singly ionized furan starts with channel $\mathrm{H}_{4} \mathrm{C}_{3}^{+} / \mathrm{CO}$ at 2 eV of internal energy. Next channels to appear are $\mathrm{H}_{2} / \mathrm{H}_{2} \mathrm{C}_{4} \mathrm{O}^{+}, \mathrm{H} / \mathrm{H}_{3} \mathrm{C}_{4} \mathrm{O}^{+}$and, the least populated among two body fragmentation, $\mathrm{H}_{3} \mathrm{C}_{3}^{+} / \mathrm{HCO}$. An internal energy increase to middle and high values results in production of many channels of the same type as observed in the dynamical simulations, such as $\mathrm{H}_{3} \mathrm{C}_{3}^{+} / \mathrm{CO} / \mathrm{H}, \mathrm{H}_{2} \mathrm{C}_{3}^{+} / \mathrm{CO} / \mathrm{H}_{2}, \mathrm{HC}_{3}^{+} / \mathrm{CO} / \mathrm{H} / \mathrm{H}_{2}$ as well as unobserved channels like $\mathrm{HCO}^{+} / \mathrm{C}_{3} / \mathrm{H} / \mathrm{H}_{2}$ and $\mathrm{H}_{2} \mathrm{C}_{2}^{+} / \mathrm{HC} / \mathrm{CO} / \mathrm{H} / \mathrm{H}$. Panel b) of Figure 5.22 shows that production of $\mathrm{H}_{4} \mathrm{C}_{3}^{+}$dominates until the energy of 3.5 eV , when $\mathrm{H}_{3} \mathrm{C}_{3}^{+}$begins to be the most abundant up to 10.5 eV . Error bars, corresponding to standard deviation of mean probabilities over all experiments, present values of around $15 \%$ for channels and $10 \%$ for species distributions. Among two-body fragmentation production of $\mathrm{H}_{4} \mathrm{C}_{3}^{+}$was found to be the most probable. Species $\mathrm{H}_{3} \mathrm{C}_{3}^{+}$ dominate as a product of three-body decomposition channels and $\mathrm{HC}_{3}^{+}$is the most abundant fragment in the four-body fragmentation.


FIGURE 5.22 Results of $\mathrm{M}_{3} \mathrm{C}$ calculations of singly ionized furan: $\mathbf{a}$ ) channels and $\mathbf{b}$ ) charged species probabilities as a function of the internal energy. Error bars correspond to standard deviations of the probabilities averaged over all experiments. Only channels/species with probabilities larger than $10 \%$ are shown.


FIGURE 5.23 Comparison of significant species probabilities calculated by ADMP method (red) and $\mathrm{M}_{3} \mathrm{C}$ (blue). Grey areas cover the energy range until the value of the lowest energy barrier for each fragment.
$\mathrm{M}_{3} \mathrm{C}$ methodology considers only final minima on the PES and discards energy barriers. The effect of mentioned approach can be seen in Figure 5.23, where results of all three theoretical methods are included. In this figure, $\mathrm{M}_{3} \mathrm{C}$ probabilities of specific species are plotted with its occurrences obtained by the ADMP method and grey blocks representing the height of calculated barriers. An assumption that the system holds enough energy to overcome all barriers can be untrue for depositions of lower energies into the system. In the case of furan cation, the undesirable feature is visible for fragments $\mathrm{H}_{4} \mathrm{C}_{3}^{+}$and $\mathrm{H}_{2} \mathrm{C}_{4} \mathrm{O}^{+}$, where $\mathrm{M}_{3} \mathrm{C}$ species probabilities begin to occur before calculated energy barriers. The $\mathrm{H}_{4} \mathrm{C}_{3}^{+}$ion starts to appear 1.09 eV before the barrier, but the shift is much more pronounced for the $\mathrm{H}_{2} \mathrm{C}_{4} \mathrm{O}^{+}$ion, which occurs 4.56 eV before the barrier. One way of getting around this problem is inclusion of barriers by increasing the energy of fragments $\mathrm{H}_{2} \mathrm{C}_{4} \mathrm{O}^{+}$and $\mathrm{H}_{4} \mathrm{C}_{3}^{+}$by the respective barrier heights. This approach requires the assumption that vibrational frequencies of the respective transition structures don't vary considerably from the products. Then, the entropic contribution of the barrier is disregarded and only the energetic part is included in the calculation.


Figure 5.24 Simplified lowest reaction pathways for furan cation decomposition. Only critical points are shown.

A simplified version of fragmentation pathways in Figure 5.24 illustrates in red values of included barriers: 5.37 eV for the $\mathrm{H}_{2} \mathrm{C}_{4} \mathrm{O}^{+}$species, 1.14 eV for allene cation and 0.64 eV for propyne cation. This alteration leads to results presented in Figures 5.25 5.27. Firstly, it can be seen that in comparison with Figure 5.23, probabilities of fragments $\mathrm{H}_{2} \mathrm{C}_{4} \mathrm{O}^{+}$and $\mathrm{H}_{3} \mathrm{C}_{4} \mathrm{O}^{+}$decrease completely and anticipated increase of $\mathrm{H}_{3} \mathrm{C}_{3}^{+}$probability occurs. Furan cation starts to dissociate around 3.5 eV . Figure 5.25 a) shows that $\mathrm{H}_{3} \mathrm{C}_{3}^{+}$ion is first produced by the channel $\mathrm{H}_{3} \mathrm{C}_{3}^{+} / \mathrm{HCO}$ and from the energy of 5 eV channel $\mathrm{H}_{3} \mathrm{C}_{3}^{+} / \mathrm{CO} / \mathrm{H}$ dominates. Moreover, $\mathrm{H}_{4} \mathrm{C}_{3}^{+} / \mathrm{CO}$ remains an important channel, but never exceeds probability for production of $\mathrm{H}_{3} \mathrm{C}_{3}^{+}$. From panel b) of Figure 5.25 it can be seen that $\mathrm{H}_{3} \mathrm{C}_{3}^{+}$ion becomes now the most abundant charged fragment until 11 eV . A significant species observed for the energy range of $3.5-7 \mathrm{eV}$ is $\mathrm{H}_{4} \mathrm{C}_{3}^{+}$cation. Since the energy of 11 eV fragmentation process begins to be so abundant that it is difficult to determine unambiguously which fragments are the most prevalent. Highly observed species are $\mathrm{H}_{2} \mathrm{C}_{3}^{+}, \mathrm{HC}_{3}^{+}$and $\mathrm{HCO}^{+}$. Figure 5.26 summarizes results of three methods applied in the present study. It can be noticed that no fragments appear before calculated energy barriers. The shift of ADMP breakdown curves to higher energy values compared with $\mathrm{M}_{3} \mathrm{C}$ is caused by a different consideration of time by the theoretical methods. ADMP method considers time explicitly, however $\mathrm{M}_{3} \mathrm{C}$ follows the ergodic hypothesis stating that time averages correspond to space averages in a microcanonical ensemble.


FIGURE 5.25 Results of $\mathrm{M}_{3} \mathrm{C}$ calculations of singly ionized furan: a) channels and $\mathbf{b}$ ) charged species probabilities as a function of the internal energy. Error bars correspond to standard deviations of the probabilities averaged over all experiments. Only channels/species with probabilities larger than $10 \%$ are shown.


FIGURE 5.26 Comparison of significant species probabilities calculated by ADMP method (red) and $\mathrm{M}_{3} \mathrm{C}$ (blue) after inclusion of barriers for fragments $\mathrm{H}_{2} \mathrm{C}_{4} \mathrm{O}^{+}$and $\mathrm{H}_{3} \mathrm{C}_{4} \mathrm{O}^{+}$. Grey areas cover the energy range until the value of calculated barrier for each fragment.

Consequently, if the dynamical simulations could run until infinite time, in principle, ADMP and $\mathrm{M}_{3} \mathrm{C}$ breakdown curves should overlap. Similar trends and maximum values can be observed for fragments $\mathrm{H}_{2} \mathrm{C}_{2} \mathrm{O}^{+}, \mathrm{HCO}^{+}$and $\mathrm{HC}_{3}^{+}$, but species $\mathrm{H}_{4} \mathrm{C}_{3}^{+}, \mathrm{H}_{3} \mathrm{C}_{3}^{+}$and $\mathrm{H}_{2} \mathrm{C}_{3}^{+}$present completely different features. Although $\mathrm{M}_{3} \mathrm{C}$ probabilities of fragments $\mathrm{H}_{2} \mathrm{C}_{4} \mathrm{O}^{+}$and $\mathrm{H}_{3} \mathrm{C}_{4} \mathrm{O}^{+}$ decrease completely, they are obtained by the ADMP method. Again, the reason of these discrepancies is limited simulation time of the molecular dynamics simulations. Hence, at some later point in time $\mathrm{H}_{2} \mathrm{C}_{4} \mathrm{O}^{+}$and $\mathrm{H}_{3} \mathrm{C}_{4} \mathrm{O}^{+}$are expected to decompose.


FIGURE 5.27 Results of $\mathrm{M}_{3} \mathrm{C}$ calculations of singly ionized furan after inclusion of calculated energy barriers: detailed channels probabilities as a function of the internal energy.

Lastly, $\mathrm{M}_{3} \mathrm{C}$ program provides an essential tool allowing to identify type of produced isomers. Figure 5.27 details channels probabilities producing ions $\mathrm{H}_{4} \mathrm{C}_{3}^{+}, \mathrm{H}_{3} \mathrm{C}_{3}^{+}, \mathrm{H}_{2} \mathrm{C}_{3}^{+}$and $\mathrm{HC}_{3}^{+}$. In accordance with PES exploration, $\mathrm{H}_{4} \mathrm{C}_{3}^{+}$cation is mostly produced in allene form as well as $\mathrm{HC}_{3}^{+}$in linear configuration. However, not always the lowest energy isomer prevails. For the $\mathrm{H}_{3} \mathrm{C}_{3}^{+}$cation, observation of cyclopropenium ion dominates initially, but since the energy of 9 eV a linear isomer - propargyl cation - becomes more abundant. Moreover, although cyclic isomer of $\mathrm{H}_{2} \mathrm{C}_{3}^{+}$presents higher stability, a linear geometry is favoured as a product of fragmentation of furan cation.

### 5.2.4 Comparison with photon and ion collision experiments

Analogies between the results presented in preceding sections and previously performed experiments enable verification of the theoretical predictions and provide novel interpretation of the already measured data. A direct comparison can be made between measured ion Appearance Energies and calculated energy barriers for production of specific species. Previous electron impact ionization [2] and photoionization [11], [39] studies provide such results, given in Table 5.5.

TABLE 5.5 Lowest energy barriers of PES for selected charged fragments (in eV ) compared with the AEs measurements of electron impact (EI), threshold photoelectron photoion coincidence (TPEPICO) and photoionization (PI) experiments.

| $\mathrm{m} / \mathrm{z}$ (fragment ion) | Channel | Lowest energy barrier | Dampc et al <br> [2] EI | Rennie et <br> al [39] <br> TPEPICO | Rennie et al [11] PI |
| :---: | :---: | :---: | :---: | :---: | :---: |
| $68\left(\mathrm{H}_{4} \mathrm{C}_{4} \mathrm{O}^{+}\right)$ |  | 8.93 | $8.80 \pm 0.10$ |  |  |
| $67\left(\mathrm{H}_{3} \mathrm{C}_{4} \mathrm{O}^{+}\right)$ | $\begin{aligned} & \min 15^{+}+\mathrm{H} \\ & \alpha \text {-furyl } \end{aligned}$ | $\begin{aligned} & 12.44 \\ & 14.60 \end{aligned}$ | $12.80 \pm 0.10$ |  | 13.22 |
| $66\left(\mathrm{H}_{2} \mathrm{C}_{4} \mathrm{O}^{+}\right)$ | $\begin{aligned} & \mathrm{H}_{2} \mathrm{C}_{4} \mathrm{O}^{+}+\mathrm{H}+\mathrm{H} \\ & \mathrm{H}_{2} \mathrm{C}_{4} \mathrm{O}^{+}+\mathrm{H}_{2} \end{aligned}$ | $\begin{aligned} & 15.38 \\ & 15.99 \end{aligned}$ | $16.85 \pm 0.10$ |  | 17.32 |
| $42\left(\mathrm{H}_{2} \mathrm{C}_{2} \mathrm{O}^{+}\right)$ | $\mathrm{H}_{2} \mathrm{C}_{2} \mathrm{O}^{+}+\mathrm{H}_{2} \mathrm{C}_{2}$ | 12.03 | $11.25 \pm 0.10$ | 11.80 | 11.8-11.9 |
| $40\left(\mathrm{H}_{4} \mathrm{C}_{3}^{+}\right)$ | $\begin{aligned} & \mathrm{H}_{2} \mathrm{CCCH}_{2}^{+}+\mathrm{CO} \\ & \mathrm{c}-\mathrm{H}_{2} \mathrm{CCHCH}^{+}+\mathrm{CO} \end{aligned}$ | $\begin{aligned} & 11.52 \\ & 11.73 \end{aligned}$ | $11.45 \pm 0.10$ | 11.60 | 11.8-12.0 |
| $39\left(\mathrm{H}_{3} \mathrm{C}_{3}^{+}\right)$ | $\begin{aligned} & \mathrm{c}-\mathrm{H}_{3} \mathrm{C}_{3}^{+}+\mathrm{HCO} \\ & \mathrm{c}-\mathrm{H}_{3} \mathrm{C}_{3}^{+}+\mathrm{CO}+\mathrm{H} \\ & \mathrm{H}_{2} \mathrm{CCCH}^{+}+\mathrm{CO}+\mathrm{H} \end{aligned}$ | $\begin{aligned} & 11.78 \\ & 12.91 \\ & 14.99 \end{aligned}$ | $12.60 \pm 0.10$ | 12.05 | 12.46 |
| $38\left(\mathrm{H}_{2} \mathrm{C}_{3}^{+}\right)$ | $\begin{aligned} & \mathrm{HCCCH}^{+}+\mathrm{H}_{2} \mathrm{CO} \\ & \mathrm{HCCCH}^{+}+\mathrm{CO}+\mathrm{H}_{2} \\ & \mathrm{HCCCH}^{+}+\mathrm{CO}+2 \mathrm{H} \\ & \mathrm{c}-\mathrm{H}_{2} \mathrm{C}_{3}^{+}+\mathrm{CO}+2 \mathrm{H} \end{aligned}$ | $\begin{aligned} & 13.43 \\ & 15.99 \\ & 17.80 \\ & 18.07 \end{aligned}$ | $12.85 \pm 0.10$ | 14.50 | 14.17 |
| $37\left(\mathrm{HC}_{3}^{+}\right)$ | $\mathrm{HC}_{3}^{+}+\mathrm{CO}+\mathrm{H}_{2} \mathrm{H}$ | 17.54 | $17.70 \pm 0.15$ | 18.25 | 18.31 |
| $29\left(\mathrm{HCO}^{+}\right)$ | $\begin{aligned} & \mathrm{HCO}^{+}+\mathrm{H}_{2} \mathrm{CCCH} \\ & \mathrm{HCO}^{+}+\mathrm{c}-\mathrm{H}_{2} \mathrm{C}_{3}+\mathrm{H} \end{aligned}$ | $\begin{aligned} & 12.78 \\ & 16.21 \end{aligned}$ | $12.40 \pm 0.20$ | 13.00 | 12.84 |
| $14\left(\mathrm{H}_{2} \mathrm{C}^{+}\right)$ | $\begin{aligned} & \mathrm{H}_{2} \mathrm{C}^{+}+\mathrm{H}_{2} \mathrm{CC}+\mathrm{CO} \\ & \mathrm{H}_{2} \mathrm{C}^{+}+\mathrm{HCCH}+\mathrm{CO} \end{aligned}$ | $\begin{aligned} & 15.72 \\ & 17.50 \end{aligned}$ | $17.35 \pm 0.15$ | 17.00 | 17.76 |

Calculated energy barriers should correspond to the dissociation onsets for specific species. Table 5.5 shows satisfactory agreement between the present computational results and experimental studies. Firstly, measured values of AEs for $\mathrm{H}_{3} \mathrm{C}_{4} \mathrm{O}^{+}$ion confirm that hydrogen is eliminated from $\mathrm{H}_{4} \mathrm{C}_{4} \mathrm{O}^{+}$isomer rather than directly from ionized furan. Moreover, studies of metastable transitions performed by Rennie et al [11] suggested that $\mathrm{H}_{2} \mathrm{C}_{4} \mathrm{O}^{+}$ion is produced by the sequential loss of two hydrogen atoms rather than by elimination of molecular hydrogen. Indeed, lower energy barrier was found for sequential H loss from furan cation, however measured AEs of $\mathrm{H}_{2} \mathrm{C}_{4} \mathrm{O}^{+}$remain around $1.5-2 \mathrm{eV}$ higher than calculated values.

A barrier higher by $0.13-0.23 \mathrm{eV}$ than measured photoionization AE was calculated for the production of ketene cation $-\mathrm{H}_{2} \mathrm{C}_{2} \mathrm{O}^{+}$. However, barrier height for formation of $\mathrm{H}_{4} \mathrm{C}_{3}^{+}$coincides perfectly with measured values. Willett and Baer [38] determined experimental rates for the production of $\mathrm{H}_{4} \mathrm{C}_{3}^{+}$and $\mathrm{H}_{2} \mathrm{C}_{2} \mathrm{O}^{+}$from the total dissociation rates and PEPICO branching ratios. Their values were identical, suggesting the competition between these species and a
possibility of common transition structure. Present study indicates that different points on the PES are rate determining for $\mathrm{H}_{4} \mathrm{C}_{3}^{+}$and $\mathrm{H}_{2} \mathrm{C}_{2} \mathrm{O}^{+}$. However, a possibility of proceeding through a shared pathway arises from a very small difference between the lowest and the second lowest barriers for production of allene cation. The transition structure for $2,1 \mathrm{H}$ transfer was located at 11.52 eV (ts1) and for $1,2 \mathrm{H}$ transfer at 11.56 eV (ts6). A difference of only 0.04 eV and equal rates for the formation of $\mathrm{H}_{4} \mathrm{C}_{3}^{+}$and $\mathrm{H}_{2} \mathrm{C}_{2} \mathrm{O}^{+}$can indicate that indeed $1,2 \mathrm{H}$ transfer is the first step of producing these species. Furthermore, the kinetic energy release distribution for the loss of the CO fragment measured by Holmes and Terlouw [36] showed that a wide range of kinetic energies is released upon fragmentation. This result implies feasible participation of many isomeric structures of $\mathrm{H}_{4} \mathrm{C}_{3}^{+}$. Indeed, the dynamical simulations also show high abundance of cyclopropene ( $\mathrm{c}-\mathrm{H}_{2} \mathrm{CCHCH}^{+}$) cation.

The barrier height for production of $\mathrm{H}_{3} \mathrm{C}_{3}^{+}$agrees best with TPEPICO studies and is 0.82 eV lower than measured after electron impact. Higher onset energy than observed for $\mathrm{H}_{4} \mathrm{C}_{3}^{+}$and $\mathrm{H}_{2} \mathrm{C}_{2} \mathrm{O}^{+}$does not exclude high production rate of this ion. Dampc et al [2] reported that $\mathrm{H}_{3} \mathrm{C}_{3}^{+}$ ions are the most abundant products of electron induced dissociation. As shown in the section of PES exploration, simple formation mechanisms with loose transition structures can be the reason for such high occurrence of $\mathrm{H}_{3} \mathrm{C}_{3}^{+}$. Rennie et al [39] concluded from their TPEPICO experiment that by the energy of around $13 \mathrm{eV} \mathrm{H}_{3} \mathrm{C}_{3}^{+}$becomes the most important fragment. They mentioned no experimental means of differentiating between direct and sequential processes, but the present study confirms that H loss channel producing $\mathrm{H}_{3} \mathrm{C}_{3}^{+}$should open around 12.91 eV .

Calculated lowest energy barrier for production of $\mathrm{H}_{2} \mathrm{C}_{3}^{+}$is located in between AEs measured by different techniques, so no clear conclusion can be made from comparison of these values. A discrepancy between thermodynamical threshold and measured AEs has been indicated by Rennie et al [39]. However, in their photoionization experiment [11] $\mathrm{H}_{2} \mathrm{C}_{3}^{+}$has been prominent in the daughter ion spectra, suggesting a sequential process. Dynamical simulations of the present study suggest production of $\mathrm{H}_{2} \mathrm{C}_{3}^{+}$cation after elimination of two hydrogen atoms, a process to which energy onset has been predicted at 17.80 eV . This is in perfect accord with an observation from [39] that a new channel to the $\mathrm{H}_{2} \mathrm{C}_{3}^{+}$fragment opens between 17.6 and 18.0 eV . Although authors propose that $\mathrm{H}_{2} \mathrm{C}_{3}^{+}$is produced by H loss from $\mathrm{H}_{3} \mathrm{C}_{3}^{+}$, this conclusion is not supported by the present study.

Good agreement can be noticed for the $\mathrm{HC}_{3}^{+}$ion. This comparison indicates that indeed H loss is followed by $\mathrm{H}_{2}$ loss in forming $\mathrm{HC}_{3}^{+}$, contrary to the proposal from [39] that this fragment is produced in channel $\mathrm{HC}_{3}^{+} / \mathrm{HCO} / \mathrm{H}_{2}$. Additional notion against this suggestion is that channel $\mathrm{HCO}^{+} / \mathrm{HC}_{3} / \mathrm{H}_{2}$ is more energetically favourable.

Measured AE aligns well with calculated lowest energy barrier for production of $\mathrm{HCO}^{+}$, indicating that formyl cations are first produced in two-body fragmentation channel resulting in propargyl radicals as neutral species. A good agreement between lowest energy barrier of channel $\mathrm{H}_{2} \mathrm{C}^{+} / \mathrm{HCCH} / \mathrm{CO}$ and AE of $\mathrm{H}_{2} \mathrm{C}^{+}$denotes that this ion is most likely produced in three body fragmentation, which requires 17.50 eV of internal energy.

It is worth pointing out that higher values of measured AEs than calculated ones can be expected due to the kinetic shift (the shift of the onset to an energy sufficient enough so that
the rate of decomposition exceeds some minimum value). Moreover, higher energy alternate processes generally show a slow onset at threshold, causing a significant kinetic shift [39]. Additionally, the applied theoretical method can be the source of some small discrepancies. As far as various computational methods are expected to give different absolute energies of optimized structures, values of relative energies should not essentially differ.


FIGURE 5.28 Comparison of breakdown curves calculated with $\mathrm{M}_{3} \mathrm{C}$ and measured in the PEPICO experiment. Lowest right panel presents fragments that didn't appear in the PEPICO experiment, but were obtained by $\mathrm{M}_{3} \mathrm{C}$ method with probability higher than $10 \%$.

An extended theoretical investigation presented in this thesis, including three methodologies, might guide new experimental efforts. In particular, breakdown curves recorded by PEPICO technique over wide energy range can be directly compared with those predicted by the statistical theory of $\mathrm{M}_{3} \mathrm{C}$. The most recent experimental measurements have been performed by Paola Bolognesi and co-workers at the Elettra synchrotron radiation facility in Trieste, Italy [96]. Figure 5.28 shows comparison of the experimental data and the theoretical results for significant species. It can be noticed that the shape of the curves is correctly reproduced for all fragments besides $\mathrm{H}_{2} \mathrm{C}^{+}$and $\mathrm{H}_{2} \mathrm{C}_{3}^{+} . \mathrm{M}_{3} \mathrm{C}$ probabilities of these ions present two
distinct maxima, whereas the ones recorded by PEPICO show only one. As for differences in intensity, a decrease of about $30 \%$ can be observed for $\mathrm{H}_{3} \mathrm{C}_{3}^{+}$between 5 and 11 eV . Despite this absolute discrepancy, both experimental and theoretical studies indicate that $\mathrm{H}_{3} \mathrm{C}_{3}^{+}$is the most abundant species in the mentioned energy range. Moreover, detailed $\mathrm{M}_{3} \mathrm{C}$ channels probabilities suggest that two peaks, which also occur in the PEPICO breakdown curve of $\mathrm{H}_{3} \mathrm{C}_{3}^{+}$, result from channels of H loss. First peak corresponds to production of $\mathrm{c}-\mathrm{H}_{3} \mathrm{C}_{3}^{+}$and the second one to production of $\mathrm{H}_{2} \mathrm{CCCH}^{+}$. A narrow breakdown curve with a maximum around 4 eV can be observed for fragmentation to $\mathrm{H}_{4} \mathrm{C}_{3}^{+}$by both studies. $\mathrm{M}_{3} \mathrm{C}$ probability for production of $\mathrm{H}_{2} \mathrm{C}_{3}^{+}$ originates from two channels: $\mathrm{H}_{2} \mathrm{C}_{3}^{+} / \mathrm{CO} / \mathrm{H}_{2}$ (lower energies) and $\mathrm{H}_{2} \mathrm{C}_{3}^{+} / \mathrm{CO} / 2 \mathrm{H}$ (higher energies). A discrepancy between experimentally observed values for lower energies suggest that this fragment is rather produced in the channel of four body fragmentation. This is in accordance with the dynamical simulations showing that indeed majority of $\mathrm{H}_{2} \mathrm{C}_{3}^{+}$is produced in channel of double atomic hydrogen loss. $\mathrm{M}_{3} \mathrm{C}$ probability for production of $\mathrm{HC}_{3}^{+}$presents a good shape in comparison with PEPICO results. However, an underestimation in the intensity of around $10 \%$ can be noticed. Breakdown curves of $\mathrm{HCO}^{+}$overlap for energies from 12 to 20 eV , but differ between 6 and 12 eV . Moreover, $\mathrm{M}_{3} \mathrm{C}$ probability for production of $\mathrm{H}_{2} \mathrm{C}_{2}^{+}$starts to appear earlier by around 5 eV . Breakdown curves of $\mathrm{H}_{2} \mathrm{C}_{2} \mathrm{O}^{+}$overlap from the energy of 3 eV , but start to diverge at 12 eV , indicating that $\mathrm{H}_{2} \mathrm{C}_{2} \mathrm{O}^{+}$is produced in channel $\mathrm{H}_{2} \mathrm{C}_{2} \mathrm{O}^{+} / \mathrm{H}_{2} \mathrm{C}_{2}$ (before 12 eV ) rather than in $\mathrm{H}_{2} \mathrm{C}_{2} \mathrm{O}^{+} / \mathrm{HC}_{2} / \mathrm{H}$ (after 12 eV ).

A source of occurring deviations can originate from a number of species obtained in the $\mathrm{M}_{3} \mathrm{C}$ calculations that were not observed in PEPICO (lowest right panel of Figure 5.28). Their appearance reduces mostly the intensity of $\mathrm{H}_{2} \mathrm{C}^{+}, \mathrm{H}_{3} \mathrm{C}_{3}^{+}$but also other species. It is possible that although fragments unrecorded by PEPICO are entropically favourable, they present a high energy barrier that $\mathrm{M}_{3} \mathrm{C}$ does not account for.

Results obtained by the $\mathrm{M}_{3} \mathrm{C}$ method may be also compared with experimental mass spectra. For this purpose it is necessary to determine energy distribution functions distinctive for every collisional system. The method of acquiring these functions is presented in Chapter 3, so here only the results of the fitting procedure are shown (Figure 5.29). Mass spectra detected after the production of singly ionized furan in the interaction with different ions ( 3 keV $\mathrm{Ar}^{+}, 48 \mathrm{keV} \mathrm{O}^{3+}, 48 \mathrm{keV} \mathrm{O}^{6+}, 165 \mathrm{keV} \mathrm{Ar}^{11+}$ and $565 \mathrm{keV} \mathrm{Xe}^{25+}$ ) have been recently obtained by Patrick Rousseau and co-workers at ARIBE, the low-energy ion beam facility of GANIL (Grand Accélérateur National d'Ions Lourds) in Caen, France [97]. It has been previously shown [98], [99] that projectile charge state significantly influences energy deposition into the system. Generally, for higher charge states the collisions take place at larger impact parameters, leading to decrease in probability of energy transfer. Results presented in this work support these findings. Figure 5.29 exhibits energy deposition functions of various shapes and positions of peaks for different projectiles. Particularly, energy deposition functions of $\mathrm{Ar}^{+}$, electrons and $\mathrm{O}^{3+}$ present only one peak with maxima at 6,4 , and 3.5 eV , respectively. Hence, it can be seen that with the increasing charge of the ions the highest peak shifts to the lower values of energy. Different distributions were found for $\mathrm{O}^{6+}, \mathrm{Ar}^{11+}$ and $\mathrm{Xe}^{25+}$, where two peaks (around 1 eV and 5 eV ) and a flat region of probability for energies between 13 and 20 eV can be noticed. As far as collision with $\mathrm{O}^{6+}$ leads to a distinct peak of around $70 \%$ at 5 eV , energy deposition
functions of $\mathrm{Ar}^{11+}$ and $\mathrm{Xe}^{25+}$ demonstrate only a small convex around $50 \%$ and $30 \%$, respectively. Presented features are reflected in the fact that multiply ionized projectiles give rise to less fragmentation products and higher intensity of the parent ion, however $\mathrm{Ar}^{+}, \mathrm{O}^{3+}$ and electrons induce richer fragmentation.


Figure 5.29 Fitted energy deposition functions for various projectiles.

Convolution of the $\mathrm{M}_{3} \mathrm{C}$ probabilities with fitted deposited energy functions results in theoretical mass spectra presented in Figures 5.30 and 5.31. Firstly, as the statistical theory produces more abundant fragmentation due to the lack of barriers, obtained theoretical mass spectra often show peaks for fragments that were not observed in the experiments. In particular, overestimations of peaks can be noticed in $\mathrm{m} / \mathrm{z}$ regions of $40-43$ and $50-53$. Furthermore, for $\mathrm{Ar}^{+}$ and electrons, when fragment $\mathrm{H}_{3} \mathrm{C}_{3}^{+}$presents the highest intensity, a peak corresponding to the parent ion is overestimated as well. Similarly to the case of photon induced fragmentation, $\mathrm{H}_{3} \mathrm{C}_{3}^{+}$was the most significant decomposition product in the interaction with different ions. Figures 5.30 and 5.31 show that the weaker the fragmentation, the better the reproduction of the most important species: $\mathrm{H}_{3} \mathrm{C}_{3}^{+}$. The most noticeable underestimation can be observed for $\mathrm{HC}_{3}^{+}$and $\mathrm{HCO}^{+}$. As a summary, a general observation in the discussion of theoretical and experimental mass spectra is that existing peaks of $\mathrm{m} / \mathrm{z}$ below $39\left(\mathrm{H}_{3} \mathrm{C}_{3}^{+}\right)$are underestimated and peaks above that value are overestimated.


FIGURE 5.30 Comparison of theoretical and experimental mass spectra after collision with a) $\mathrm{Ar}^{+}$b) $\mathrm{e}^{-}$c) $\mathrm{O}^{3+}$.


FIGURE 5.31 Comparison of theoretical and experimental mass spectra after collision with a) $\mathrm{O}^{6+}$ b) $\mathrm{Ar}^{11+}$ c) $\mathrm{Xe}^{25+}$.

### 5.3 Doubly ionized furan

### 5.3.1 Molecular Dynamics

Results of the dynamical simulations of doubly ionized furan are presented in Figures 5.32 5.36. A different approach than for neutral and singly ionized molecule was required for clear discussion of observed processes. Four possible mechanisms have been distinguished: (1) isomerization (2) skeleton fragmentation (3) $\mathrm{H}^{+} / \mathrm{H}_{2}^{+}$loss and (4) $\mathrm{H} / \mathrm{H}_{2}$ loss. Their abundances are presented in Figure 5.32 a). Again, isomerization indicates intramolecular hydrogen migration or cleavage of one of the C-O/C-C bonds. This process already appears for the first considered energy of 5 eV and is lastly identified at 24 eV . Isomerization occurs for a wide energy range, however, its abundance never exceeds $20 \%$. Such outcome does not exclude isomerization taking place throughout the course of the simulation, but indicates that at the last time step (300 fs) observation of only this process is infrequent. Skeleton fragmentation denotes here that no atomic or molecular hydrogen is ejected in neither neutral nor charged state. From the energy of 10 eV until 20 eV , cleavage of the furan ring dominates. Third process, corresponding to loss of an ionized hydrogen $\left(\mathrm{H}^{+} / \mathrm{H}_{2}^{+}\right)$, prevails for energies between 21 and 30 eV . It is possible that channels of this type also contain H or $\mathrm{H}_{2}$ as fragments in a neutral state. Finally, fourth family of observed processes implies neutral hydrogen loss, meaning that charge is localized


FIgURE 5.32 Results of the ADMP simulations of doubly ionized furan: total occurrence of a) observed processes b) number of fragments as a function of internal energy.
on fragments containing C and/or O . This mechanism is never a dominant process, but since 14 eV its total occurrence increases until reaching maximum value of $42 \%$ for the energy of 26 eV . Figure $5.32 \mathbf{~ b}$ ) illustrates number of produced fragments as a function of the deposited energy. The occurrence of one fragment decreases until the energy of 26 eV . Two fragments can be observed for all considered energies with a maximum of $86 \%$ at 14 eV . Next, three body fragmentation occurs from 12 to 30 eV and is the most abundant process between 20 and 29 eV . At last considered energy of 30 eV four body fragmentation prevails. Production of five fragments was a minor process occurring from 27 eV with a maximum probability of $9 \%$ at 30 eV .


FIGURE 5.33 Results of the ADMP simulations of doubly ionized furan: a) total occurrence of the most abundant isomerization channels b) snapshots of trajectories leading to channels from the left panel.

The process requiring the least amount of internal energy was found to be isomerization, detailed in Figure 5.33. Three principal structures have been identified. Panel a) illustrates their occurrence as a function of the internal energy and panel $\mathbf{b}$ ) shows possible production mechanisms of these isomers. The first and most populated structure is produced through ring opening by cleavage of the $\mathrm{C}-\mathrm{O}$ bond and rotation around $\mathrm{C}_{\alpha}-\mathrm{C}_{\beta}$ bond. This mechanism is the most abundant from the energy of 5 until 13 eV . Second isomer implies ring opening by cleavage of the C-O bond as well, but is followed by a $2,1 \mathrm{H}$ transfer. Finally, isomerization channel dominating for higher energies (between 16 and 19 eV ) relies on cleavage of the $\mathrm{C}-\mathrm{O}$ bond and concerted 1,2 and $2,1 \mathrm{H}$ transfer occurring on the opposite sides of the furan ring.


FIgURE 5.34 Results of the ADMP simulations of doubly ionized furan: a) total occurrence of channels in coincidence with $\mathrm{HCO}^{+} \mathbf{b}$ ) snapshots of trajectories leading to channels from the left panel. Only channels that appeared at least $5 \%$ at a certain point in the energy range are presented.

Results of the dynamical simulations finishing with charged fragments $\mathrm{HCO}^{+}$and $\mathrm{H}_{n} \mathrm{C}_{3}^{+}$ ( $\mathrm{n}=3-1$ ) are shown in Figure 5.34. Panel a) of Figure 5.34 demonstrates that two-body decomposition to $\mathrm{H}_{3} \mathrm{C}_{3}^{+}$and $\mathrm{HCO}^{+}$is clearly the most abundant channel between energies of 11 and 21 eV and is also the only significant channel of skeleton fragmentation. Time evolution of trajectories containing decomposition to two possible configurations of $\mathrm{H}_{3} \mathrm{C}_{3}^{+}$are shown in the first two panels of Figure 5.34 b). Production of a cyclopropenium cation (c$\mathrm{H}_{3} \mathrm{C}_{3}^{+}$) proceeds through ring opening by rupture of the C -O bond and subsequent $\mathrm{C}_{\alpha}-\mathrm{C}_{\beta}$ bond cleavage. An intermediate step of this mechanism corresponds to the most abundant channel of isomerization, indicating that if given more simulation time, trajectories finishing with $\mathrm{HCCHCHCHO}^{++}$would increase the production yield of channel $\mathrm{c}-\mathrm{H}_{3} \mathrm{C}_{3}^{+} / \mathrm{HCO}^{+}$. Formation of propargyl cation $\left(\mathrm{H}_{2} \mathrm{CCCH}^{+}\right)$has been observed as well and is presented in the second panel of Figure 5.34 b). This channel follows rearrangement to $\mathrm{H}_{2} \mathrm{CCCHCHO}^{++}$(second most populated isomer) by cleavage of the $\mathrm{C}_{\alpha}-\mathrm{C}_{\beta}$ bond. Hence again, longer simulation time should increase the abundance of channel $\mathrm{H}_{2} \mathrm{CCCH}^{+} / \mathrm{HCO}^{+}$. Among skeleton fragmentation channels, $\mathrm{c}-\mathrm{H}_{3} \mathrm{C}_{3}^{+} / \mathrm{HCO}^{+}$is expected to be the most abundant due to simple formation mechanism. However, the conclusion which isomer will prevail can only be confirmed by further exploration of the Potential Energy Surface of these reactions. Remaining channels, presented in Figure 5.34 , rely on additional $\mathrm{H} / \mathrm{H}_{2}$ loss. The one exhibiting significant occurrence corresponds to formation of $\mathrm{H}_{2} \mathrm{C}_{3}^{+}, \mathrm{HCO}^{+}$and H . Statistical analysis of trajectories producing this channel indicates that $\alpha$ position is the preferable site for hydrogen loss ( $53 \%$ of observed cases). Possible mechanism of producing this channel, demonstrated in Figure 5.34 b), proceeds through removal of hydrogen from $\alpha$ position, cleavages of $\mathrm{C}-\mathrm{O}$ and subsequently $\mathrm{C}_{\alpha}-\mathrm{C}_{\beta}$ bonds.

The least populated channels, presented in Figure 5.34 a), produce $\mathrm{HC}_{3}^{+}, \mathrm{HCO}^{+}$as charged species and either hydrogen molecule or two atomic hydrogens. Of these two, $\mathrm{HC}_{3}^{+} / \mathrm{HCO}^{+} / \mathrm{H}_{2}$ appears earlier in the energy range (at 12 eV ) and is dominant until the energy of 24 eV . At 26 eV channel $\mathrm{HC}_{3}^{+} / \mathrm{HCO}^{+} / 2 \mathrm{H}$ shows maximum probability, but its total occurrence never exceeds $10 \%$. Snapshots of exemplifying trajectories indicate that production of $\mathrm{HCO}^{+} / \mathrm{H}_{2} \mathrm{CCCH}^{+}$is an intermediate step in channel $\mathrm{HC}_{3}^{+} / \mathrm{HCO}^{+} / \mathrm{H}_{2}$ and $\mathrm{H}_{2}$ is removed from propargyl cation. Four-body fragmentation to channel $\mathrm{HC}_{3}^{+} / \mathrm{HCO}^{+} / 2 \mathrm{H}$ might proceed through two hydrogens being lost from adjacent $\alpha$ and $\beta$ positions, $\mathrm{C}-\mathrm{O}$ and $\mathrm{C}_{\alpha}-\mathrm{C}_{\beta}$ bond cleavages with cyclization of the $\mathrm{HC}_{3}^{+}$fragment.


FIGURE 5.35 Results of ADMP simulations of doubly ionized furan: a) total occurrence of channels in coincidence with $\mathrm{H}^{+} \mathbf{b}$ ) snapshots of trajectories leading to channels from the left panel. Only channels that appeared at least $5 \%$ at a certain point in the energy range are presented.

Second type of distinguished mechanisms, presented in Figure 5.35, consists of deprotonation. Loss of $\mathrm{H}^{+}$has been observed in coincidence with $\mathrm{H}_{3} \mathrm{C}_{4} \mathrm{O}^{+}$and with $\mathrm{H}_{n} \mathrm{C}_{3}^{+}$( $\mathrm{n}=$ 3-1). Channel $\mathrm{H}_{3} \mathrm{C}_{4} \mathrm{O}^{+} / \mathrm{H}^{+}$is the first to appear, but at the energy of 16 eV the dynamical simulations already show prevalence of the $\mathrm{H}_{3} \mathrm{C}_{3}^{+} / \mathrm{H}^{+} / \mathrm{CO}$, the most abundant channel of deprotonation over all energies. First two panels of Figure 5.35 b) illustrate possible production mechanisms, which rely on $\mathrm{H}_{\alpha}^{+}$loss and subsequent $\mathrm{C}-\mathrm{O}$ and $\mathrm{C}_{\alpha}-\mathrm{C}_{\beta}$ bond cleavages to produce $\mathrm{c}-\mathrm{H}_{3} \mathrm{C}_{3}^{+}$or 1,2 and $2,1 \mathrm{H}$ transfers on the opposite sides of the ring, followed by $\mathrm{C}-\mathrm{O}$ and $\mathrm{C}_{\alpha}-\mathrm{C}_{\beta}$ bond cleavages to produce $\mathrm{H}_{2} \mathrm{CCCH}^{+}$. Loss of $\mathrm{H}_{\alpha}^{+}$prevails in substantial majority of calculated trajectories $(81 \%)$. At the energy of 27 eV channel $\mathrm{H}_{2} \mathrm{C}_{3}^{+} / \mathrm{H}^{+} / \mathrm{CO} / \mathrm{H}$ becomes the most abundant. Formation mechanism of this channel is presented in the third panel of Figure 5.35 b). It can be seen that $\mathrm{H}^{+}$and H loss from adjacent $\alpha$ and $\beta$ positions is followed by fragmentation. The least populated channel in Figure 5.35 a) reaches maximum total occurrence of $10 \%$ at the energy of 28 eV and produces $\mathrm{HC}_{3}^{+}, \mathrm{H}^{+}, \mathrm{CO}$ and $\mathrm{H}_{2}$. Probable formation mechanism, presented in the last panel of Figure $5.35 \mathbf{b}$ ), implies $\mathrm{H}^{+}$loss from $\alpha$ position, fragmentation to $\mathrm{c}-\mathrm{H}_{3} \mathrm{C}_{3}^{+} / \mathrm{CO}$ and finally $\mathrm{H}_{2}$ loss from $\mathrm{c}-\mathrm{H}_{3} \mathrm{C}_{3}^{+}$.


FIGURE 5.36 Results of the ADMP simulations of doubly ionized furan: average time scales of sequential events leading to channels that appeared at least $10 \%$ at a certain point in the energy range: a) $\mathrm{H}_{2} \mathrm{C}_{3}^{+} / \mathrm{HCO}^{+} / \mathrm{H}$, b) $\left.\mathrm{H}_{3} \mathrm{C}_{3}^{+} / \mathrm{H}^{+} / \mathrm{CO}, \mathrm{c}\right) \mathrm{H}_{2} \mathrm{C}_{3}^{+} / \mathrm{H}^{+} / \mathrm{CO} / \mathrm{H}$ d) $\mathrm{HC}_{3}^{+} / \mathrm{H}^{+} / \mathrm{CO} / \mathrm{H}_{2}$. Borders of bars represent when, for different energies, on average either $\mathrm{H}, \mathrm{H}^{+}, \mathrm{H}_{2}$ loss or fragmentation take place. Inset plots show abundance of different processes.

More insight into three- and four-body fragmentation processes can be obtained by investigation of the order of occurring events as the trajectory progresses. Results of such analysis are presented in Figure 5.36. From panel a) it can be noticed that in majority of trajectories producing channel $\mathrm{H}_{2} \mathrm{C}_{3}^{+} / \mathrm{HCO}^{+} / \mathrm{H}$ hydrogen loss is followed by fragmentation. Hydrogen atom is ejected around 10-30 fs and the time interval for fragmentation decreases with increasing energy. Moreover, analysis of the sequence of events of channel $\mathrm{H}_{3} \mathrm{C}_{3}^{+} / \mathrm{H}^{+} / \mathrm{CO}$ (panel b)) indicates clearly that $\mathrm{H}^{+}$loss takes place from $\mathrm{H}_{4} \mathrm{C}_{4} \mathrm{O}^{++}$and subsequently singly charged $\mathrm{H}_{3} \mathrm{C}_{4} \mathrm{O}^{+}$decomposes to $\mathrm{H}_{3} \mathrm{C}_{3}^{+} / \mathrm{CO}$. As it is shown in Figure 5.36 c), the most frequent sequence of events in channel $\mathrm{H}_{2} \mathrm{C}_{3}^{+} / \mathrm{H}^{+} / \mathrm{CO} / \mathrm{H}$ is $\mathrm{H}^{+} / \mathrm{H}$ loss $\rightarrow$ fragmentation. Interestingly, the increase of the internal energy does not affect when the first step of fragmentation takes place, which, on average, occurs at 9 fs . There is no way of differentiating whether $\mathrm{H}^{+}$or H is lost primarily based on the result of the dynamical simulations. Panel d) details two most populated sequences of events in channel $\mathrm{HC}_{3}^{+} / \mathrm{H}^{+} / \mathrm{CO} / \mathrm{H}_{2}: \mathrm{H}^{+}$loss $\rightarrow \mathrm{H}_{2}$ loss $\rightarrow$ fragmentation and $\mathrm{H}^{+}$loss $\rightarrow$ fragmentation $\rightarrow \mathrm{H}_{2}$ loss without evident distinction which process is more favourable. Further insight into production of these channels is necessary through exploration of the PES.

### 5.3.2 Potential Energy Surface

Following the analysis of the dynamical simulations, stability and mechanistic properties are investigated by exploration of the Potential Energy Surface. Figure 5.37 summarizes calculated pathways and groups them in types of observed process. This scheme demonstrates the most significant channels obtained in the MD, as well as additional plausible channels of two-body fragmentation. Optimized critical points on the fragmentation pathways of furan dication are presented in Figures 5.38-5.47. Energies, calculated at B3LYP/6-311++G(d,p) level of theory, are given in eV relative to neutral furan. ZPE corrections are included. For the reasons of clarity, complete pathways are shown even though some parts are duplicated in multiple figures (such as ts3 $\rightarrow$ ts6 in Figures 5.38-5.40 and 5.42).


FIGURE 5.37 Calculated fragmentation pathways of furan dication.

Firstly, isomerization of the furan dication and subsequent decomposition to two fragments is illustrated in Figures 5.38-5.41. As it was previously pointed out, the only channel of skeleton fragmentation observed in the molecular dynamics with prominent probability was $\mathrm{H}_{3} \mathrm{C}_{3}^{+} / \mathrm{HCO}^{+}$. The lowest energy pathway leading to production of c- $\mathrm{H}_{3} \mathrm{C}_{3}^{+}$and $\mathrm{HCO}^{+}(27.09$ eV ) implies ring opening by $\mathrm{C}-\mathrm{O}$ bond cleavage and rotation around $\mathrm{C}_{\alpha}-\mathrm{C}_{\beta}$ bond ( $\mathbf{t s} \mathbf{1} \rightarrow \mathbf{t s} \mathbf{2}$ ). Propargyl cation, linear isomer of $\mathrm{H}_{3} \mathrm{C}_{3}^{+}$, can be obtained through $2,1 \mathrm{H}$ transfer or $3,2 \mathrm{H}$ transfer on the furan ring and subsequent $\mathrm{C}-\mathrm{O}$ and $\mathrm{C}-\mathrm{C}$ bond cleavages. The highest points of these reaction pathways are transition structures corresponding to hydrogen migration, which are equal to 28.49 eV (ts3) and $28.83 \mathrm{eV}\left(\right.$ ts8 8 ), respectively. Finally, production of the $\mathrm{H}_{2} \mathrm{CCHC}{ }^{+}$ isomer is possible after $3,2 \mathrm{H}$ transfer, $2,1 \mathrm{H}$ transfer followed by $\mathrm{C}-\mathrm{O}$ and $\mathrm{C}-\mathrm{C}$ bond cleavages through an energy barrier of 28.83 eV . Hydrogen shift to the oxygen atom (ts17-28.88 eV) can also lead to channel $\mathrm{H}_{3} \mathrm{C}_{3}^{+} / \mathrm{HCO}^{+}$, however, it is less likely because of high energy barriers present in this mechanism. Moreover, exit channels obtained after hydrogen shift to oxygen are less stable. because produced fragment $\mathrm{HOC}^{+}$lies 1.60 eV higher in energy than formyl cation $\left(\mathrm{HCO}^{+}\right)$.


Figure 5.38 Potential Energy Surface for production of $\mathrm{H}_{3} \mathrm{C}_{3}^{+}$and $\mathrm{HCO}^{+}$through skeleton fragmentation. Panel a) shows pathways producing linear and cyclic isomers of $\mathrm{H}_{3} \mathrm{C}_{3}^{+}$. Panel $\mathbf{b}$ ) shows pathways producing $\mathrm{H}_{2} \mathrm{CCHC}^{+}$ isomer (left) and pathways following H migration to oxygen (right).


FIGURE 5.39 Potential Energy Surface for production of $\mathrm{H}_{2} \mathrm{C}_{2} \mathrm{O}^{+}$and $\mathrm{H}_{2} \mathrm{C}_{2}^{+}$through skeleton fragmentation.


Figure 5.40 Potential Energy Surface for production of $\mathrm{H}_{2} \mathrm{CO}^{+}$and $\mathrm{H}_{2} \mathrm{C}_{3}^{+}$through skeleton fragmentation. Panel a) shows pathways following $2,1 \mathrm{H}$ transfer. Panel $\mathbf{b}$ ) shows pathways following H migration to oxygen.

Figure 5.39 exhibits mechanisms of skeleton fragmentation producing $\mathrm{H}_{2} \mathrm{C}_{2} \mathrm{O}^{+}$and $\mathrm{H}_{2} \mathrm{C}_{2}^{+}$. The lowest energy pathway relies on ring opening concerted with $1,2 \mathrm{H}$ shift (ts23), $\mathrm{C}_{\beta}-\mathrm{C}_{\beta}$ bond cleavage (ts25-highest point 27.91 eV ) and temporary C-O rebonding (ts26). A higher energy pathway (by 0.58 eV ) proceeds through $2,1 \mathrm{H}$ shift, $\mathrm{C}-\mathrm{O}$ bond cleavage, formation of the $\mathrm{O}-\mathrm{C}_{\beta}$ bond and finally $\mathrm{C}_{\beta}-\mathrm{C}_{\beta}$ bond cleavage leading to fragmentation. Lastly, exit channel producing less stable isomer of $\mathrm{H}_{2} \mathrm{C}_{2}^{+}: \mathrm{H}_{2} \mathrm{CC}^{+}$is shown. This channel requires only one step from min13 of concerted $3,4 \mathrm{H}$ transfer and $\mathrm{C}_{\beta}-\mathrm{C}_{\beta}$ bond cleavage to reach fragmentation (ts28-28.44 eV).

Potential Energy Surface of the channel producing $\mathrm{H}_{2} \mathrm{CO}^{+}$and $\mathrm{H}_{2} \mathrm{C}_{3}^{+}$is presented in Figure 5.40. After initial 2,1 H transfer, which is also the highest step on the PES, two pathways are possible. Starting from min3, the system can either proceed through $\mathrm{C}_{\alpha}-\mathrm{C}_{\beta}$ and $\mathrm{C}-\mathrm{O}$ bond cleavage or $\mathrm{C}-\mathrm{O}$ bond cleavage and formation of a structure with cyclic $\mathrm{H}_{2} \mathrm{C}_{3}$ group (min19). The first mechanism implies barrier of $27.76 \mathrm{eV}(\mathbf{t s 3 5})$ and leads to formation of $\mathrm{HCCCH}^{+}$, whereas the highest point of second pathway is located at $27.45 \mathrm{eV}(\mathbf{t s} 32)$ and produces $\mathrm{c}-\mathrm{H}_{2} \mathrm{C}_{3}^{+}$. Pathway with a higher barrier ( 28.88 eV ) corresponds to formation of $\mathrm{H}_{2} \mathrm{CO}^{+} / \mathrm{H}_{2} \mathrm{C}_{3}^{+}$after H shift to oxygen presented in panel b). From min11 there are three options: (1) partial cyclization and $\mathrm{C}_{\alpha}-\mathrm{C}_{\beta}$ bond cleavage (ts37-28.26 eV) leading to $\mathrm{HCOH}^{+} / \mathrm{c}-\mathrm{H}_{2} \mathrm{C}_{3}^{+}$, (2) dihedral rotation around $\mathrm{C}_{\alpha}-\mathrm{C}_{\beta}$ bond, $2,1 \mathrm{H}$ transfer and $\mathrm{C}_{\alpha}-\mathrm{C}_{\beta}$ bond cleavage leading to $\mathrm{HCOH}^{+} / \mathrm{HCCCH}^{+}$ and (3) $2,1 \mathrm{H}$ transfer and $\mathrm{C}_{\alpha}-\mathrm{C}_{\beta}$ bond cleavage also leading to $\mathrm{HCOH}^{+} / \mathrm{HCCCH}^{+}$. The energy barriers of mentioned pathways are $28.36 \mathrm{eV}, 28.43 \mathrm{eV}$ and 28.49 eV , respectively.


Figure 5.41 Potential Energy Surface for production of $\mathrm{HC}_{2} \mathrm{O}^{+}$and $\mathrm{H}_{3} \mathrm{C}_{2}^{+}$through skeleton fragmentation.

Fourth possibility of skeleton fragmentation is demonstrated in Figure 5.41 and shows decomposition to $\mathrm{HC}_{2} \mathrm{O}^{+}$and $\mathrm{H}_{3} \mathrm{C}_{2}^{+}$. The most plausible fragmentation pathway follows initial $3,2 \mathrm{H}$ transfer (ts8-28.83 eV) by C-O bond cleavage, temporary $\mathrm{C}_{\alpha}-\mathrm{C}_{\beta}$ bond formation and C-O bond cleavage. This mechanism produces more stable, linear isomer of $\mathrm{HC}_{2} \mathrm{O}^{+}$. In a second mechanism, after min6 a $2,1 \mathrm{H}$ transfer and subsequent $\mathrm{C}-\mathrm{O}$ and $\mathrm{C}_{\beta}-\mathrm{C}_{\beta}$ bond cleavages take
place, leading to production of the cyclic isomer of $\mathrm{HC}_{2} \mathrm{O}^{+}$that is less stable by 1.10 eV than the linear isomer of $\mathrm{HC}_{2} \mathrm{O}^{+}$.


Figure 5.42 Potential Energy Surface for channels $\mathrm{H}_{2} \mathrm{C}_{3} \mathrm{O}^{+} / \mathrm{H}_{2} \mathrm{C}^{+}$and $\mathrm{H}_{3} \mathrm{C}_{2} \mathrm{O}^{+} / \mathrm{HC}_{2}^{+}$through skeleton fragmentation.

Last PES of skeleton fragmentation (Figure 5.42) shows production of two channels: $\mathrm{H}_{2} \mathrm{C}_{3} \mathrm{O}^{+} / \mathrm{H}_{2} \mathrm{C}^{+}$ (right) and $\mathrm{H}_{3} \mathrm{C}_{2} \mathrm{O}^{+} / \mathrm{HC}_{2}^{+}$(left). The lowest energy pathway leading to channel $\mathrm{H}_{2} \mathrm{C}_{3} \mathrm{O}^{+} / \mathrm{H}_{2} \mathrm{C}^{+}$ relies on $\mathrm{C}_{\alpha}-\mathrm{C}_{\beta}$ bond cleavage of min16 and overcoming an energy barrier of 29.38 eV . This mechanism leads also to the most stable isomer of $\mathrm{H}_{2} \mathrm{C}_{3} \mathrm{O}^{+}$. Secondly, a higher energy barrier was found ( $\mathbf{t s 4 5}-29.40 \mathrm{eV}$ ) for production of $\mathrm{H}_{2} \mathrm{C}_{3} \mathrm{O}^{+}$in a cyclic, less stable form. The only calculated pathway producing $\mathrm{H}_{3} \mathrm{C}_{2} \mathrm{O}^{+}$and $\mathrm{HC}_{2}^{+}$proceeds through $3,2 \mathrm{H}$ transfer, concerted $\mathrm{C}_{\beta}-\mathrm{C}_{\beta}$ bond cleavage and $1,2 \mathrm{H}$ shift and finally C-O bond cleavage. The highest point of this pathway is located at 30.58 eV (ts48), making it unlikely to occur.

ts63 $\rightarrow$ ts54). In the panel $\mathbf{b}$ ) of Figure 5.43 , PES corresponding to H loss from isomers of furan dication is shown. It can be noticed that $\mathrm{H}_{\beta}$ loss from $\min 2$ proceeds through a barrier of 31.43 eV and if followed by $\mathrm{C}_{\alpha}-\mathrm{C}_{\beta}$ bond cleavage ( $\mathrm{ts} 70-31.87 \mathrm{eV}$ ) leads to production of channel c- $\mathrm{H}_{2} \mathrm{C}_{3}^{+} / \mathrm{HCO}^{+} / \mathrm{H}$. The same channel might be produced through a barrierless $\mathrm{H}_{\alpha}$ loss from min40 and subsequent $\mathrm{C}_{\alpha}-\mathrm{C}_{\beta}$ bond fission. This reaction implies a barrier of 32.27 eV . In comparison with H loss directly from furan dication, H loss from isomeric structures requires more energy.


Figure 5.44 Potential Energy Surface for production of $\mathrm{HC}_{3}^{+}$and $\mathrm{HCO}^{+}$after two H loss.


FIgURE 5.45 Potential Energy Surface for production of $\mathrm{H}_{3} \mathrm{C}_{3}^{+}$and CO after $\mathrm{H}^{+}$loss directly from furan dication.

If enough energy is deposited into the system, loss of two atomic hydrogens might take place. In this respect, the MD simulations showed minor occurrence of channel producing $\mathrm{HC}_{3}^{+}, \mathrm{HCO}^{+}$and 2 H . Moreover, H loss proved to be the first step of the decomposition process. Figure 5.44 presents fragmentation pathways after two barrierless H losses, occurring directly from furan dication. The examined positions of hydrogens loss were: two $\mathrm{H}_{\beta}$ ( $\min 48$ 35.98 eV ), opposite $\mathrm{H}_{\alpha}$ and $\mathrm{H}_{\beta}(\min 42-36.03 \mathrm{eV})$, and adjacent $\mathrm{H}_{\alpha}$ and $\mathrm{H}_{\beta}(\boldsymbol{m i n} 50-37.16 \mathrm{eV})$. The lowest energy pathway consists of ejection of hydrogens from two $\beta$ positions and onestep ring opening leading to fragmentation (ts83-36.26 eV). An energy barrier higher only by 0.04 eV was calculated for an opposite $\mathrm{H}_{\alpha}$ and $\mathrm{H}_{\beta}$ loss followed by $\mathrm{C}_{\alpha}-\mathrm{C}_{\beta}$ bond fission and ring reorganization (ts75-36.30 eV). Three other pathways were obtained for min42 decomposition, but they present higher barriers than the one mentioned before. Two of those mechanism lead to production of less stable isomer of $\mathrm{HC}_{3}^{+}$through energy barriers of 36.53 eV (ts80) and 37.00 eV (ts81). In the case of adjacent $\mathrm{H}_{\alpha}$ and $\mathrm{H}_{\beta}$ loss, the multiple-step ring rupture implies the highest energy barrier of 37.49 eV (ts87).

A significant process observed in the MD consisted of deprotonation. When charge is localized on ejected hydrogen ion and the rest of the molecule remains singly ionized, possible skeleton fragmentation follows mechanisms described in the previous section of furan cation PES 5.2.2. However, contrary to H loss, $\mathrm{H}^{+}$loss is not a barrierless process. From Figure 5.45 it can be seen that loss of $\mathrm{H}_{\alpha}^{+}$and $\mathrm{H}_{\beta}^{+}$exhibit barriers of 30.14 eV (ts84) and 30.28 eV (ts74), respectively. These transition structures are the highest points on the pathways leading to fragmentation, indicating that the remaining singly ionized system will easily decompose to channel $\mathrm{H}_{3} \mathrm{C}_{3}^{+} / \mathrm{H}^{+} / \mathrm{CO}$.


Figure 5.46 Potential Energy Surface for $\mathrm{H}^{+}$and H loss. Panel a) shows pathways of $\mathrm{H}^{+}$loss followed by the loss of H . Panel $\mathbf{b}$ ) shows pathways of H loss followed by the loss of $\mathrm{H}^{+}$.

Sequential loss of H and $\mathrm{H}^{+}$was also observed in the dynamical simulations. As charge distribution is only established at the end of the calculation, there is no way of concluding whether H or $\mathrm{H}^{+}$has been ejected first. However, optimization of critical structures can provide information about the preferable order of the $\mathrm{H} / \mathrm{H}^{+}$loss. Energy profiles of this process have been investigated and are presented in Figure 5.46. It can be noticed that reaching exit channel $\mathrm{H}_{2} \mathrm{C}_{4} \mathrm{O}^{+} / \mathrm{H}^{+} / \mathrm{H}$ requires around 33 eV of energy in the case of $\mathrm{H}^{+} \rightarrow \mathrm{H}$ loss and more than 35 eV in the case of $\mathrm{H} \rightarrow \mathrm{H}^{+}$loss.


Figure 5.47 Potential Energy Surface for production of $\mathrm{H}_{2} \mathrm{C}_{3}^{+}$and CO after sequential $\mathrm{H}^{+}$and H loss.

Finally, the process of consecutive H and $\mathrm{H}^{+}$loss can be followed by fragmentation. Again, decomposition of singly ionized $\mathrm{H}_{2} \mathrm{C}_{4} \mathrm{O}^{+}$has been previously explored in section 5.2.2. As presented in Figure 5.47, the lowest energy pathway proceeds through a barrier of 33.39 eV and consists of $\mathrm{H}_{\beta} \rightarrow \mathrm{H}_{\beta}^{+}$loss from the furan dication ring and $\mathrm{C}-\mathrm{O}$ and $\mathrm{C}_{\alpha}-\mathrm{C}_{\beta}$ bond cleavages.

In summary, altogether 66 fragmentation pathways have been studied. Table 5.6 summarizes the highest points on the lowest energy pathways associated with activation energy producing specific exit channels. In order to maintain the information about the width of the barriers, the table includes also the number of transition states comprising the reaction pathway.

TABLE 5.6 Summary of the exploration of the Potential Energy Surface of furan dication.

| Exit Channel | Lowest <br> energy <br> barrier <br> [eV] | Corresponding <br> TS | Number of TS | Exit energy [eV] |
| :--- | :--- | :--- | :---: | :---: |
| $\mathrm{HCO}^{+} / \mathrm{H}_{3} \mathrm{C}_{3}^{+}$ | 27.09 | ts2 | 2 |  |
| $\mathrm{H}_{2} \mathrm{C}_{2} \mathrm{O}^{+} / \mathrm{H}_{2} \mathrm{C}_{2}^{+}$ | 28.49 | ts3 | 3 | $20.05\left(\mathrm{c}-\mathrm{H}_{3} \mathrm{C}_{3}^{+}\right)$ |
| $\mathrm{H}_{2} \mathrm{CO}^{+} / \mathrm{H}_{2} \mathrm{C}_{3}^{+}$ | 27.91 | ts25 | 4 | $21.08\left(1-\mathrm{H}_{3} \mathrm{C}_{3}^{+}\right)$ |
| $\mathrm{HC}_{2} \mathrm{O}^{+} / \mathrm{H}_{3} \mathrm{C}_{2}^{+}$ | 28.49 | ts3 | 42.78 |  |
| $\mathrm{H}_{2} \mathrm{C}_{3} \mathrm{O}^{+} / \mathrm{H}_{2} \mathrm{C}^{+}$ | 29.33 | ts8 | ts47 | 5 |
| $\mathrm{H}_{3} \mathrm{C}_{2} \mathrm{O}^{+} / \mathrm{HC}_{2}^{+}$ | 30.58 | ts48 | 4 | $24.00\left(\mathrm{c}-\mathrm{H}_{2} \mathrm{C}_{3}^{+}\right)$ |
| $\mathrm{HCO}^{+} / \mathrm{H}_{2} \mathrm{C}_{3}^{+} / \mathrm{H}$ | 31.08 | ts53 | $4.08\left(1-\mathrm{H}_{2} \mathrm{C}_{3}^{+}\right)$ |  |
| $\mathrm{HCO}^{+} / \mathrm{HC}_{3}^{+} / 2 \mathrm{H}$ | 31.72 | ts58 | 3.13 | ts74 |
| $\mathrm{H}_{3} \mathrm{C}_{3}^{+} / \mathrm{H}^{+} / \mathrm{CO}$ | 30.14 | ts84 | 2 | 24.43 |
| $\mathrm{H}_{2} \mathrm{C}_{3}^{+} / \mathrm{H}^{+} / \mathrm{CO} / \mathrm{H}$ | 33.39 | ts92 | 2 | 25.09 |

### 5.3.3 Comparison with ion collision experiment

Coincidence time-of-flight (TOF) mass spectrometry has been employed to study the interaction of $46 \mathrm{keV} \mathrm{O}^{6+}$ ions with neutral furan. The experiment has been performed at ARIBE, the low-energy ion beam facility of GANIL in Caen, France. Detailed description of the experimental setup can be found in [100]. In this experiment, mechanism of the double ionization of the target relies on the capture of two valence electrons in a single ion-molecule collision. Subsequently, excess energy deposited into the system induces unimolecular decomposition. Figures 5.48-5.50 depict 2D histograms of the recorded ion pairs, in which the flight time of the slower ion (TOF 2 ) is plotted as a function of the flight time of the faster ion (TOF 1). After false coincidences (giving $m_{1} / q_{1}+m_{2} / q_{2}>68$ ) subtracted out, the experiment recorded over 45000 events altogether. Quantum chemistry calculations, such as AIMD and exploration of PES, can help to elucidate evolution of the system upon collision, as well as suggest transient steps of reaching final fragmentation products.

Geometrical parameters of the measured correlation islands, such as shape, size and orientation, can be indicative of the mechanism of a specific dissociation channel. The dynamics of the fragmentation reactions have been discussed in [101] by means of the laws of energy and momentum conservation. Slopes of the correlation islands point out to the momenta of measured fragments and, hence, can provide information on the sequence of events. Firstly, two-body fragmentation produces an island of a narrow bar shape and slope of -1 . Among the three-body fragmentation channels, producing two charged ( $A^{+}$and $B^{+}$, where $m_{A}<m_{B}$ ) and one neutral fragment $(C)$, three processes can be differentiated:
deferred charge separation corresponding to reaction
$A B^{2+} \longrightarrow A B^{2+}+C \longrightarrow A^{+}+B^{+}+C$
consists of ejection of neutral species from the parent ion followed by fragmentation of doubly ionized intermediate. The peak shape of this mechanism is a lozenge of slope -1 . The peak's ends present a slope of $m_{B} / m_{A}$ caused by a random momentum component associated with rotation of $A B^{2+}$ to a random angle following ejection of $C$, but ahead of fragmentation. Additional evidence of this mechanism is the observation of an $A B^{2+}$ peak in the mass spectrum.
secondary decay of primary fragments corresponding to reaction
$A \mathrm{BC}^{2+} \longrightarrow A C^{+}+B^{+} \longrightarrow A^{+}+C+B^{+}$
implies charge separation first and subsequent decay of the singly ionized species, taking place outside of the Coulomb zone. The resulting peak shape is a bar of slope $-\left(m_{A}+\right.$ $\left.m_{C}\right) / m_{A}$ with horizontal ends. In this case, the deviation from -1 slope is associated with fragment $C$ carrying some of the initial momentum of the intermediate $A C^{+}$. Hence, the width of the bar points out to the energy release in the secondary decay.
fast concerted dissociation corresponding to reaction

$$
A B C^{2+} \longrightarrow A^{+}+B^{+}+C
$$

results in a complex peaks shape. This mechanism relies on the simultaneous three-body dissociation, where, if present, an intermediate has no time to rotate ahead of fragmentation. The shape of the coincidence island can indicate the angle of ejection of fragment $C$ relative to the line connecting $A^{+}$and $B^{+}$. If this emission is close to perpendicular, an ovoid shape can be observed. Conversely, loss of $C$ in a parallel direction produces a fan-shaped peak. In the case of concerted processes the peak slope are impossible to interpret due to variety of possible combinations of vector magnitude and orientation.

From the ion-ion TOF plot presented in Figure 5.48 four of the most significant correlation islands are identified. Each pattern has been assigned to a specific charged fragments pair and its measured relative intensity (RI) has been compared with calculated relative energy of the lowest-energy pathways in Table 5.7. With $17.06 \%$ of all counts, the major correlation island is clearly ion pair $29^{+} / 39^{+}$, corresponding to $\mathrm{HCO}^{+} / \mathrm{H}_{3} \mathrm{C}_{3}^{+}$channel of skeleton fragmentation. As concluded from the MD simulations, this channel dominates in the range of internal energy between 5 and 13 eV . Moreover, exploration of the PES indicated that production of ions $\mathrm{HCO}^{+}$ and $\mathrm{H}_{3} \mathrm{C}_{3}^{+}$proceeds through the lowest energy barrier for furan dication decomposition. Both observations prompted a conclusion that fragmentation of furan dication induced by collisions with ions is dominated by the ring breakup. Furthermore, the experimental results point out to another, minor channel of two-body decomposition, ion pair $\mathbf{2 6}^{+} / \mathbf{4 2}{ }^{+}$, corresponding to fragments $\mathrm{H}_{2} \mathrm{C}_{2}^{+} / \mathrm{H}_{2} \mathrm{C}_{2} \mathrm{O}^{+}$. The activation barrier for this process equals to 27.91 eV , which is only 0.82 eV higher than the barrier for channel $\mathrm{HCO}^{+} / \mathrm{H}_{3} \mathrm{C}_{3}^{+}$. However, such low intensity of island $\mathbf{2 6}^{+} / \mathbf{4 2} \mathbf{2}^{+}$can be explained by the multiple steps of isomerization required ahead of the fragmentation. Supporting of this conclusion are also results of the MD calculations, in which only 21 out of all 3900 trajectories finished in fragmentation to channel $\mathrm{H}_{2} \mathrm{C}_{2}^{+} / \mathrm{H}_{2} \mathrm{C}_{2} \mathrm{O}^{+}$.


FIGURE 5.48 Coincidence map for the fragmentation of furan in collision with $46 \mathrm{keV} \mathrm{O}^{6+}$ ions. The most abundant coincidence islands are assigned to respective ion masses according to the formula: $T O F \propto \sqrt{\frac{m}{q}}$.

TABLE 5.7 Major coincidence islands are identified, assigned to respective fragmentation channels and compared with calculated energy barriers. Relative Intensities indicates total number of events in a square of side 1 amu centered on the respective TOF values, relative to all measured events and given in $\%$.

| Exit Channel | Ion pair <br> $\mathbf{m} / \mathbf{z}$ | Relative <br> Intensity [\%] | Lowest energy <br> barrier $[\mathbf{e V}]$ | Corresponding <br> TS |
| :--- | :--- | :--- | :---: | :---: |
| $\mathrm{HCO}^{+} / \mathrm{H}_{3} \mathrm{C}_{3}^{+}$ | $\mathbf{2 9}^{+} / 3 \mathbf{9}^{+}$ | 17.06 | 27.09 | ts2 |
| $\mathrm{H}_{2} \mathrm{C}_{2}^{+} / \mathrm{H}_{2} \mathrm{C}_{2} \mathrm{O}^{+}$ | $\mathbf{2 6}^{+} / \mathbf{4 \mathbf { 2 } ^ { + }}$ | 0.98 | 27.91 | ts25 |
| $\mathrm{HCO}^{+} / \mathrm{H}_{2} \mathrm{C}_{3}^{+} / \mathrm{H}$ | $\mathbf{2 9}^{+} / 3 \mathbf{8}^{+}$ | 14.60 | 31.08 | ts53 |
| $\mathrm{HCO}^{+} / \mathrm{HC}_{3}^{+} / 2 \mathrm{H}$ | $\mathbf{2 9}^{+} / 37^{+}$ | 6.17 | 36.13 | ts 74 |
| $\mathrm{H}_{3} \mathrm{C}_{3}^{+} / \mathrm{H}^{+} / \mathrm{CO}$ | $\mathbf{1}^{+} / \mathbf{3 9 ^ { + }}$ | 1.01 | 30.14 | ts84 |
| $\mathrm{H}_{2} \mathrm{C}_{3}^{+} / \mathrm{H}^{+} / \mathrm{CO} / \mathrm{H}$ | $\mathbf{1}^{+} / 3 \mathbf{3 8}^{+}$ | 0.61 | 33.39 | ts92 |

Islands of the second and the third highest intensities are related to loss of neutral hydrogen, either single: ion pair $29^{+} / 38^{+}$or double: ion pair $\mathbf{2 9}^{+} / 37^{+}$. These channels have also been identified by the MD simulations as following in frequency after channel $\mathrm{HCO}^{+} / \mathrm{H}_{3} \mathrm{C}_{3}^{+}$ for the middle energies considered. Total measured RI of ion pair $29^{+} / 38^{+}$is high and equals to $14.60 \%$. The MD simulations indicated that the loss of hydrogen mostly takes place directly from parent ion and charge separation follows. This conclusion can be verified by the consideration of island $29^{+} / 38^{+}$, which, indeed shows the slope of -1 . Total RI of measured coincidence island $29^{+} / 37^{+}$is $6.17 \%$. The dynamical simulations pointed out to the prevalence of double hydrogen atom loss rather than loss of hydrogen molecule. Moreover, it was found that this process occurs sequentially, directly from $\mathrm{H}_{4} \mathrm{C}_{4} \mathrm{O}^{2+}$.


FIgURe 5.49 Zoom on the coincidence map for fragmentation of furan in collision with $46 \mathrm{keV} \mathrm{O}^{6+}$ ions involving correlation islands of deprotonation.

Channels of deprotonation have also been recorded. Figure 5.49 shows two patterns of fragments measured in coincidence with $\mathrm{H}^{+}$: correlation island $\mathbf{1}^{+} / 39^{+}$(corresponding to $\mathrm{H}^{+} / \mathrm{H}_{3} \mathrm{C}_{3}^{+}$) and $\mathbf{1}^{+} / 38^{+}\left(\mathrm{H}^{+} / \mathrm{H}_{2} \mathrm{C}_{3}^{+}\right)$. Relative Intensities of these ion pars are $1.01 \%$ and $0.61 \%$, respectively, which are low but not negligible. The possible explanation of such low abundance of this process in the measured spectrum is the soft character of collisions with $\mathrm{O}^{6+}$ ions. Indeed, the MD simulations showed that deprotonation briefly dominates over other mechanisms in the high energy region of $22 \mathrm{eV}\left(\mathrm{H}_{3} \mathrm{C}_{3}^{+} / \mathrm{H}^{+} / \mathrm{CO}\right)$ and also $30 \mathrm{eV}\left(\mathrm{H}_{2} \mathrm{C}_{3}^{+} / \mathrm{H}^{+} / \mathrm{CO} / \mathrm{H}\right)$.


FIGURE 5.50 Coincidence map for fragmentation of furan in collision with $46 \mathrm{keV} \mathrm{O}^{6+}$ ions.

Finally, a long tail starting from the TOF values of ion pair $29^{+} / 39^{+}$and extending to the TOF values of the parent dication has been measured (highlighted by a blue box in Figure 5.50). This feature indicates slow charge separation associated with the production of metastable $\mathrm{H}_{4} \mathrm{C}_{4} \mathrm{O}^{2+}$. Indeed, PES of channel $\mathrm{HCO}^{+} / \mathrm{H}_{3} \mathrm{C}_{3}^{+}$demonstrates two transition structures and one minimum ahead of fragmentation, which correspond to ring breakup by rotation around $\mathrm{C}_{\alpha}-\mathrm{C}_{\beta}$ bond. Previous studies of lifetimes of metastable molecular doubly charged ions have been performed by Field and Eland [102]. In their work they provide a way of predicting mean lifetimes of metastable structures from the experimental mass spectra. However, more recently, the production of the metastable $\mathrm{CO}_{2}^{2+}$ has been investigated by Alagia et al [103]. Therein, it has been concluded that the mean lifetimes derived from obtained measurements are significantly influenced by the time observation window specific to each experiment and, hence, do not provide universal values.

The two areas of the metastable tail: "AR" and "DR" in Figure 5.50 a) point out to the delayed decay of the doubly charged ion taking place in different regions of the experimental setup. If the precursor dication undergoes fragmentation outside of the interaction volume, in the acceleration region, the measured TOFs fall into the area marked as "AR". The characteristic V shaped area "DR" comes from dissociation events occurring in the field-free drift region. Two arms of this shape should present slopes $m_{A} / m_{B}$ and $m_{B} / m_{A}$, which correspond to 0.74 and 1.35 for the ion pair $\mathbf{2 9}^{+} / 39^{+}$, respectively. Their lengths are associated with the kinetic energy release of the dissociation. Measured slopes are equal to 0.76 and 1.29 , indicating that indeed metastable $\mathrm{H}_{4} \mathrm{C}_{4} \mathrm{O}^{2+}$ produces the ion pair $29^{+} / 39^{+}$.

In conclusion, the complementary approach of two theoretical methods proved effective in the interpretation of the mechanism of the interaction of $\mathrm{O}^{6+}$ ions with the neutral furan. Direct ring fission, H and $\mathrm{H}^{+}$loss and deferred fragmentation have been experimentally observed and were supported by the theoretical results.

## Chapter 6

## Summary and perspective

The approach presented in this thesis combined three theoretical methodologies, allowing for a complete overview of the fragmentation process. Firstly, I performed molecular dynamics calculations, which provided details on the evolution of the system after deposition of various amounts energy. Consequently, a statistical analysis of the occurring mechanisms indicated the most prominent channels of fragmentation as a function of the internal energy. Secondly, I explored the potential energy surface considering the fragmentation mechanism and energetic dependence of the probable reaction pathways in a static manner. Finally, I employed a new statistical method based on the maximum entropy assumption, which provided breakdown curves with a substantially lower computational cost compared to the molecular dynamics simulations.

Although MD is the most computationally expensive approach, it complements the investigation of fragmentation processes with intermediate steps that might be difficult to determine only based on the chemical intuition. Another advantage of performing the MD simulations is the possibility of systematic investigation in a wide energy range. The same benefit characterizes the $\mathrm{M}_{3} \mathrm{C}$ method, with the additional advantage of a lower computational cost. Moreover, ab initio MD calculations are limited by the choice of the total simulation time. Instead, the ergodic hypothesis of the statistical $\mathrm{M}_{3} \mathrm{C}$ method replaces the consideration of time with the consideration of space and, consequently, provides the results as if the system had infinite time to evolve.

A drawback of the $\mathrm{M}_{3} \mathrm{C}$ approach remains in the approximation of sudden fragmentation and disregard of the transition states constituting a reaction pathway. In my thesis the solution to this problem relied on a manual introduction of energy barriers previously determined by quantum chemistry calculations, a step that was rather time consuming. Alternatively, further developments of the $\mathrm{M}_{3} \mathrm{C}$ program should focus on the search for less demanding procedures. Moreover, future $\mathrm{M}_{3} \mathrm{C}$ applications will extend to multiply charged molecules, in which Coulomb explosion processes compete with mechanisms of decomposition to one, multiply charged and few neutral fragments. In such case energy barriers may play an even more significant role in the mechanism of fragmentation. As the main goal of the $\mathrm{M}_{3} \mathrm{C}$ method is providing a general tool that can be applicable to a wide range of systems, additional improvements are necessary and I plan to continue with efforts in this direction.

As for the obtained results, I focused on the investigation of the fragmentation mechanism of the furan molecule in three charge states. It has been shown that preceding ionization of the molecule leads to divergent fragmentation patterns. Apart from evident production of ionized
species, the most prevalent products differed in composition. Dynamics of the fragmentation of the neutral furan is dominated by channels $\mathrm{HCCH}+\mathrm{H}_{2} \mathrm{CCO}$ and $\mathrm{CO}+\mathrm{H}_{2} \mathrm{CCCH}_{2}$ for lower energies and by $\mathrm{H}_{2}+\mathrm{CO}+\mathrm{HCCCH}$ for higher energies. On the other hand, the most abundant channels in the case of singly ionized furan were $\mathrm{c}-\mathrm{H}_{3} \mathrm{C}_{3}{ }^{+}+\mathrm{HCO}$ for lower energies and $\mathrm{c}-\mathrm{H}_{3} \mathrm{C}_{3}{ }^{+}+\mathrm{CO}+\mathrm{H}$ and $\mathrm{HCCCH}^{+}+\mathrm{CO}+2 \mathrm{H}$ for higher energies. Similarly to the furan cation, furan dication fragments to $\mathrm{c}-\mathrm{H}_{3} \mathrm{C}_{3}^{+}+\mathrm{HCO}^{+}$and $\mathrm{c}-\mathrm{H}_{3} \mathrm{C}_{3}{ }^{+}+\mathrm{CO}+\mathrm{H}^{+}$with the highest probability. The frequency of trajectories finishing with an isomer of furan decreased when the molecule is ionized. All three cases of charge states showed that at low energies, if at all, isomerization takes place late in the dynamics. Hence, provided longer simulation times the system could potentially undergo fragmentation. The mechanism of skeleton fragmentation differs with ionization as well. Decomposition in the neutral case requires prior hydrogen transfer. Fragmentation of singly ionized furan relies only on the ring cleavage and formation of a metastable complex. Then again, skeleton fragmentation of furan dication proceeds through C-O bond scission and rotation around $\mathrm{C}_{\alpha}-\mathrm{C}_{\beta}$ bond. Finally, H and $\mathrm{H}_{2}$ loss processes were extensively studied due to their abundant occurrence at higher energies.

Theoretical predictions presented in my dissertation were compared with previously published studies, as well as with results of recently performed experiments. Consequently, novel theoretical methodology could be verified and employed to support the interpretation of the measured data. Investigation of the neutral furan decomposition showed channels and mechanisms of skeleton fragmentation in accordance with previous works. A new insight relied on demonstration of multifragmentation processes. As for the furan cation, a direct comparison between theory and experiment was possible owing to the new PEPICO measurements. I concluded that theoretical breakdown curves mostly maintain the shape of experimental curves. Moreover, analogies between measured Appearance Energies and calculated energy barriers for certain pathways confirmed the most likely mechanisms of decomposition. Another important outcome of my work relied on the determination of the energy transfer function based on the comparison between reproduced theoretical and measured mass spectra. Finally, coincidence measurements of ionic fragments produced by ion-furan collisions allowed for qualitative comparison and first elucidation of the furan dication decomposition mechanism. Moreover, an explanation for the observation of the metastable furan dication, with a lifetime larger than the time needed by the molecule to reach the detector, was proposed.

As a way of complementing the present work, further studies on the furan fragmentation processes could deal with the excited state behaviour and non-adiabatic effects - essential aspects of electron transfer processes, heterolytic dissociation and many recombination reactions [104]. Such features as the excited state lifetime and deactivating pathways may differ significantly from the properties of thermally activated systems. Therefore, a detailed analysis of the excited state dynamics with methods like Time-dependent Density Functional Theory [105] or trajectory surface hopping [106] might provide some valuable, new information. Moreover, several recent studies [107], [108] focused on the fragmentation of fullerenes and Polycyclic Aromatic Hydrocarbons induced by low energy collisions with heavy particles and displayed
evidence of non-statistical fragmentation. In this mechanism, the excess energy is not redistributed over internal degrees of freedom, but rather single atoms are knocked out few femtoseconds after the collision. Such processes have not been investigated in the present work, however, due to significantly smaller size of the target molecule, non-statistical fragmentation is expected to play a minor role in the decomposition of furan.

## Appendix A

## $\mathrm{M}_{3} \mathrm{C}$ fragments database

This appendix presents the collection of possible fragments, which were taken as the input database for the $\mathrm{M}_{3} \mathrm{C}$ calculations of furan. Molecules are sorted by the increasing number of atoms. The .rxyz files containing the electronic energy, geometry in an xyz format, vibrational frequencies, symmetry of the wave function and molecular symmetry of every molecule presented here are available at an open-access repository [109]. The naming of the molecules corresponds to the following scheme: <stoichiometry>.q<charge>.m<multiplicity>-<id>.




| $\mathrm{H}_{2}$ |  |
| :---: | :---: |
|  |  |
|  |  |
| $\substack{\text { H2.q0.m1-2 } \\ \text { 1-SGG (D*H) }}$ | H2.q1.m2-1 <br> 2-SGG (D*H) |




| $\mathrm{H}_{2} \mathrm{C}$ |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: |


| $\mathrm{H}_{2} \mathrm{O}$ |  |  |
| :---: | :---: | :---: |
|  |  |  |




| $\mathrm{C}_{2} \mathrm{O}$ |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: |
|  |  | ! |  | $\xi$ |
| $\begin{gathered} 1 \\ \text { C20.q0.m1-2 } \\ \text { 1-SG (C C*V } \end{gathered}$ | $\begin{gathered} 2 \\ \begin{array}{c} 2 \\ \text { C2O.q0.m1-3 } \\ \text { 1-A1 (C2V) } \end{array} \end{gathered}$ | $\begin{gathered} 3 \\ \substack{3 \\ \text { C2O.q0.m3-2 } \\ 3-\mathrm{SG}\left(\mathrm{C}^{*} \mathrm{~V}\right)} \end{gathered}$ | $\begin{gathered} 4 \\ \mathrm{C}_{\mathrm{CO} \cdot \mathrm{q} 1 . \mathrm{m} 2-1}^{2-\mathrm{PI}\left(\mathrm{C}^{*} \mathrm{~V}\right)} \end{gathered}$ |  |


| $\mathrm{H}_{3} \mathrm{C}$ |  |  |
| :---: | :---: | :---: |



| $\mathrm{H}_{2} \mathrm{CO}$ |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  |  |  |  |
|  |  |  |  |  |  |


| $\mathrm{HC}_{3}$ |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  | $\&$ | $\$$ |  |  | $\}$ |
| $\underset{\substack{\mathrm{HC} .900 . \mathrm{m}-1 \\ 2-\mathrm{A}(\mathrm{CS})}}{1}$ | $\underset{\substack{\mathrm{HCc.a0} 0 \mathrm{~m} 2-2 \\ 2 \cdot \mathrm{B2}(\mathrm{C2V})}}{2}$ | $\underset{\substack{\text { HC3.q.a.m-16 } \\ 4.5 G(C \cdot v)}}{3}$ | $\underset{\substack{\mathrm{HC} 3.90 . m 418 \\ 4 \cdot \mathrm{~A}^{\prime}(\mathrm{CS})}}{4}$ | $\underset{\substack{\text { HC.an1.m-1 } \\ 1-\mathrm{Al} 1(\mathrm{CV})}}{5}$ | $\underset{\substack{\text { HC.an1.m-2 } \\ 1-\mathrm{Al}(\mathrm{CVV})}}{6}$ |
| \$ | $\$$ | $\&$ |  |  |  |
|  |  |  |  |  |  |


| $\mathrm{HC}_{2} \mathrm{O}$ |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  | $\begin{gathered} 2 \\ \text { HC2O.q0.m2-5 } \\ \text { 2-A" (CS) } \end{gathered}$ | $\begin{gathered} 3 \\ \text { HC2O.q0.m4-6 } \\ 4-\mathrm{A} "(\mathrm{CS}) \end{gathered}$ | $\begin{gathered} 4 \\ \text { HC2O.q0.m4-8 } \\ \text { 4-A (C1) } \end{gathered}$ | $\begin{gathered} \text { HC2O.q0.m4-13 } \\ \text { 4-A" (CS) } \end{gathered}$ |  |
| $\begin{gathered} 7 \\ \text { HC2O.q0.m4-16 } \\ \text { 4-A" (CS) } \end{gathered}$ |  | $\begin{gathered} 9 \\ \mathrm{HC} 2 \mathrm{O} \cdot \mathrm{q} 1 . \mathrm{m} 1-2 \\ 1-\mathrm{A}^{\prime}(\mathrm{CS}) \end{gathered}$ |  | $\begin{gathered} 11 \\ \text { HC2O.q1.m1-4 } \\ \text { 1-A (C1) } \end{gathered}$ | $\begin{gathered} 12 \\ \text { HC2O.q1.m1-5 } \\ 1-\mathrm{A}^{\prime}(\mathrm{CS}) \end{gathered}$ |
|  | $\begin{gathered} 14 \\ \text { HC2O.q1.m3-2 } \\ \text { 3-A" (CS) } \end{gathered}$ |  |  |  |  |



| $\mathrm{C}_{3} \mathrm{O}$ |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
| $\begin{gathered} 1 \\ \text { C3O.q0.m1-3 } \\ 1-\mathrm{A}^{\prime}(\mathrm{CS}) \end{gathered}$ | $\begin{gathered} 2 \\ \text { C3O.q0.m1-4 } \\ \text { 1-SG }\left(\mathrm{C}^{*} \mathrm{~V}\right) \end{gathered}$ | $\begin{gathered} 3 \\ \text { C3O.q0.m1-5 } \\ \text { 1-SG }\left(\mathrm{C}^{*} \mathrm{~V}\right) \end{gathered}$ | $\begin{gathered} 4 \\ \text { C3O.q0.m3-1 } \\ 3-\mathrm{A}^{\prime}(\mathrm{CS}) \end{gathered}$ | $\begin{gathered} 5 \\ \text { C3O.q1.m2-2 } \\ \text { 2-SG }\left(\mathrm{C}^{*} \mathrm{~V}\right) \end{gathered}$ | $\begin{gathered} 6 \\ \text { C3O.q1.m2-3 } \\ \text { 2-SG }\left(\mathrm{C}^{*} \mathrm{~V}\right) \end{gathered}$ |
| $\begin{gathered} 7 \\ \text { C3O.q1.m2-4 } \\ \text { 2-A (C1) } \end{gathered}$ | $\begin{gathered} 8 \\ \text { C3O.q1.m4-4 } \\ \text { 4-A2 (C2V) } \end{gathered}$ | $\begin{gathered} 9 \\ \text { C3O.q1.m4-5 } \\ \text { 4-A (C1) } \end{gathered}$ |  |  |  |


| $\mathrm{H}_{4}$ |
| :---: |
| 0 |
| 0 |
| $0=0$ |
| 1 |
| H4.q1.m2-1 |
| 2-A1 (C2V) |


| $\mathrm{H}_{4} \mathrm{C}$ |  |
| :---: | :---: |
| 1 <br> H4C.90.m1-1 <br> 1-A1 (TD) | $\substack{\text { H4C.q1.m2-1 } \\ \text { 2-B2 (D2D) }}$ |



| $\mathrm{H}_{3} \mathrm{CO}$ |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: |
| $\begin{gathered} 1 \\ \text { H3CO.q0.m2-1 } \\ 2-\mathrm{A}^{\prime}(\mathrm{CS}) \end{gathered}$ | $\begin{gathered} 2 \\ \text { H3CO.q0.m2-2 } \\ \text { 2-A (C1) } \end{gathered}$ | $\begin{gathered} 3 \\ \text { H3CO.q1.m1-3 } \\ 1-\mathrm{A}^{\prime}(\mathrm{CS}) \end{gathered}$ | $\begin{gathered} 4 \\ \text { H3CO.q1.m3-2 } \\ \text { 3-A" (CS) } \end{gathered}$ | $\begin{gathered} 5 \\ \text { H3CO.q1.m3-8 } \\ \text { 3-A" (CS) } \end{gathered}$ |


| $\mathrm{H}_{2} \mathrm{C}_{3}$ |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
| $\begin{gathered} 1 \\ \text { H2C3.q0.m1-2 } \\ \text { 1-A1 (C2V) } \end{gathered}$ | $\begin{gathered} 2 \\ \text { H2C3.q0.m1-3 } \\ \text { 1-AG (C2H) } \end{gathered}$ | $\begin{gathered} 3 \\ \text { H2C3.q0.m1-4 } \\ \text { 1-A1 (C2V) } \end{gathered}$ | $\begin{gathered} 4 \\ \text { H2C3.q0.m1-5 } \\ \text { 1-A (C2) } \end{gathered}$ |  | $\begin{gathered} 6 \\ \text { H2C3.q0.m3-2 } \\ \text { 3-A" (CS) } \end{gathered}$ |
| $\begin{gathered} 7 \\ \text { H2C3.q0.m3-3 } \\ 3 \text {-A" (CS) } \end{gathered}$ | $\begin{gathered} 8 \\ \text { H2C3.q0.m3-4 } \\ \text { 3-B2 (C2V) } \end{gathered}$ | $\begin{gathered} 9 \\ \text { H2C3.q0.m3-5 } \\ \text { 3-A (C1) } \end{gathered}$ | 10 $\begin{gathered} \text { H2C3.q1.m2-1 } \\ \text { 2-PIG (D*H) } \end{gathered}$ | $\begin{gathered} 11 \\ \text { H2C3.q1.m2-2 } \\ \text { 2-A }{ }^{\prime}(\mathrm{CS}) \end{gathered}$ | $\begin{gathered} 12 \\ \text { H2C3.q1.m2-3 } \\ \text { 2-A1 (C2V) } \end{gathered}$ |
| 13 <br> H2C3.q1.m4-1 <br> 4-A2 (C2V) | 14 <br> H2C3.q1.m4-2 <br> 4-A (C1) | $\begin{gathered} 15 \\ \text { H2C3.q1.m4-4 } \\ \text { 4-A2 (C2V) } \end{gathered}$ |  |  |  |


| $\mathrm{H}_{2} \mathrm{C}_{2} \mathrm{O}$ |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
| $\begin{gathered} 1 \\ \text { H2C2O.q0.m1-4 } \\ \text { 1-A' (CS) } \end{gathered}$ | $\begin{gathered} 2 \\ \mathrm{H} 2 \mathrm{C} 2 \mathrm{O} . \mathrm{q} 0 . \mathrm{m} 1-5 \\ \text { 1-A1 (C2V) } \end{gathered}$ | $\begin{gathered} 3 \\ \text { H2C2O.q0.m1-6 } \\ \text { 1-A (C1) } \end{gathered}$ | $\begin{gathered} 4 \\ \text { H2C2O.q0.m1-7 } \\ \text { 1-A (C1) } \end{gathered}$ | $\begin{gathered} 5 \\ \text { H2C2O.q0.m3-5 } \\ 3-\mathrm{A}^{\prime \prime}(\mathrm{CS}) \end{gathered}$ | $\begin{gathered} { }^{6} \\ \text { H2C2O.q1.m2-2 } \\ \text { 2-A (C1) } \end{gathered}$ |
| $\begin{gathered} 7 \\ \text { H2C2O.q1.m2-3 } \\ \text { 2-A (C1) } \end{gathered}$ | $\begin{gathered} 8 \\ \mathrm{H} 2 \mathrm{C} 2 \mathrm{O} . \mathrm{q} 1 . \mathrm{m} 4-4 \\ \text { 4-A" (CS) } \end{gathered}$ | $\begin{gathered} 9 \\ \text { H2C2O.q1.m4-5 } \\ 4-\mathrm{A}^{\prime}(\mathrm{CS}) \end{gathered}$ | $\begin{gathered} 10 \\ \text { H2C2O.q1.m4-6 } \\ 4-\mathrm{A}^{\prime \prime}(\mathrm{CS}) \end{gathered}$ | $\begin{gathered} 11 \\ \text { H2C2O.q1.m4-8 } \\ 4-\mathrm{A}^{\prime \prime}(\mathrm{CS}) \end{gathered}$ |  |


| $\mathrm{HC}_{4}$ |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
| $\begin{gathered} 1 \\ \text { HC4.q0.m2-1 } \\ 2-\mathrm{A}^{\prime}(\mathrm{CS}) \end{gathered}$ | $\begin{gathered} 2 \\ \text { HC4.q0.m2-2 } \\ \text { 2-A (C1) } \end{gathered}$ | $\begin{gathered} 3 \\ \text { HC4.q0.m2-5 } \\ \text { 2-A } \mathrm{A}^{\prime}(\mathrm{CS}) \end{gathered}$ | $\begin{gathered} 4 \\ \text { HC4.q0.m2-6 } \\ \text { 2-B1 (C2V) } \end{gathered}$ | $\begin{gathered} 5 \\ \text { HC4.q0.m4-1 } \\ 4-\mathrm{A}(\mathrm{C} 1) \end{gathered}$ | $\begin{gathered} { }^{6} \\ \text { HC4.q0.m4-2 } \\ \text { 4-A" (CS) } \end{gathered}$ |
| $\begin{gathered} 7 \\ \text { HC4.q0.m4-3 } \\ 4-\mathrm{A}^{\prime}(\mathrm{CS}) \end{gathered}$ | $\begin{gathered} 8 \\ \text { HC4.q0.m4-4 } \\ \text { 4-A" (CS) } \end{gathered}$ | $\begin{gathered} 9 \\ \text { HC4.q0.m4-5 } \\ \text { 4-A" (CS) } \end{gathered}$ | $\begin{gathered} 10 \\ \text { HC4.q1.m1-1 } \\ \text { 1-A1 (C2V) } \end{gathered}$ | $\begin{gathered} 11 \\ \text { HC4.q1.m1-3 } \\ 1-\mathrm{A}^{\prime}(\mathrm{CS}) \end{gathered}$ | 12 <br> HC4.q1.m1-4 <br> 1-SG ( $\mathrm{C}^{*} \mathrm{~V}$ ) |
| $\begin{gathered} 13 \\ \text { HC4.q1.m1-5 } \\ \text { 1-A1 (C2V) } \end{gathered}$ | $\begin{gathered} 14 \\ \text { HC4.q1.m3-3 } \\ \text { 3-A" (CS) } \end{gathered}$ | 15 <br> HC4.q1.m3-4 <br> 3-A2 (C2V) | $\begin{gathered} 16 \\ \text { HC4.q1.m3-5 } \\ \text { 3-A" (CS) } \end{gathered}$ | $\begin{gathered} 17 \\ \text { HC4.q1.m3-6 } \\ \text { 3-A" (CS) } \end{gathered}$ |  |


| $\mathrm{HC}_{3} \mathrm{O}$ |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
| $\begin{gathered} 1 \\ \text { HC3O.q0.m2-1 } \\ 2-\mathrm{A}^{\prime}(\mathrm{CS}) \end{gathered}$ | $\begin{gathered} 2 \\ \text { HC3O.q0.m4-1 } \\ 4-\mathrm{A}(\mathrm{C} 1) \end{gathered}$ | $\begin{gathered} 3 \\ \text { HC3O.q1.m1-1 } \\ \text { 1-A (C1) } \end{gathered}$ | $\begin{gathered} 4 \\ \text { HC3O.q1.m1-2 } \\ 1-\mathrm{A}^{\prime}(\mathrm{CS}) \end{gathered}$ | $\begin{gathered} 5 \\ \text { HC3O.q1.m1-3 } \\ \text { 1-SG }\left(\mathrm{C}^{*} \mathrm{~V}\right) \end{gathered}$ | $\begin{gathered} 6 \\ \text { HC3O.q1.m3-1 } \\ \text { 3-A' (CS) } \end{gathered}$ |
| $\begin{gathered} 7 \\ \text { HC3O.q1.m3-2 } \\ \text { 3-A (C1) } \end{gathered}$ |  |  |  |  |  |


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| $\mathrm{H}_{4} \mathrm{C}_{2}$ |  |  |  |  |  |
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| $\mathrm{H}_{4} \mathrm{CO}$ |  |
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| $0$ | $0$ |
| $\begin{gathered} 1 \\ \mathrm{H} 4 \mathrm{CO} . \mathrm{q} 0 . \mathrm{m} 1-6 \\ 1-\mathrm{A}^{\prime}(\mathrm{CS}) \end{gathered}$ | $\begin{gathered} 2 \\ \text { H4CO.91.m2-3 } \\ 2-\mathrm{A}^{4}(\mathrm{CS}) \end{gathered}$ |


| $\mathrm{H}_{3} \mathrm{C}_{3}$ |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | $\begin{aligned} & 3 \\ & \begin{array}{c} 3 \\ \text { H3C3.q0.m2-3 } \\ \text { 2-A" (CS) } \end{array} \\ & \hline \end{aligned}$ |  |  |  |
| H3C3.q1.m1-3 <br> 1-A' (CS) |  |  | $\begin{gathered} \text { \% } \\ \substack{10 \\ \text { HBC.3.1.13-2 } \\ 3-A(1) 1)} \end{gathered}$ |  |  |


| $\mathrm{H}_{3} \mathrm{C}_{2} \mathrm{O}$ |  |  |  |  |  |
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| $\mathrm{H}_{2} \mathrm{C}_{4}$ |  |  |  |  |  |
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| $\begin{gathered} 1 \\ \text { H2C4.q0.m1-1 } \\ \text { 1-SG }\left(\mathrm{C}^{*} \mathrm{~V}\right) \end{gathered}$ | $\begin{gathered} 2 \\ \mathrm{H} 2 \mathrm{C} 4 . \mathrm{q} 0 . \mathrm{m} 1-2 \\ 1-\mathrm{A}^{\prime}(\mathrm{CS}) \end{gathered}$ | $\begin{gathered} 3 \\ \mathrm{H} 2 \mathrm{C} 4 . \mathrm{q} 0 . \mathrm{m} 1-4 \\ \text { 1-A (C2) } \end{gathered}$ |  $\begin{gathered} 4 \\ \text { H2C4.q0.m1-5 } \\ \text { 1-A1 (C2V) } \end{gathered}$ | $\begin{gathered} 5 \\ \text { H2C4.q0.m1-7 } \\ \text { 1-A1 (C2V) } \end{gathered}$ | $\begin{gathered} 6 \\ \text { H2C4.q0.m1-8 } \\ \text { 1-A1 (C2V) } \end{gathered}$ |
|  | $\begin{gathered} 8 \\ \text { H2C4.q0.m3-2 } \\ \text { 3-A2 (C2V) } \end{gathered}$ | $\begin{gathered} 9 \\ \text { H2C4.q0.m3-3 } \\ 3-\mathrm{AU}(\mathrm{CI}) \end{gathered}$ | 10 H2C4.q0.m3-4 3-A (C1) | $\begin{gathered} 11 \\ \text { H2C4.q0.m3-5 } \\ \text { 3-A (C1) } \end{gathered}$ | $\begin{gathered} 12 \\ \mathrm{H} 2 \mathrm{C} 4 . \mathrm{q} 0 . \mathrm{m} 3-7 \\ 3-\mathrm{A}(\mathrm{C} 1) \end{gathered}$ |
|  | $\begin{gathered} 14 \\ \text { H2C4.q0.m3-10 } \\ \text { 3-A2 (C2V) } \end{gathered}$ | $\begin{gathered} 15 \\ \text { H2C4.q0.m3-11 } \\ \text { 3-A (C1) } \end{gathered}$ |  <br> 16 H2C4.q1.m2-2 | 17 $\begin{gathered} \mathrm{H} 2 \mathrm{C} 4 . q 1 . \mathrm{m} 2-3 \\ 2-\mathrm{B} 1(\mathrm{C} 2 \mathrm{~V}) \end{gathered}$ | $\begin{gathered} 18 \\ \text { H2C4.q1.m2-4 } \\ \text { 2-A (C1) } \end{gathered}$ |
| $\begin{gathered} 19 \\ \text { H2C4.q1.m2-7 } \\ \text { 2-A" (CS) } \end{gathered}$ |  |  |  | 23 <br> H2C4.q1.m4-4 <br> 4-A2 (C2V) | $\begin{gathered} 24 \\ \text { H2C4.q1.m4-5 } \\ \text { 4-A (C1) } \end{gathered}$ |
| $\begin{gathered} 25 \\ \text { H2C4.q1.m4-6 } \\ 4-\mathrm{A}(\mathrm{C} 1) \end{gathered}$ | $\begin{gathered} 26 \\ \text { H2C4.q1.m4-7 } \\ 4-\mathrm{Al}^{\prime}(\mathrm{CS}) \end{gathered}$ | $\begin{gathered} 27 \\ \text { H2C4.q1.m4-8 } \\ 4-\mathrm{A}(\mathrm{C} 1) \end{gathered}$ |  |  |  |



| $\mathrm{HC}_{4} \mathrm{O}$ |  |  |  |  |  |
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| $\%$ | \& | $8$ |  | $\xi$ | $8$ |
| $\begin{gathered} 1 \\ \text { HC40.90.m2-1 } \\ 2-A^{1}(\text { CS }) \end{gathered}$ | $\underset{\substack{\text { HC40.91. } 1 \mathrm{cl-1} \\ 1-\mathrm{A}(\mathrm{CS})}}{2}$ | $\stackrel{3}{\substack{\text { HC40.9..m-2 } \\ 1-A(C S)}}$ | $\underset{\substack{\text { HC40.a1.m-3 } \\ 1-\mathrm{A}(\mathrm{Cl})}}{4}$ | $\underset{\substack{5 \\ \text { HC40.q1.m1-6 } \\ 1-A^{\prime}(\mathrm{CS})}}{\mathrm{S}^{2}}$ | $\underset{\substack{\text { HC40-91..1-7-7 } \\ 1-\mathrm{A}(\mathrm{Cl} 1)}}{6}$ |


| $\mathrm{H}_{4} \mathrm{C}_{3}$ |  |  |  |  |  |
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| $\begin{gathered} 1 \\ \mathrm{H} 4 \mathrm{C} 3 . \mathrm{q} 0 . \mathrm{m} 1-1 \\ 1-\mathrm{A}(\mathrm{C} 1) \end{gathered}$ | $\begin{gathered} 2 \\ \text { H4C3.q0.m1-2 } \\ \text { 1-A1 (C2V) } \end{gathered}$ |  | $\begin{gathered} 4 \\ \text { H4C3.q0.m1-4 } \\ \text { 1-A1 (C3V) } \end{gathered}$ | $\begin{gathered} 5 \\ \text { H4C3.q0.m1-5 } \\ \text { 1-A1 (C2V) } \end{gathered}$ | $\begin{gathered} 6 \\ \text { H4C3.q0.m3-2 } \\ \text { 3-A (C1) } \end{gathered}$ |
| $\begin{gathered} 7 \\ \text { H4C3.q0.m3-4 } \\ \text { 3-A (C1) } \end{gathered}$ | $\begin{gathered} 8 \\ \text { H4C3.q0.m3-5 } \\ \text { 3-B1 (C2V) } \end{gathered}$ | $\begin{gathered} 9 \\ \text { H4C3.q0.m3-6 } \\ \text { 3-A" (CS) } \end{gathered}$ | 10 <br> H4C3.q0.m3-7 <br> 3-A" (CS) | 11 <br> H4C3.q1.m2-1 <br> 2-A (C1) | 12 <br> H4C3.q1.m2-2 <br> 2-A (C1) |
|  |  | 15 <br> H4C3.q1.m2-6 <br> 2-B (C2) | $\begin{gathered} 16 \\ \text { H4C3.q1.m4-1 } \\ 4-\mathrm{A}^{\prime \prime}(\mathrm{CS}) \end{gathered}$ |  | 18 $\begin{gathered} \text { H4C3.q1.m4-3 } \\ 4-\mathrm{A}^{\prime \prime}(\mathrm{CS}) \end{gathered}$ |
|  | $\begin{gathered} 20 \\ \text { H4C3.q1.m4-5 } \\ \text { 4-A" (CS) } \end{gathered}$ |  |  |  |  |


| $\mathrm{H}_{3} \mathrm{C}_{4}$ |  |  |  |  |  |
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| $\begin{gathered} 1 \\ \text { H3C4.q0.m2-2 } \\ \text { 2-B2 (C2V) } \end{gathered}$ | $\begin{gathered} 2 \\ \text { H3C4.q0.m2-3 } \\ \text { 2-A (C1) } \end{gathered}$ | $\begin{gathered} 3 \\ \text { H3C4.q0.m2-4 } \\ 2-\mathrm{A}^{\prime}(\mathrm{CS}) \end{gathered}$ | $\begin{gathered} 4 \\ \text { H3C4.q0.m2-5 } \\ \text { 2-A (CS) } \end{gathered}$ | $\begin{gathered} 5 \\ \text { H3C4.q0.m2-7 } \\ 2-\mathrm{A}(\mathrm{C} 1) \end{gathered}$ | $\begin{gathered} 6 \\ \text { H3C4.q0.m2-8 } \\ \text { 2-A (C1) } \end{gathered}$ |
| $\begin{gathered} 7 \\ \text { H3C4.q0.m2-10 } \\ \text { 2-A (C1) } \end{gathered}$ | $\begin{gathered} 8 \\ \text { H3C4.q0.m2-12 } \\ 2-A^{\prime \prime}(\mathrm{CS}) \end{gathered}$ | $\begin{gathered} 9 \\ \text { H3C4.q0.m2-13 } \\ \text { 2-A" (CS) } \end{gathered}$ | $\begin{gathered} 10 \\ \text { H3C4.q0.m2-14 } \\ \text { 2-A (C1) } \end{gathered}$ | $\begin{gathered} 11 \\ \text { H3C4.q0.m4-1 } \\ \text { 4-A1 (C3V) } \end{gathered}$ | 12 <br> H3C4.q0.m4-2 <br> 4-A" (CS) |
| $\begin{gathered} 13 \\ \text { H3C4.q0.m4-3 } \\ 4-\mathrm{A}^{\prime \prime}(\mathrm{CS}) \end{gathered}$ | 14 <br> H3C4.q0.m4-4 4-A" (CS) | $\begin{gathered} 15 \\ \text { H3C4.q0.m4-5 } \\ \text { 4-A (C1) } \end{gathered}$ | $\begin{gathered} 16 \\ \text { H3C4.q0.m4-6 } \\ \text { 4-A (C1) } \end{gathered}$ | $\begin{gathered} 17 \\ \text { H3C4.q0.m4-7 } \\ \text { 4-A" (CS) } \end{gathered}$ | 18 $\text { НЗС } 4 . q 0 . \mathrm{m} 4-8$ 4-A" (CS) |
| $\begin{gathered} 19 \\ \text { H3C4.q0.m4-9 } \\ 4-\mathrm{A}(\mathrm{C} 1) \end{gathered}$ | 4-A (C1) | $\begin{gathered} 21 \\ \text { H3C4.q0.m4-12 } \\ 4-\mathrm{B} 2(\mathrm{C} 2 \mathrm{~V}) \end{gathered}$ |  | $\begin{gathered} 23 \\ \text { H3C4.q0.m4-14 } \\ 4-\mathrm{A}^{\prime \prime}(\mathrm{CS}) \end{gathered}$ | $\begin{gathered} 24 \\ \text { H3C4.q1.m1-1 } \\ \text { 1-A1 (C3V) } \end{gathered}$ |
| $\begin{gathered} 25 \\ \text { H3C4.q1.m1-2 } \\ \text { 1-A1 (C2V) } \end{gathered}$ | $\begin{gathered} 26 \\ \text { H3C4.q1.m1-3 } \\ \text { 1-A (C1) } \end{gathered}$ | $\begin{gathered} 27 \\ \text { H3C4.q1.m1-5 } \\ 1-\mathrm{A}^{\prime}(\mathrm{CS}) \end{gathered}$ | $\begin{gathered} 28 \\ \text { H3C4.q1.m1-7 } \\ \text { 1-A (C1) } \end{gathered}$ | $\begin{gathered} 29 \\ \text { H3C4.q1.m1-10 } \\ 1-\mathrm{A}^{\prime}(\mathrm{CS}) \end{gathered}$ | $\begin{gathered} 30 \\ \text { H3C4.q1.m1-11 } \\ \text { 1-A (C1) } \end{gathered}$ |
| $\begin{gathered} 31 \\ \text { H3C4.q1.m1-13 } \\ \text { 1-A1 (C2V) } \end{gathered}$ | $\begin{gathered} 32 \\ \text { H3C4.q1.m1-15 } \\ \text { 1-A (C1) } \end{gathered}$ | $\begin{gathered} 33 \\ \text { H3C4.q1.m3-1 } \\ \text { 3-A" (CS) } \end{gathered}$ | $\begin{gathered} 34 \\ \text { H3C4.q1.m3-2 } \\ \text { 3-A2 (C2V) } \end{gathered}$ |  | $\begin{gathered} 36 \\ \text { H3C4.q1.m3-4 } \\ \text { 3-A" (CS) } \end{gathered}$ |
| $\begin{gathered} 37 \\ \text { H3C4.q1.m3-5 } \\ \text { 3-A" (CS) } \end{gathered}$ | $\begin{gathered} 38 \\ \text { H3C4.q1.m3-7 } \\ \text { 3-A" (CS) } \end{gathered}$ | $\begin{gathered} 39 \\ \text { H3C4.q1.m3-8 } \\ \text { 3-A (C1) } \end{gathered}$ | $\begin{gathered} 40 \\ \text { H3C4.q1.m3-10 } \\ \text { 3-A (C1) } \end{gathered}$ | 41 <br> H3C4.q1.m3-11 <br> 3-A (C1) |  |
|  | 44 $\begin{aligned} & \text { H3C4.q1.m3-14 } \\ & \text { 3-A (C1) } \end{aligned}$ | $\begin{gathered} 45 \\ \text { H3C4.q1.m3-15 } \\ 3-\mathrm{A}^{\prime}(\mathrm{CS}) \end{gathered}$ |  |  |  |



| $\mathrm{H}_{2} \mathrm{C}_{4} \mathrm{O}$ |  |  |  |  |  |
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| H2C4O.q0.m1-1 1-A (C1) |  |  |  |  |  |
| (2) |  |  |  |  |  |


| $\mathrm{H}_{3} \mathrm{C}_{3} \mathrm{O}$ |  |  |  |
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| $\underset{\substack{1 \\ \text { нзсз3.9.1.ml-1 } \\ 1-\mathrm{A}(\mathrm{CS})}}{1}$ | $\begin{gathered} \text { H3C3O.q1.m1-2 } \\ 1-\mathrm{A}^{\prime}(\mathrm{CS}) \end{gathered}$ |  | H3C3O.q1.m1-6 $1-\mathrm{A}^{\prime}(\mathrm{CS})$ |


| $\mathrm{H}_{3} \mathrm{C}_{4} \mathrm{O}$ |  |  |  |  |  |
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| $\begin{gathered} 1 \\ \text { H3C4O.q0.m2-1 } \\ \text { 2-A" (CS) } \end{gathered}$ | $\begin{gathered} 2 \\ \mathrm{H} 3 \mathrm{C} 4 \mathrm{O} . \mathrm{q} 0 . \mathrm{m} 2-2 \end{gathered}$ |  | $\begin{gathered} \text { H3C4O.q1.m1-2 } \\ \text { 1-A (C1) } \end{gathered}$ | $5$ | H3C4O.q1.m1-4 1-A (C1) |
| $\begin{gathered} 7 \\ \text { H3C4O.q1.m1-5 } \\ \text { 1-A (C1) } \end{gathered}$ |  |  |  |  |  |


| $\mathrm{H}_{4} \mathrm{C}_{4}$ |  |  |  |  |  |
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| $\begin{gathered} 1 \\ \text { H4C4.q0.m1-1 } \\ 1-\mathrm{A}^{\prime}(\mathrm{CS}) \end{gathered}$ | $\begin{gathered} 2 \\ \mathrm{H} 4 \mathrm{C} 4 . \mathrm{q} 0 . \mathrm{m} 1-2 \\ 1-\mathrm{A}(\mathrm{C} 1) \end{gathered}$ | $\begin{gathered} 3 \\ \mathrm{H} 4 \mathrm{C} 4 . \mathrm{q} 0 . \mathrm{m} 1-3 \\ \text { 1-A (C1) } \end{gathered}$ | $\begin{gathered} 4 \\ \text { H4C4.q0.m1-4 } \\ \text { 1-A1 (C2V) } \end{gathered}$ | $\begin{gathered} 5 \\ \text { H4C4.q0.m1-5 } \\ \text { 1-A (C1) } \end{gathered}$ | $\begin{gathered} 6 \\ \text { H4C4.q0.m1-6 } \\ 1-\mathrm{A}^{\prime}(\mathrm{CS}) \end{gathered}$ |
| $\begin{gathered} 7 \\ \text { H4C4.q0.m1-7 } \\ \text { 1-A' (CS) } \end{gathered}$ | $\begin{gathered} 8 \\ \text { H4C4.q0.m1-11 } \\ \text { 1-A (C1) } \end{gathered}$ | $\begin{gathered} 9 \\ \mathrm{H} 4 \mathrm{C} 4 . \mathrm{q} 0 . \mathrm{m} 1-12 \\ 1-\mathrm{A}^{\prime}(\mathrm{CS}) \end{gathered}$ | $\begin{gathered} 10 \\ \text { H4C4.q0.m1-13 } \\ \text { 1-AG (D2H) } \end{gathered}$ | $\begin{gathered} 11 \\ \text { H4C4.q0.m1-14 } \\ \text { 1-A (C1) } \end{gathered}$ | $\begin{gathered} 12 \\ \text { H4C4.q0.m1-15 } \\ 1-\mathrm{A}^{\prime}(\mathrm{CS}) \end{gathered}$ |
| $\begin{gathered} 13 \\ \text { H4C4.q0.m1-17 } \\ 1-\mathrm{A}^{\prime}(\mathrm{CS}) \end{gathered}$ | $\begin{gathered} 14 \\ \text { H4C4.q0.m1-18 } \\ \text { 1-A1 (TD) } \end{gathered}$ | 15 <br> H4C4.q0.m1-19 <br> 1-AG (D2H) | $\begin{gathered} 16 \\ \text { H4C4.q0.m3-1 } \\ \text { 3-A" (CS) } \end{gathered}$ | $\begin{gathered} 17 \\ \text { H4C4.q0.m3-3 } \\ \text { 3-A (C1) } \end{gathered}$ | $\begin{gathered} 18 \\ \text { H4C4.q0.m3-4 } \\ \text { 3-A (C1) } \end{gathered}$ |
| 19 $\begin{gathered} \text { H4C4.q0.m3-5 } \\ \text { 3-A (C1) } \end{gathered}$ | $\begin{gathered} 20 \\ \text { H4C4.q0.m3-6 } \\ 3-\mathrm{A}^{\prime \prime}(\mathrm{CS}) \end{gathered}$ | 21 <br> H4C4.q0.m3-7 <br> 3-BU (C2H) | $\begin{gathered} 22 \\ \text { H4C4.q0.m3-8 } \\ \text { 3-A (C1) } \end{gathered}$ |  | $\begin{gathered} 24 \\ \text { H4C4.q0.m3-10 } \\ \text { 3-A (C1) } \end{gathered}$ |
| $\begin{gathered} 25 \\ \text { H4C4.q0.m3-12 } \\ \text { 3-A (C1) } \end{gathered}$ | $\begin{gathered} 26 \\ \text { H4C4.q0.m3-13 } \\ \text { 3-AG (CI) } \end{gathered}$ |  | $\begin{gathered} 28 \\ \text { H4C4.q0.m3-15 } \\ \text { 3-A2 (C2V) } \end{gathered}$ | 29 $\begin{gathered} \mathrm{H} 4 \mathrm{C} 4 . \mathrm{q} 0 . \mathrm{m} 3-16 \\ 3-\mathrm{B} 2(\mathrm{C} 2 \mathrm{~V}) \end{gathered}$ | $\begin{gathered} 30 \\ \text { H4C4.q0.m3-17 } \\ \text { 3-A (C1) } \end{gathered}$ |
| $\begin{gathered} 31 \\ \text { H4C4.q0.m3-18 } \\ \text { 3-A" (CS) } \end{gathered}$ | 32 <br> H4C4.q0.m3-19 <br> 3-A1 (D2D) | $\begin{gathered} 33 \\ \text { H4C4.q1.m2-1 } \\ \text { 2-A (C1) } \end{gathered}$ | $\begin{gathered} 34 \\ \text { H4C4.q1.m2-2 } \\ 2-\text { Al" }^{\prime}(\mathrm{CS}) \end{gathered}$ | $\begin{gathered} 35 \\ \text { H4C4.q1.m2-3 } \\ \text { 2-A (C1) } \end{gathered}$ | $\begin{gathered} 36 \\ \text { H4C4.q1.m2-4 } \\ \text { 2-B1 (C2V) } \end{gathered}$ |
| $\begin{gathered} 37 \\ \text { H4C4.q1.m2-5 } \\ \text { 2-A (C1) } \end{gathered}$ | 38 $\begin{gathered} \text { H4C4.q1.m2-6 } \\ 2-\mathrm{A}^{\prime \prime}(\mathrm{CS}) \end{gathered}$ | $\begin{gathered} 39 \\ \text { H4C4.q1.m2-7 } \\ \text { 2-A (C1) } \end{gathered}$ | $\begin{gathered} 40 \\ \text { H4C4.q1.m2-8 } \\ 2-\mathrm{A}^{\prime}(\mathrm{CS}) \end{gathered}$ | $\begin{gathered} 41 \\ \text { H4C4.q1.m2-9 } \\ \text { 2-A (C1) } \end{gathered}$ | $\begin{gathered} 42 \\ \text { H4C4.q1.m2-10 } \\ 2-\mathrm{A}(\mathrm{C} 1) \end{gathered}$ |
| $\begin{gathered} 43 \\ \text { H4C4.q1.m2-11 } \\ \text { 2-A (C1) } \end{gathered}$ | $\begin{gathered} 44 \\ \text { H4C4.q1.m2-12 } \\ \text { 2-A" (CS) } \end{gathered}$ | 45 <br> H4C4.q1.m2-13 <br> 2-B2G (D2H) | $\begin{gathered} 46 \\ \text { H4C4.q1.m2-14 } \\ \text { 2-A (C1) } \end{gathered}$ | $\begin{gathered} 47 \\ \text { H4C4.q1.m2-15 } \\ \text { 2-A' (CS) } \end{gathered}$ | 48 $\begin{gathered} \mathrm{H} 4 \mathrm{C} 4 . \mathrm{q} 1 . \mathrm{m} 2-17 \\ 2-\mathrm{BU}(\mathrm{C} 2 \mathrm{H}) \end{gathered}$ |


| $\mathrm{H}_{4} \mathrm{C}_{4}$ (Continued from previous page) |  |  |  |  |  |
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| $\mathrm{H}_{4} \mathrm{C}_{3} \mathrm{O}$ |  |  |  |  |  |
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|  |  |  | \& | $\begin{gathered} 5 \\ \text { H4C3O.q1.m2-2 } \end{gathered}$ <br> 2-A (C1) |  |
|  | $\underbrace{}_{\substack{8 \\ \text { H4C30. } 91 . \mathrm{m} 4-2 \\ 4-A(C 1)}}$ |  |  |  |  |


| $\mathrm{C}_{4} \mathrm{H}_{4} \mathrm{O}$ |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
| $\begin{gathered} 1 \\ \text { C4H4O.q0.m1-1 } \\ 1-\mathrm{A}^{\prime}(\mathrm{CS}) \end{gathered}$ | $\begin{gathered} 2 \\ \text { C4H4O.q0.m1-2 } \\ \text { 1-A1 (C2V) } \end{gathered}$ | $\begin{gathered} 3 \\ \mathrm{C} 4 \mathrm{H} 4 \mathrm{O} . \mathrm{q} 0 . \mathrm{m} 1-3 \\ 1-\mathrm{A}^{\prime}(\mathrm{CS}) \end{gathered}$ | $\begin{gathered} 4 \\ \text { C4H4O.q0.m1-4 } \\ \text { 1-A1 (C2V) } \end{gathered}$ |  $\begin{gathered} 5 \\ \text { C4H4O.q0.m1-5 } \\ 1-\mathrm{A}^{\prime}(\mathrm{CS}) \end{gathered}$ | $\begin{gathered} 6 \\ \text { C4H4O.q0.m1-6 } \\ 1-\mathrm{A}^{\prime}(\mathrm{CS}) \end{gathered}$ |
| $\begin{gathered} 7 \\ \text { C4H4O.q0.m1-7 } \\ \text { 1-A (C1) } \end{gathered}$ | $\begin{gathered} 8 \\ \text { C4H4.q0.m1-8 } \\ 1-\mathrm{A}^{\prime}(\mathrm{CS}) \end{gathered}$ | $\begin{gathered} 9 \\ \mathrm{C} 4 \mathrm{H} 4 \mathrm{O} . \mathrm{q} 0 . \mathrm{m} 1-9 \\ 1-\mathrm{A}^{\prime}(\mathrm{CS}) \end{gathered}$ | $\begin{gathered} 10 \\ \text { C4H4O.q0.m1-10 } \\ 1-\mathrm{A}^{\prime}(\mathrm{CS}) \end{gathered}$ | $\begin{gathered} 11 \\ \text { C4H4O.q0.m1-11 } \\ 1-\mathrm{A}^{\prime}(\mathrm{CS}) \end{gathered}$ | $\begin{gathered} 12 \\ \text { C4H4O.q0.m1-12 } \\ 1-\mathrm{A}^{\prime}(\mathrm{CS}) \end{gathered}$ |
|  $\begin{gathered} 13 \\ \text { C4H4O.q0.m1-13 } \\ 1-\mathrm{A}^{\prime}(\mathrm{CS}) \end{gathered}$ | $\begin{gathered} \text { C4H4O.q0.m1-14 } \\ 1-\mathrm{A}^{\prime}(\mathrm{CS}) \end{gathered}$ |  | $\begin{gathered} 16 \\ \text { C4H4O.q0.m1-16 } \\ 1-\mathrm{A}(\mathrm{C} 1) \end{gathered}$ | $\begin{gathered} 17 \\ \text { C4H4O.q0.m1-17 } \\ 1-\mathrm{A}^{\prime}(\mathrm{CS}) \end{gathered}$ | $\begin{gathered} 18 \\ \text { C4H4O.q0.m1-18 } \\ 1-\mathrm{A}^{\prime}(\mathrm{CS}) \end{gathered}$ |
| $\begin{gathered} 19 \\ \text { C4H4O.q0.m1-19 } \\ 1-\mathrm{A}^{\prime}(\mathrm{CS}) \end{gathered}$ | $\begin{gathered} 20 \\ \text { C4H4O.q0.m1-20 } \\ \text { 1-A' (CS) } \end{gathered}$ | $\begin{gathered} 21 \\ \text { C4H4O.q0.m1-21 } \\ 1-\mathrm{A}^{\prime}(\mathrm{CS}) \end{gathered}$ | $\begin{gathered} 22 \\ \text { C4H4O.q1.m2-1 } \\ 2-\mathrm{A}^{\prime}(\mathrm{CS}) \end{gathered}$ | $\begin{gathered} 23 \\ \text { C4H4O.q1.m2-2 } \\ \text { 2-A (C1) } \end{gathered}$ | $\begin{gathered} 24 \\ \text { C4H4O.q1.m2-3 } \\ \text { 2-A2 (C2V) } \end{gathered}$ |
| $\begin{gathered} 25 \\ \text { C4H4O.q1.m2-4 } \\ 2-\mathrm{A}^{\prime}(\mathrm{CS}) \end{gathered}$ | $\begin{gathered} 26 \\ \text { C4H4O.q1.m2-5 } \\ 2-\mathrm{A}^{\prime \prime}(\mathrm{CS}) \end{gathered}$ | 27 C4H4O.q1.m2-6 2-A (C1) |  |  | $\begin{gathered} 30 \\ \text { C4H4O.q1.m2-9 } \\ \text { 2-A" (CS) } \end{gathered}$ |
| $\begin{gathered} 31 \\ \text { C4H4O.q1.m2-10 } \\ 2-\mathrm{A}^{\prime}(\mathrm{CS}) \end{gathered}$ | $\begin{gathered} 32 \\ \text { C4H4O.q1.m2-11 } \\ 2-\mathrm{A}(\mathrm{C} 1) \end{gathered}$ | 33 <br> C4H4O.q1.m2-12 <br> 2-A (C1) | $\begin{gathered} 34 \\ \text { C4H4O.q1.m2-13 } \\ \text { 2-A (C1) } \end{gathered}$ | $\begin{gathered} 35 \\ \text { C4H4O.q1.m2-14 } \\ 2-\mathrm{A}^{\prime}(\mathrm{CS}) \end{gathered}$ |  |
|  | $\begin{gathered} 38 \\ \mathrm{C} 4 \mathrm{H} 4 \mathrm{O} \cdot \mathrm{q} 1 . \mathrm{m} 2-19 \\ 2-\mathrm{A}^{\prime}(\mathrm{CS}) \end{gathered}$ | $\begin{gathered} 39 \\ \mathrm{C} 4 \mathrm{H} 4 \mathrm{O} \cdot \mathrm{q} 1 . \mathrm{m} 2-20 \\ 2-\mathrm{A}(\mathrm{C} 1) \end{gathered}$ |  |  |  |

## Appendix B

## $\mathbf{M}_{3} \mathbf{C}$ input file

The following code presents the input file of $\mathrm{M}_{3} \mathrm{C}$ calculations for the singly ionized furan. The results of this simulation were presented in Chapter 5.2.3.

```
BEGIN EXCITATION_ENERGY_SCAN
excitationEnergy = 0:10:21 # dE = 0.5 eV
END EXCITATION_ENERGY_SCAN
BEGIN GOPTIONS
systemRadius = 13.0
overlappingRadius = 0.4
useRandomWalkers = FALSE
randomWalkStepRadius = 1.0
useZPECorrection = TRUE
useSpinConservationRules = FALSE
angularMomentumCouplingScheme = JJL
structureSamplingMethod = SEQUENTIAL
END GOPTIONS
BEGIN MARKOV_CHAIN
fask = V,T,R,5*S:0,V,T,R,5*S:1:-1
burnInFraction = 0.1
reactives = C4H4Op(d3)
excitationEnergy = 4.0
tracking = none
numberOfEvents = 200000
numberOfExperiments = 500
historyFileFrequency = 500
geometryHistoryFilePrefix = geom
energyHistoryFile = C4H4O.q1.energy.dat
weightHistoryFile = C4H4O.q1. weight. dat
JHistoryFile = C4H4O.q1.J.dat
histogramFile = C4H4O.q1.histogram.dat
END MARKOV_CHAIN
BEGIN FRAGMENTS_DATABASE
store = /home/eerd/Furan_M3Cv2.0/new5_rxyz
reference = C4H4Op(d3)
\begin{tabular}{|c|c|c|c|c|c|c|c|c|c|c|}
\hline \# Label & & Z M & M WL & SYM & geomFile & Eelec & \multicolumn{4}{|l|}{maxVib} \\
\hline \(\mathrm{H}(\mathrm{d} 2)\) & 0 & 2 & 1 & 1 & H. q0.m2-2.rxyz & -13.667114 & & \# & & SO3(2-S) \\
\hline \(\mathrm{C}(\mathrm{s} 2)\) & 0 & 1 & 5 & 1 & C.q0.m1-2.rxyz & -1028.370642 & & \# & & SO3(1-D) \\
\hline \(\mathrm{C}(\mathrm{t} 1)\) & 0 & 3 & 3 & 1 & C.q0.m3-1.rxyz & -1030.149091 & & \# & & SO3(3-P) \\
\hline \(\mathrm{O}(\mathrm{s} 2)\) & 0 & 1 & 5 & 1 & O.q0.m1-2.rxyz & -2040.552863 & & \# & & SO3(1-D) \\
\hline \(\mathrm{O}(\mathrm{t} 1)\) & 0 & 3 & 3 & 1 & O. \(\mathrm{q} 0 . \mathrm{m} 3-1 . \mathrm{rxyz}\) & -2043.300455 & & \# & & SO3(3-P) \\
\hline H2(s2) & 0 & 1 & 1 & 2 & H2.q0.m1-2.rxyz & -32.097788 & \(\mathrm{H}(\mathrm{d} 2)+\mathrm{H}(\mathrm{d} 2\) ) & \# & 4.76 & D*H(1-SGG) \\
\hline \(\mathrm{HC}(\mathrm{d} 1)\) & 0 & 2 & 2 & 1 & HC. q0.m2-1.rxyz & -1047.478280 & \(\mathrm{H}(\mathrm{d} 2)+\mathrm{C}(\mathrm{t} 1)\) & \# & 3.66 & \(\mathrm{C} * \mathrm{~V}(2-\mathrm{PI})\) \\
\hline \(\mathrm{HC}(\mathrm{q} 24)\) & & 04 & 41 & 1 & HC. q0.m4-24.rxyz & -1046.582374 & \(\mathrm{H}(\mathrm{d} 2)+\mathrm{C}(\mathrm{t} 1)\) & \# & 2.77 & \(\mathrm{C} * \mathrm{~V}(4-\mathrm{SG})\) \\
\hline \(\mathrm{HO}(\mathrm{d} 2)\) & 0 & 2 & 2 & 1 & HO. q0.m2-2.rxyz & -2061.601014 & \(\mathrm{H}(\mathrm{d} 2)+\mathrm{O}(\mathrm{t} 1)\) & \# & 4.63 & \(\mathrm{C} * \mathrm{~V}(2-\mathrm{PI})\) \\
\hline C2(s3) & 0 & 1 & 1 & 2 & C2.q0.m1-3.rxyz & -2065.388103 & \(\mathrm{C}(\mathrm{t} 1)+\mathrm{C}(\mathrm{t} 1)\) & \# & 5.09 & D \(*\) H(1-SGG) \\
\hline C2(t2) & 0 & 3 & 2 & 2 & C2.q0.m3-2.rxyz & -2066.382008 & \(\mathrm{C}(\mathrm{t} 1)+\mathrm{C}(\mathrm{t} 1)\) & \# & 6.08 & \(\mathrm{D} * \mathrm{H}(3-\mathrm{PIU})\) \\
\hline
\end{tabular}
```



| CO. $\mathrm{q} 0 . \mathrm{m} 1-2 . \mathrm{rxyz}$ | -3084.385908 |
| :---: | :---: |
| CO. $\mathrm{q} 0 . \mathrm{m} 3-2 . \mathrm{rxyz}$ | -3078.539149 |
| H2C. q0.m1-1.rxyz | -1065.237570 |
| H2C. q0.m3-7.rxyz | -1065.764739 |
| H2C.q0.m3-9.rxyz | -1062.565811 |
| H2O. q0.m1-2.rxyz | -2080.543368 |
| HC2. q0.m2-1.rxyz | -2085.234915 |
| HC2. q0.m2-3.rxyz | -2084.226879 |
| HC2.q0.m4-1.rxyz | -2081.632608 |
| HCO. q0.m2-2.rxyz | -3097.317862 |
| HCO. q0.m2-7.rxyz | -3099.142127 |
| HCO. q0.m4-12.rxyz | -3094.144308 |
| C3.q0.m1-1.rxyz | -3104.192084 |
| C3.q0.m3-1.rxyz | -3103.356704 |
| C3.q0.m3-3.rxyz | -3101.996725 |
| C2O. q0.m1-2.rxyz | -4116.133213 |
| C2O. q0.m1-3.rxyz | -4115.306606 |
| C2O. q0.m3-2.rxyz | -4117.219022 |
| H3C.q0.m2-1.rxyz | -1084.515305 |
| H2C2.q0.m1-2.rxyz | -2104.982786 |
| H2C2.q0.m1-3.rxyz | -2103.110538 |
| H2C2.q0.m3-1.rxyz | -2101.052209 |
| H2C2.q0.m3-2.rxyz | -2100.723310 |
| H2C2.q0.m3-4.rxyz | -2101.216995 |
| H2CO. q0.m1-1.rxyz | -3116.843626 |
| H2CO. q0.m1-3.rxyz | -3109.932451 |
| H2CO. $\mathrm{q} 0 . \mathrm{m} 1-4 . \mathrm{rxyz}$ | -3114.565682 |
| H2CO. $\mathrm{q} 0 . \mathrm{m} 3-4 . \mathrm{rxyz}$ | -3113.908267 |
| HC3. $90 . \mathrm{m} 2-1 . \mathrm{rxyz}$ | -3121.463520 |
| HC3. q0.m2-2.rxyz | -3121.481650 |
| HC3.q0.m4-16.rxyz | -3120.091298 |
| HC3.q0.m4-18.rxyz | -3118.684622 |
| HC2O. $\mathrm{q} 0 . \mathrm{m} 2-2 . \mathrm{rxyz}$ | -4135.429877 |
| HC2O. $\mathrm{q} 0 . \mathrm{m} 2-5 . \mathrm{rxyz}$ | -4133.003853 |
| HC2O. $\mathrm{q} 0 . \mathrm{m} 4-6 . \mathrm{rxyz}$ | -4130.479318 |
| HC2O. $\mathrm{q} 0 . \mathrm{m} 4-8 . \mathrm{rxyz}$ | -4130.099054 |
| HC2O. q0.m4-13.rxyz | -4130.580540 |
| HC2O. q0.m4-14.rxyz | -4132.954431 |
| HC2O. q0.m4-16.rxyz | -4130.086184 |
| C4.q0.m1-1.rxyz | -4138.951566 |
| C4.q0.m1-3.rxyz | -4139.021954 |
| C4.q0.m3-1.rxyz | -4139.723603 |
| C4.q0.m3-2.rxyz | -4138.150510 |
| C4.q0.m3-5.rxyz | -4137.870781 |
| C3O.q0.m1-3.rxyz | -5150.874006 |
| C3O. q0.m1-4.rxyz | -5150.554249 |
| C3O. q0.m1-5.rxyz | -5155.225939 |
| C3O. $\mathrm{q} 0 . \mathrm{m} 3-1 . \mathrm{rxyz}$ | -5152.236992 |
| H4C. q0.m1-1.rxyz | -1102.985717 |
| H3C2.q0.m2-1.rxyz | -2118.467253 |
| H3C2.q0.m2-2.rxyz | -2120.556900 |
| H3C2.q0.m4-8.rxyz | -2116.944015 |
| H3C2.q0.m4-9.rxyz | -2117.310373 |
| H3CO. $\mathrm{q} 0 . \mathrm{m} 2-1 . \mathrm{rxyz}$ | -3131.820663 |
| H3CO. $\mathrm{q} 0 . \mathrm{m} 2-2 . \mathrm{rxyz}$ | -3132.100672 |
| H2C3.q0.m1-2.rxyz | -3139.846584 |
| H2C3.q0.m1-3.rxyz | -3138.896382 |
| H2C3.q0.m1-4.rxyz | -3139.322057 |
| H2C3.q0.m1-5.rxyz | -3138.897037 |
| H2C3.q0.m3-2.rxyz | -3136.860097 |
| H2C3.q0.m3-3.rxyz | -3138.055634 |
| H2C3.q0.m3-4.rxyz | -3136.757974 |
| H2C3.q0.m3-5.rxyz | -3137.625178 |
| H2C2O. $90 . \mathrm{m} 1-4 . \mathrm{rxyz}$ | -4150.125582 |
| H2C2O. 0 0.m1-5.rxyz | -4153.863118 |
| H2C2O. $00 . \mathrm{m} 1-6 . r$ ryz | -4152.257034 |
| H2C2O. q0.m1-7.rxyz | -4150.071871 |
| H2C2O. $90 . \mathrm{m} 3-5 . \mathrm{rxyz}$ | -4151.612634 |
| HC4.q0.m2-1.rxyz | -4158.322644 |
| HC4.q0.m2-2.rxyz | -4156.788760 |
| HC4.q0.m2-5.rxyz | -4156.002094 |
| HC4.q0.m2-6.rxyz | -4156.916497 |
| HC4.q0.m4-1.rxyz | -4154.587179 |
| HC4.q0.m4-2.rxyz | -4154.587224 |
| HC4.q0.m4-3.rxyz | -4154.646601 |
| HC4.q0.m4-4.rxyz | -4155.175823 |
| HC4.q0.m4-5.rxyz | -4155.687064 |
| HC3O.q0.m2-1.rxyz | -5169.766105 |
| HC3O. $\mathrm{q} 0 . \mathrm{m} 4-1 . \mathrm{rxyz}$ | -5167.828815 |
| C4O. q0.m1-2.rxyz | -6184.266574 |
| C4O.q0.m1-3.rxyz | -6185.014804 |


| 138 | C4O(s4) | $0 \quad 1$ | 1 | 1 |
| :---: | :---: | :---: | :---: | :---: |
| 139 | C4O(s5) | 0 | 1 | 2 |
| 140 | C4O(t2) | 03 | 1 | 1 |
| 141 | H4C2(s3) | 0 | 11 | 1 |
| 142 | H4C2(s4) | 0 | 11 | 4 |
| 143 | H4C2(t4) | 0 | 31 | 1 |
| 144 | H4C2(t5) | 0 | 31 | 4 |
| 145 | H4CO(s6) | 0 | 11 | 1 |
| 46 | H3C3(d1) | 0 | 21 | 2 |
| 47 | H3C3(d2) | 0 | 21 | 1 |
| 148 | H3C3(d3) | 0 | 1 | 1 |
| 149 | H3C3(q1) | 0 | 1 | 1 |
| 50 | Н3C3(q2) | 0 | 41 | 1 |
| 151 | H3C2O(d1) | 0 | 2 |  |
| 52 | H3C2O(q3) | 0 | 4 |  |
| 153 | H3C2O(q4) | 0 | 4 |  |
| 54 | H2C4(s1) | 0 | 1 | 1 |
| 55 | H2C4(s2) |  | 1 | 1 |
| 156 | H2C4(s4) | 0 | 1 | 2 |
| 157 | H2C4(s5) | 0 | 1 | 2 |
| 158 | H2C4(s7) | 0 | 1 | 2 |
| 159 | H2C4(s8) | 0 | 1 | 2 |
| 160 | H2C4(s9) | 0 | 1 | 2 |
| 161 | H2C4(t2) | 0 | 1 | 2 |
| 162 | H2C4(t3) | 0 | 1 | 1 |
| 63 | H2C4(t4) | 0 | 1 | 1 |
| 164 | H2C4(t5) | 0 | 1 | 1 |
| 165 | H2C4(t7) | 0 | 1 | 1 |
| 166 | H2C4(t9) | 0 | 1 | 2 |
| 167 | $\mathrm{H} 2 \mathrm{C} 4(\mathrm{t} 10)$ | 0 | 3 |  |
| 168 | H2C4(t11) | 0 | 3 |  |
| 169 | H2C3O(s1) | 0 | 1 |  |
| 70 | H2C3O(s2) | 0 | 1 |  |
| 171 | H2C3O(t1) | 0 | 3 |  |
| 72 | HC4O(d1) |  | 21 | 1 |
| 173 | H4C3( s1) |  | 1 | 1 |
| 174 | H4C3(s2) |  | 1 | 2 |
| 175 | H4C3(s3) |  | 1 | 1 |
| 176 | H4C3(s4) |  | 1 | 3 |
| 177 | H4C3(s5) |  | 1 | 2 |
| 8 | H4C3(t2) |  | 1 | 1 |
| 179 | H4C3(t4) |  | 1 | 1 |
| 80 | H4C3(t5) | 0 | 1 | 2 |
| 181 | H4C3(t6) |  | 1 | 1 |
| 82 | H4C3(t7) | 0 | 1 | 1 |
| 183 | H4C2O( s3) | 0 | 1 |  |
| 184 | H4C2O(s5) | 0 | 1 |  |
| 185 | H4C2O(s9) | 0 | 1 |  |
| 186 | H4C2O(s10) |  | 1 |  |
| 187 | H3C4(d2) | 0 | 2 | 2 |
| 188 | H3C4(d3) |  | 1 | 1 |
| 89 | H3C4(d4) | 0 | 1 | 1 |
| 190 | H3C4(d5) |  | 1 | 1 |
| 191 | H3C4(d7) | 0 | 1 | 1 |
| 192 | H3C4(d8) |  | 21 | 1 |
| 19 | H3C4(d10) | 0 | 2 |  |
| 194 | H3C4(d12) | 0 | 2 |  |
| 195 | H3C4(d13) | 0 | 2 |  |
| 196 | H3C4(d14) | 0 | 2 |  |
| 197 | H3C4(q1) | 0 | 1 | 3 |
| 198 | H3C4(q2) | 0 | 1 | 1 |
| 199 | H3C4(q3) | 0 | 1 | 1 |
| 00 | H3C4(q4) | 0 | 1 | 1 |
| 1 | H3C4(q5) | 0 | 1 | 1 |
| 202 | H3C4(q6) | 0 | 1 | 1 |
| 203 | H3C4(q7) | 0 | 1 | 1 |
| 20 | H3C4(q8) | 0 | 1 | 1 |
| 205 | H3C4(q9) | 0 | 41 | 1 |
| 206 | H3C4(q10) |  | 4 |  |
| 207 | H3C4( $\mathrm{q}^{12 \text { ) }}$ | 0 | 4 |  |
| 208 | H3C4( q 13 ) | 0 | 4 |  |
| 209 | H3C4(q14) | 0 | 4 |  |
| 210 | H2C4O(s1) | 0 | 1 |  |
| 21 | H2C4O(s2) | 0 | 1 |  |
| 212 | H4C4(s1) | 0 | 11 | 1 |
| 213 | H4C4(s2) | 0 | 1 | 1 |
| 214 | H4C4(s3) | 0 | 1 | 1 |
| 215 | H4C4(s4) | 0 | 1 | 2 |
| 216 | H4C4(s5) |  | 1 | 1 |
| 217 | H4C4(s6) |  | 11 |  |
| 218 | H4C4(s7) |  | 11 |  |


| (s2) +C3(s1) | \# | 1.04 | $\mathrm{CS}(1-\mathrm{A}$ |
| :---: | :---: | :---: | :---: |
| $\mathrm{CO}(\mathrm{s} 2)+\mathrm{C} 3(\mathrm{~s} 1)$ | \# | 0.66 | $\mathrm{C} 2 \mathrm{~V}(1-\mathrm{A} 1)$ |
| $\mathrm{CO}(\mathrm{s} 2)+\mathrm{C} 3$ (s1) | \# | 1.74 | $\mathrm{C} * \mathrm{~V}(3-\mathrm{SG})$ |
| H2(s2)+H2C2(s3) | \# | 0.74 | C1(1-A) |
| $\mathrm{H} 2(\mathrm{~s} 2)+\mathrm{H} 2 \mathrm{C} 2(\mathrm{~s} 2)$ | \# | 2.16 | D2H(1-AG) |
| $\mathrm{H} 2(\mathrm{~s} 2)+\mathrm{H} 2 \mathrm{C} 2(\mathrm{~s} 3)$ | \# | 0.95 | $\mathrm{CS}\left(3-\mathrm{A}^{\prime \prime}\right)$ |
| $\mathrm{H} 2(\mathrm{~s} 2)+\mathrm{H} 2 \mathrm{C} 2(\mathrm{~s} 3)$ | \# | 1.25 | D2D(3-A1) |
| $\mathrm{H} 2(\mathrm{~s} 2)+\mathrm{H} 2 \mathrm{CO}(\mathrm{s} 1)$ | \# | 1.19 | $\mathrm{CS}\left(1-\mathrm{A}^{\prime}\right)$ |
| $\mathrm{H} 2(\mathrm{~s} 2)+\mathrm{HC} 3(\mathrm{~d} 2)$ | \# | 4.02 | $\mathrm{C} 2 \mathrm{~V}(2-\mathrm{B} 1)$ |
| $\mathrm{H} 2(\mathrm{~s} 2)+\mathrm{HC3}(\mathrm{~d} 2)$ | \# | 2.57 | $\mathrm{CS}\left(2-\mathrm{A}^{\prime}\right)$ |
| $\mathrm{H} 2(\mathrm{~s} 2)+\mathrm{HC3}(\mathrm{~d} 2)$ | \# | 1.92 | $\mathrm{CS}\left(2-\mathrm{A}^{\prime \prime}\right)$ |
| $\mathrm{H}(\mathrm{d} 2)+\mathrm{H} 2 \mathrm{C} 3$ ( s 5 ) | \# | 0.24 | C1(4-A) |
| $\mathrm{H} 2(\mathrm{~s} 2)+\mathrm{HC} 3(\mathrm{~d} 2)$ | \# | 0.28 | $\mathrm{CS}\left(4-\mathrm{A}{ }^{\prime \prime}\right)$ |
| $\mathrm{H}(\mathrm{d} 2)+\mathrm{H} 2 \mathrm{C} 2 \mathrm{O}(\mathrm{s} 5)$ | \# | 0.80 | C1(2-A) |
| $\mathrm{H}(\mathrm{d} 2)+\mathrm{H} 2 \mathrm{C} 2 \mathrm{O}(\mathrm{t} 5)$ | \# | 0.13 | C1(4-A) |
| $\mathrm{HC}(\mathrm{d} 1)+\mathrm{H} 2 \mathrm{CO}(\mathrm{s} 1)$ | \# | 0.06 | C1(4-A) |
| $\mathrm{H}(\mathrm{d} 2)+\mathrm{HC4}(\mathrm{~d} 1)$ | \# | 5.80 | $\mathrm{C} * \mathrm{~V}(1-\mathrm{SG})$ |
| $\mathrm{H}(\mathrm{d} 2)+\mathrm{HC4}(\mathrm{~d} 1)$ | \# | 3.03 | $\mathrm{CS}\left(1-\mathrm{A}^{\prime}\right)$ |
| $\mathrm{H}(\mathrm{d} 2)+\mathrm{HC} 4(\mathrm{~d} 1)$ | \# | 2.49 | C2(1-A) |
| $\mathrm{H}(\mathrm{d} 2)+\mathrm{HC4}(\mathrm{~d} 1)$ | \# | 1.39 | $\mathrm{C} 2 \mathrm{~V}(1-\mathrm{A} 1)$ |
| $\mathrm{H}(\mathrm{d} 2)+\mathrm{HC4}(\mathrm{~d} 1)$ | \# | 2.70 | $\mathrm{C} 2 \mathrm{~V}(1-\mathrm{A} 1)$ |
| $\mathrm{H}(\mathrm{d} 2)+\mathrm{HC4}(\mathrm{~d} 1)$ | \# | 4.01 | $\mathrm{C} 2 \mathrm{~V}(1-\mathrm{A} 1)$ |
| H(d2) + $\mathrm{HC4} 4$ (d1) | \# | 3.02 | $\mathrm{C} 2 \mathrm{H}(1-\mathrm{AG})$ |
| $\mathrm{H}(\mathrm{d} 2)+\mathrm{HC4}(\mathrm{~d} 1)$ | \# | 2.38 | $\mathrm{C} 2 \mathrm{~V}(3-\mathrm{A} 2)$ |
| $\mathrm{H}(\mathrm{d} 2)+\mathrm{HC4}(\mathrm{~d} 1)$ | \# | 2.39 | $\mathrm{CI}(3-\mathrm{AU})$ |
| $\mathrm{H}(\mathrm{d} 2)+\mathrm{HC4}(\mathrm{~d} 1)$ | \# | 2.52 | C1(3-A) |
| H2(s2)+C4(s1) | \# | 0.00 | C1(3-A) |
| $\mathrm{H}(\mathrm{d} 2)+\mathrm{HC4}(\mathrm{~d} 1)$ | \# | 1.74 | C1(3-A) |
| $\mathrm{H}(\mathrm{d} 2)+\mathrm{HC4}(\mathrm{~d} 1)$ | \# | 2.26 | $\mathrm{C} 2 \mathrm{~V}(3-\mathrm{A} 2)$ |
| H(d2) +HC4 (d1) | \# | 2.10 | $\mathrm{C} 2 \mathrm{~V}(3-\mathrm{A} 2)$ |
| $\mathrm{H}(\mathrm{d} 2)+\mathrm{HC} 4(\mathrm{~d} 1)$ | \# | 1.72 | C1(3-A) |
| $\mathrm{H} 2(\mathrm{~s} 2)+\mathrm{C} 3 \mathrm{O}(\mathrm{s} 5)$ | \# | 0.00 | $\mathrm{CS}\left(1-\mathrm{A}^{\prime}\right)$ |
| H2C2(s3) $+\mathrm{CO}(\mathrm{s} 2)$ | \# | 0.06 | $\mathrm{CS}\left(1-\mathrm{A}^{\prime}\right)$ |
| H2C2(t2) $+\mathrm{CO}(\mathrm{s} 2)$ | \# | 0.09 | C1(3-A) |
| $\mathrm{HCO}(\mathrm{d} 7)+\mathrm{C} 3(\mathrm{~s} 1)$ | \# | 0.28 | CS(2-A") |
| H2(s2)+H2C3(s2) | \# | 0.80 | $\mathrm{C} 1(1-\mathrm{A})$ |
| $\mathrm{H} 2(\mathrm{~s} 2)+\mathrm{H} 2 \mathrm{C} 3(\mathrm{~s} 2)$ | \# | 2.38 | $\mathrm{C} 2 \mathrm{~V}(1-\mathrm{A} 1)$ |
| $\mathrm{H} 2(\mathrm{~s} 2)+\mathrm{H} 2 \mathrm{C} 3(\mathrm{~s} 2)$ | \# | 3.50 | C1(1-A) |
| $\mathrm{H} 2(\mathrm{~s} 2)+\mathrm{H} 2 \mathrm{C} 3(\mathrm{~s} 2)$ | \# | 3.43 | $\mathrm{C} 3 \mathrm{~V}(1-\mathrm{A} 1)$ |
| $\mathrm{H} 2(\mathrm{~s} 2)+\mathrm{H} 2 \mathrm{C} 3(\mathrm{~s} 2)$ | \# | 0.47 | $\mathrm{C} 2 \mathrm{~V}(1-\mathrm{A} 1)$ |
| $\mathrm{H} 2(\mathrm{~s} 2)+\mathrm{H} 2 \mathrm{C} 3(\mathrm{~s} 2)$ | \# | 1.36 | C1(3-A) |
| $\mathrm{H} 2(\mathrm{~s} 2)+\mathrm{H} 2 \mathrm{C} 3(\mathrm{~s} 2)$ | \# | 1.26 | C1(3-A) |
| $\mathrm{H} 2(\mathrm{~s} 2)+\mathrm{H} 2 \mathrm{C} 3(\mathrm{~s} 4)$ | \# | 0.42 | $\mathrm{C} 2 \mathrm{~V}(3-\mathrm{B} 1)$ |
| $\mathrm{H} 2(\mathrm{~s} 2)+\mathrm{H} 2 \mathrm{C} 3(\mathrm{~s} 4)$ | \# | 0.13 | $\mathrm{CS}\left(3-\mathrm{A}{ }^{\prime \prime}\right)$ |
| $\mathrm{H} 2(\mathrm{~s} 2)+\mathrm{H} 2 \mathrm{C} 3(\mathrm{~s} 2)$ | \# | 1.24 | $\mathrm{CS}\left(3-\mathrm{A}{ }^{\prime \prime}\right)$ |
| $\mathrm{H} 2(\mathrm{~s} 2)+\mathrm{H} 2 \mathrm{C} 2 \mathrm{O}(\mathrm{s} 6)$ | \# | 0.62 | $\mathrm{CS}\left(1-\mathrm{A}^{\prime}\right)$ |
| $\mathrm{H} 2(\mathrm{~s} 2)+\mathrm{H} 2 \mathrm{C} 2 \mathrm{O}(\mathrm{s} 6)$ | \# | 0.78 | C1(1-A) |
| $\mathrm{H} 2(\mathrm{~s} 2)+\mathrm{H} 2 \mathrm{C} 2 \mathrm{O}(\mathrm{s} 5)$ | \# | 0.94 | $\mathrm{CS}\left(1-\mathrm{A}^{\prime}\right)$ |
| $\mathrm{H} 2(\mathrm{~s} 2)+\mathrm{H} 2 \mathrm{C} 2 \mathrm{O}(\mathrm{s} 5)$ |  | 0.88 | $8 \mathrm{CS}\left(1-\mathrm{A}^{\prime}\right)$ |
| $\mathrm{H}(\mathrm{d} 2)+\mathrm{H} 2 \mathrm{C} 4(\mathrm{~s} 1)$ | \# | 2.31 | $\mathrm{C} 2 \mathrm{~V}(2-\mathrm{B} 2)$ |
| $\mathrm{H}(\mathrm{d} 2)+\mathrm{H} 2 \mathrm{C} 4(\mathrm{~s} 1)$ | \# | 0.99 | C1(2-A) |
| $\mathrm{H} 2(\mathrm{~s} 2)+\mathrm{HC4}(\mathrm{~d} 1)$ | \# | 0.65 | $\mathrm{CS}\left(2-\mathrm{A}^{\prime}\right)$ |
| $\mathrm{H}(\mathrm{d} 2)+\mathrm{H} 2 \mathrm{C} 4(\mathrm{~s} 1)$ | \# | 1.63 | $\mathrm{CS}\left(2-\mathrm{A}^{\prime}\right)$ |
| $\mathrm{H}(\mathrm{d} 2)+\mathrm{H} 2 \mathrm{C} 4(\mathrm{~s} 1)$ | \# | 0.94 | C1(2-A) |
| $\mathrm{H} 2(\mathrm{~s} 2)+\mathrm{HC4}(\mathrm{~d} 1)$ | \# | 0.33 | C1(2-A) |
| $\mathrm{H}(\mathrm{d} 2)+\mathrm{H} 2 \mathrm{C} 4(\mathrm{~s} 1)$ | \# | . 61 | C1(2-A) |
| $\mathrm{H}(\mathrm{d} 2)+\mathrm{H} 2 \mathrm{C} 4(\mathrm{~s} 1)$ | \# | 0.48 | $\mathrm{CS}\left(2-\mathrm{A}{ }^{\prime \prime}\right)$ |
| $\mathrm{H}(\mathrm{d} 2)+\mathrm{H} 2 \mathrm{C} 4(\mathrm{~s} 1)$ | \# | 0.65 | CS(2-A") |
| $\mathrm{H} 2(\mathrm{~s} 2)+\mathrm{HC4}(\mathrm{~d} 1)$ | \# | 0.90 | C1(2-A) |
| $\mathrm{H} 2(\mathrm{~s} 2)+\mathrm{HC4}(\mathrm{~d} 1)$ | \# | 0.08 | $\mathrm{C} 3 \mathrm{~V}(4-\mathrm{A} 1)$ |
| $\mathrm{H} 2(\mathrm{~s} 2)+\mathrm{HC} 4(\mathrm{~d} 1)$ | \# | 0.95 | $\mathrm{CS}\left(4-\mathrm{A}{ }^{\prime \prime}\right)$ |
| $\mathrm{H}(\mathrm{d} 2)+\mathrm{H} 2 \mathrm{C} 4(\mathrm{~s} 8)$ | \# | 0.22 | $\mathrm{CS}\left(4-\mathrm{A}{ }^{\prime \prime}\right)$ |
| HC2(d3)+ $\mathrm{H} 2 \mathrm{C} 2(\mathrm{~s} 2)$ | \# | 0.21 | $\mathrm{CS}\left(4-\mathrm{A}{ }^{\prime \prime}\right)$ |
| $\mathrm{H} 2(\mathrm{~s} 2)+\mathrm{HC4}(\mathrm{~d} 1)$ | \# | 0.08 | C1(4-A) |
| $\mathrm{H} 2(\mathrm{~s} 2)+\mathrm{HC} 4(\mathrm{~d} 2)$ | \# | 0.03 | C1(4-A) |
| $\mathrm{H}(\mathrm{d} 2)+\mathrm{H} 2 \mathrm{C} 4(\mathrm{~s} 8)$ | \# | 0.24 | $\mathrm{CS}\left(4-\mathrm{A}{ }^{\prime \prime}\right)$ |
| HC2(d3)+H2C2(s2) | \# | 0.06 | $\mathrm{CS}\left(4-\mathrm{A}{ }^{\prime \prime}\right)$ |
| $\mathrm{H}(\mathrm{d} 2)+\mathrm{H} 2 \mathrm{C} 4(\mathrm{~s} 2)$ | \# | 0.00 | C1(4-A) |
| H2 (s2) $+\mathrm{HC} 4(\mathrm{~d} 6$ ) | \# | 0.03 | C1(4-A) |
| $\mathrm{H} 2(\mathrm{~s} 2)+\mathrm{HC4}(\mathrm{~d} 1)$ | \# | 0.75 | $\mathrm{C} 2 \mathrm{~V}(4-\mathrm{B} 2)$ |
| $\mathrm{HC2}(\mathrm{~d} 3)+\mathrm{H} 2 \mathrm{C} 2(\mathrm{~s} 2)$ | \# | 0.39 | $\mathrm{CS}\left(4-\mathrm{A}^{\prime}\right)$ |
| $\mathrm{H}(\mathrm{d} 2)+\mathrm{H} 2 \mathrm{C} 4(\mathrm{~s} 8$ ) | \# | 0.39 | $\mathrm{CS}\left(4-\mathrm{A}{ }^{\prime \prime}\right)$ |
| $\mathrm{CO}(\mathrm{s} 2)+\mathrm{H} 2 \mathrm{C} 3(\mathrm{~s} 2)$ | \# | 0.07 | $\mathrm{C} 1(1-\mathrm{A})$ |
| $\mathrm{CO}(\mathrm{s} 2)+\mathrm{H} 2 \mathrm{C} 3(\mathrm{t} 3$ ) | \# | 0.80 | $\mathrm{C} 1(1-\mathrm{A})$ |
| $\mathrm{H} 2(\mathrm{~s} 2)+\mathrm{H} 2 \mathrm{C} 4(\mathrm{~s} 8)$ | \# | 1.66 | $\mathrm{CS}\left(1-\mathrm{A}^{\prime}\right)$ |
| H2(s2) $+\mathrm{H} 2 \mathrm{C} 4(\mathrm{~s} 8)$ | \# | 1.30 | C1(1-A) |
| H2C2(s2) $+\mathrm{H} 2 \mathrm{C} 2(\mathrm{~s} 2)$ | \# | 0.35 | C1(1-A) |
| H2C2(s2) $+\mathrm{H} 2 \mathrm{C} 2(\mathrm{~s} 2)$ | \# | 0.91 | $\mathrm{C} 2 \mathrm{~V}(1-\mathrm{A} 1)$ |
| H2(s2)+H2C4(s8) | \# | 0.70 | $\mathrm{C} 1(1-\mathrm{A})$ |
| H2C2(s2)+H2C2(s2) | \# | 1.91 | $\mathrm{CS}\left(1-\mathrm{A}^{\prime}\right)$ |
| $\mathrm{H}(\mathrm{d} 2)+\mathrm{H} 3 \mathrm{C} 4(\mathrm{~d} 2)$ | \# | 0.46 | $\mathrm{CS}\left(1-\mathrm{A}^{\prime}\right)$ |


| H4C4(s11) | 0 | 1 | 1 |  |
| :---: | :---: | :---: | :---: | :---: |
| H4C4(s12) | 0 | 1 | 1 | 1 |
| H4C4(s13) | 0 | 1 | 1 | 4 |
| H4C4(s14) | 0 | 1 | 1 | 1 |
| H4C4(s15) | 0 | 1 | 1 | 1 |
| H4C4(s17) | 0 | 1 | 1 | 1 |
| H4C4(s18) | 0 | 1 | 1 | 12 |
| H4C4(s19) | 0 | 1 | 1 | 4 |
| H4C4(t1) | 0 | 3 | 1 | 1 |
| H4C4(t3) | 0 | 31 | 1 | 1 |
| H4C4(t4) | 0 | 3 | 1 | 1 |
| H4C4(t5) | 0 | 3 | 1 | 1 |
| H4C4(t6) | 0 | 3 | 1 | 1 |
| H4C4(t7) | 0 | 3 | 1 | 2 |
| H4C4(t8) | , | 3 | 1 | 1 |
| H4C4(t9) | 0 | 31 |  | 1 |
| H4C4(t10) | 0 | 3 | 1 | 1 |
| H4C4(t12) | 0 | 3 | 1 | 1 |
| H4C4(t13) | 0 | 3 | 1 | 1 |
| H4C4(t14) | 0 | 3 | 1 | 1 |
| H4C4(t15) | 0 | 3 | 1 | 2 |
| H4C4(t16) | 0 | 3 | 1 | 2 |
| H4C4(t17) | 0 | 3 | 1 | 1 |
| H4C4(t18) | 0 | 3 | 1 | 1 |
| H4C4(t19) | 0 | 3 | 1 | 4 |
| H4C3O(s2) | 0 | 1 | 1 | 1 |
| H4C3O(s3) | 0 | 1 | 1 | 1 |
| H4C3O(s4) | 0 | 1 | 1 | 1 |
| H4C3O(t2) | 0 | 3 | 1 | 1 |
| $\mathrm{H} 3 \mathrm{C} 4 \mathrm{O}(\mathrm{d} 1)$ | 0 | 2 | 1 | 1 |
| $\mathrm{H} 3 \mathrm{C} 4 \mathrm{O}(\mathrm{d} 2)$ | 0 | 2 | 1 | 1 |
| C4H4O(s1) | 0 | 1 | 1 | 1 |
| $\mathrm{C} 4 \mathrm{H} 4 \mathrm{O}(\mathrm{s} 2)$ | 0 | 1 | 1 | 2 |
| C4H4O(s3) | 0 | 1 | 1 | 1 |
| C4H4O(s4) | 0 | 1 | 1 | 2 |
| C4H4O(s5) | 0 | 1 | 1 | 1 |
| C4H4O(s6) | 0 | 1 | 1 | 1 |
| C4H4O(s7) | 0 | 1 | 1 | 1 |
| C4H4O(s8) | 0 | 1 | 1 | 1 |
| C4H4O(s9) | 0 | 1 | 1 | 1 |
| C4H4O(s10) |  | ) 1 | 1 |  |
| C4H4O(s11) |  | 1 | 1 |  |
| C4H4O(s12) | 0 | ) 1 | 1 |  |
| C4H4O(s13) |  | ) 1 | 1 |  |
| C4H4O(s14) | 0 | 0 | 1 |  |
| C4H4O(s15) | 0 | 0 | 1 |  |
| C4H4O(s16) |  | ) 1 | 1 |  |
| C4H4O(s17) | 0 | 0 | 1 |  |
| C4H4O(s18) | 0 | 0 | 1 |  |
| C4H4O(s19) | 0 | ) 1 | 1 |  |
| C4H4O(s20) |  | ) 1 |  |  |
| C4H4O(s21) |  | 1 |  |  |
| $\mathrm{Hp}(\mathrm{s} 1)$ | 1 | 1 |  | 1 |
| Cp(d2) | 2 | 3 |  | 1 |
| Cp(q1) | 14 | 3 |  | 1 |
| $\mathrm{Op}(\mathrm{d} 2)$ | 12 | 5 |  | 1 |
| $\mathrm{Op}(\mathrm{q} 1)$ | 14 | 1 |  | 1 |
| H2p(d1) |  |  |  | 2 |
| $\mathrm{HCp}(\mathrm{s} 1)$ | 11 | 11 |  | 1 |
| $\mathrm{HCp}(\mathrm{t} 1)$ | 13 | 3 |  | 1 |
| HOp(s1) | 11 | 1 |  | 1 |
| HOp(t1) | 13 | 31 |  | 1 |
| C2p(d4) | 12 | 2 |  | 2 |
| C2p(q1) | 14 | 41 |  | 2 |
| COp(d3) | 12 | 21 |  | 1 |
| COp(q8) | 14 | 2 |  | 1 |
| H3p ( s 7 ) | 11 | 1 |  | 2 |
| $\mathrm{H} 2 \mathrm{Cp}(\mathrm{d} 18)$ |  | 2 |  | 2 |
| $\mathrm{H} 2 \mathrm{Cp}(\mathrm{q} 1)$ | 1 | 41 |  | 2 |
| $\mathrm{H} 2 \mathrm{Op}(\mathrm{d} 5)$ | 1 | 21 | 1 | 2 |
| H2Op(d6) | 1 | 21 | 1 | 2 |
| HC2p(s2) | 1 | 11 | 1 | 1 |
| HC2p(t1) | 1 | 32 | 2 | 1 |
| HCOp(s1) | 1 | 11 | 1 | 1 |
| HCOp( s2) | 1 | 11 | 1 | 1 |
| HCOp( t2) | 1 | 31 | 1 | 1 |
| HCOp(t3) | 1 | 31 |  | 1 |
| C3p (d1) | 12 | 21 |  | 2 |
| C3p(d2) | 12 | 2 |  | 1 |
| C3p(q3) | 4 |  |  | 2 |
| C3p(q4) | 4 | 41 |  | 6 |



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| -3085.130738 |
| -3092.280087 |
| -3092.045156 |
| -3090.591166 |
| -3091.639940 |


| H2(s2) $+\mathrm{H} 2 \mathrm{C} 4(\mathrm{~s} 8)$ | \# | 1.32 | $\mathrm{C} 1(1-\mathrm{A})$ |
| :---: | :---: | :---: | :---: |
| H2(s2) $+\mathrm{H} 2 \mathrm{C} 4(\mathrm{~s} 8)$ | \# | 1.72 | $\mathrm{CS}\left(1-\mathrm{A}^{\prime}\right)$ |
| H2C2(s2)+H2C2(s2) | \# | 0.21 | D2H(1-AG) |
| H2(s2) $+\mathrm{H} 2 \mathrm{C} 4(\mathrm{~s} 8)$ | \# | 1.72 | C1(1-A) |
| H2(s2) $+\mathrm{H} 2 \mathrm{C} 4(\mathrm{~s} 8)$ | \# | 1.41 | $\mathrm{CS}\left(1-\mathrm{A}^{\prime}\right)$ |
| H2(s2) $+\mathrm{H} 2 \mathrm{C} 4(\mathrm{~s} 8)$ | \# | 0.66 | $\mathrm{CS}\left(1-\mathrm{A}^{\prime}\right)$ |
| $\mathrm{H} 2(\mathrm{~s} 2)+\mathrm{H} 2 \mathrm{C} 4(\mathrm{~s} 8)$ | \# | 0.99 | $\mathrm{TD}(1-\mathrm{A} 1)$ |
| H2C2(s2)+H2C2(s2) | \# | 1.75 | D2H(1-AG) |
| H2(s2) $+\mathrm{H} 2 \mathrm{C} 4(\mathrm{~s} 8$ ) | \# | 0.18 | $\mathrm{CS}\left(3-\mathrm{A}^{\prime \prime}\right)$ |
| $\mathrm{H}(\mathrm{d} 2)+\mathrm{H} 3 \mathrm{C} 4(\mathrm{~d} 2)$ | \# | 0.64 | C1(3-A) |
| $\mathrm{H} 2(\mathrm{~s} 2)+\mathrm{H} 2 \mathrm{C} 4(\mathrm{~s} 8)$ | \# | 1.14 | C1(3-A) |
| $\mathrm{H} 2(\mathrm{~s} 2)+\mathrm{H} 2 \mathrm{C} 4(\mathrm{~s} 8)$ | \# | 0.54 | C1(3-A) |
| $\mathrm{H} 2(\mathrm{~s} 2)+\mathrm{H} 2 \mathrm{C} 4(\mathrm{~s} 8)$ | \# | 1.36 | $\mathrm{CS}\left(3-\mathrm{A}{ }^{\prime \prime}\right)$ |
| H2 (s2) +H 2 C 4 ( s 8 ) | \# | 0.42 | $\mathrm{C} 2 \mathrm{H}(3-\mathrm{BU})$ |
| $\mathrm{H}(\mathrm{d} 2)+\mathrm{H} 3 \mathrm{C} 4(\mathrm{~d} 2)$ | \# | 0.20 | C1(3-A) |
| H2(s2) $+\mathrm{H} 2 \mathrm{C} 4(\mathrm{~s} 7$ ) | \# | 0.28 | C1(3-A) |
| H2C2(s3)+H2C2(s3) | \# | 0.04 | C1(3-A) |
| $\mathrm{H}(\mathrm{d} 2)+\mathrm{H} 3 \mathrm{C} 4(\mathrm{~d} 2)$ | \# | 0.64 | C1(3-A) |
| H2(s2)+H2C4(s1) | \# | 0.03 | $\mathrm{CI}(3-\mathrm{AG})$ |
| $\mathrm{H} 2(\mathrm{~s} 2)+\mathrm{H} 2 \mathrm{C} 4(\mathrm{~s} 8)$ | \# | 0.88 | $\mathrm{CS}\left(3-\mathrm{A}{ }^{\prime \prime}\right)$ |
| H2(s2)+H2C4(s8) | \# | 0.78 | $\mathrm{C} 2 \mathrm{~V}(3-\mathrm{A} 2)$ |
| $\mathrm{H}(\mathrm{d} 2)+\mathrm{H} 3 \mathrm{C} 4(\mathrm{~d} 2)$ | \# | 0.37 | $\mathrm{C} 2 \mathrm{~V}(3-\mathrm{B} 2)$ |
| $\mathrm{H}(\mathrm{d} 2)+\mathrm{H} 3 \mathrm{C} 4(\mathrm{~d} 2)$ | \# | 0.05 | C1(3-A) |
| $\mathrm{H}(\mathrm{d} 2)+\mathrm{H} 3 \mathrm{C} 4(\mathrm{~d} 2)$ | \# | 0.44 | CS(3-A") |
| H2C2(s2)+H2C2(s2) | \# | 0.28 | D2D(3-A1) |
| H2C2 (s2) + $\mathrm{H} 2 \mathrm{CO}(\mathrm{s} 1)$ | \# | 0.75 | C1(1-A) |
| H2C2(s2) + $\mathrm{H} 2 \mathrm{CO}(\mathrm{s} 1)$ | \# | 0.10 | C1(1-A) |
| $\mathrm{H} 2 \mathrm{O}(\mathrm{s} 2)+\mathrm{H} 2 \mathrm{C} 3(\mathrm{~s} 2)$ | \# | 0.12 | C1(1-A) |
| $\mathrm{H} 2 \mathrm{O}(\mathrm{s} 2)+\mathrm{H} 2 \mathrm{C} 3(\mathrm{~s} 2)$ | \# | 0.12 | C1(3-A) |
| $\mathrm{CO}(\mathrm{s} 2)+\mathrm{H} 3 \mathrm{C} 3$ (d2) | \# | 0.75 | CS(2-A") |
| $\mathrm{CO}(\mathrm{s} 2)+\mathrm{H} 3 \mathrm{C} 3(\mathrm{~d} 2)$ | \# | 1.41 | C1(2-A) |
| $\mathrm{CO}(\mathrm{s} 2)+\mathrm{H} 4 \mathrm{C} 3$ ( s3) | \# | 0.27 | $\mathrm{CS}\left(1-\mathrm{A}^{\prime}\right)$ |
| H2C2 (s2) + $\mathrm{H} 2 \mathrm{C} 2 \mathrm{O}(\mathrm{s} 5)$ | \# | 0.91 | $\mathrm{C} 2 \mathrm{~V}(1-\mathrm{A} 1)$ |
| H2C2(s2)+H2C2O(s5) | \# | 0.15 | $\mathrm{CS}\left(1-\mathrm{A}^{\prime}\right)$ |
| $\mathrm{CO}(\mathrm{s} 2)+\mathrm{H} 4 \mathrm{C} 3(\mathrm{~s} 3)$ | \# | 1.18 | $\mathrm{C} 2 \mathrm{~V}(1-\mathrm{A} 1)$ |
| $\mathrm{CO}(\mathrm{s} 2)+\mathrm{H} 4 \mathrm{C} 3$ ( s3) | \# | 0.05 | $\mathrm{CS}\left(1-\mathrm{A}^{\prime}\right)$ |
| H2C2(s2)+ $\mathrm{H} 2 \mathrm{C} 2 \mathrm{O}(\mathrm{s} 5)$ | \# | 0.54 | $\mathrm{CS}\left(1-\mathrm{A}^{\prime}\right)$ |
| $\mathrm{CO}(\mathrm{s} 2)+\mathrm{H} 4 \mathrm{C} 3$ ( s3 ) | \# | 0.08 | $\mathrm{C} 1(1-\mathrm{A})$ |
| $\mathrm{CO}(\mathrm{s} 2)+\mathrm{H} 4 \mathrm{C} 3$ (s3) | \# | 0.21 | $\mathrm{CS}\left(1-\mathrm{A}^{\prime}\right)$ |
| $\mathrm{H} 2 \mathrm{O}(\mathrm{s} 2)+\mathrm{H} 2 \mathrm{C} 4(\mathrm{~s} 1)$ | \# | 0.19 | $\mathrm{CS}\left(1-\mathrm{A}^{\prime}\right)$ |
| $\mathrm{CO}(\mathrm{s} 2)+\mathrm{H} 4 \mathrm{C} 3(\mathrm{~s} 3)$ | \# | 0.40 | $0 \mathrm{CS}\left(1-\mathrm{A}^{\prime}\right)$ |
| H2C2(s2)+ $\mathrm{H} 2 \mathrm{C} 2 \mathrm{O}(\mathrm{s} 5)$ | \# | 0.81 | $1 \mathrm{CS}\left(1-\mathrm{A}^{\prime}\right)$ |
| H2C2(s2)+ $\mathrm{H} 2 \mathrm{C} 2 \mathrm{O}(\mathrm{s} 5)$ | \# | 0.79 | $9 \mathrm{CS}\left(1-\mathrm{A}^{\prime}\right)$ |
| H2C2(s2)+ $\mathrm{H} 2 \mathrm{C} 2 \mathrm{O}(\mathrm{s} 5)$ | \# | 0.09 | $9 \mathrm{CS}\left(1-\mathrm{A}^{\prime}\right)$ |
| H2C2(s2)+ $\mathrm{H} 2 \mathrm{C} 2 \mathrm{O}(\mathrm{s} 5)$ | \# | 0.15 | $5 \mathrm{CS}\left(1-\mathrm{A}^{\prime}\right)$ |
| H2C2(s2) $+\mathrm{H} 2 \mathrm{C} 2 \mathrm{O}(\mathrm{s} 5)$ | \# | 0.68 | $8 \mathrm{C} 1(1-\mathrm{A})$ |
| H2C2(s2)+H2C2O(s5) | \# | 0.81 | $1 \mathrm{C}(1-\mathrm{A})$ |
| $\mathrm{CO}(\mathrm{s} 2)+\mathrm{H} 4 \mathrm{C} 3(\mathrm{~s} 3)$ | \# | 0.15 | $5 \mathrm{CS}\left(1-\mathrm{A}^{\prime}\right)$ |
| $\mathrm{CO}(\mathrm{s} 2)+\mathrm{H} 4 \mathrm{C} 3$ (s3) |  | 0.27 | $7 \mathrm{CS}\left(1-\mathrm{A}^{\prime}\right)$ |
| $\mathrm{H} 2 \mathrm{O}(\mathrm{s} 2)+\mathrm{H} 2 \mathrm{C} 4(\mathrm{~s} 1)$ | \# | 0.18 | $8 \mathrm{CS}\left(1-\mathrm{A}^{\prime}\right)$ |
| $\mathrm{H} 2 \mathrm{O}(\mathrm{s} 2)+\mathrm{H} 2 \mathrm{C} 4(\mathrm{~s} 1)$ |  | 0.19 | $9 \mathrm{CS}\left(1-\mathrm{A}^{\prime}\right)$ |
| H2C2(s2)+H2C2O(s5) | \# | 0.79 | $9 \mathrm{CS}\left(1-\mathrm{A}^{\prime}\right)$ |
|  |  |  | O3(1-S) |
|  |  |  | O3(2-P) |
|  |  |  | O3(4-P) |
|  | \# |  | O3(2-D) |
|  |  |  | O3(4-S) |
| $\mathrm{H}(\mathrm{d} 2)+\mathrm{Hp}(\mathrm{s} 1)$ | \# | 2.92 D | D*H(2-SGG) |
| $\mathrm{H}(\mathrm{d} 2)+\mathrm{Cp}(\mathrm{d} 2)$ | \# | 4.21 C | $\mathrm{C} * \mathrm{~V}(1-\mathrm{SG})$ |
| $\mathrm{H}(\mathrm{d} 2)+\mathrm{Cp}(\mathrm{d} 2)$ | \# | 3.30 C | $\mathrm{C} * \mathrm{~V}(3-\mathrm{PI})$ |
| $\mathrm{Hp}(\mathrm{s} 1)+\mathrm{O}(\mathrm{t} 1)$ | \# | 2.05 C | $\mathrm{C} * \mathrm{~V}(1-\mathrm{SG})$ |
| $\mathrm{Hp}(\mathrm{s} 1)+\mathrm{O}(\mathrm{t} 1)$ | \# | 5.06 C | $\mathrm{C} * \mathrm{~V}(3-\mathrm{SG})$ |
| $\mathrm{C}(\mathrm{t} 1)+\mathrm{Cp}(\mathrm{d} 2)$ | \# | 4.30 D | D*H(2-PIU) |
| $\mathrm{C}(\mathrm{t} 1)+\mathrm{Cp}(\mathrm{d} 2)$ | \# | 5.72 D | D*H(4-SGG) |
| $\mathrm{Cp}(\mathrm{d} 2)+\mathrm{O}(\mathrm{t} 1)$ | \# | 8.29 C | $\mathrm{C} * \mathrm{~V}(2-\mathrm{SG})$ |
| $\mathrm{Cp}(\mathrm{d} 2)+\mathrm{O}(\mathrm{t} 1$ ) | \# | 1.60 C | $\mathrm{C} * \mathrm{~V}(4-\mathrm{PI})$ |
| $\mathrm{Hp}(\mathrm{s} 1)+\mathrm{H} 2(\mathrm{~s} 2)$ | \# | 4.53 | $\mathrm{C} 2 \mathrm{~V}(1-\mathrm{A} 1)$ |
| $\mathrm{H} 2(\mathrm{~s} 2)+\mathrm{Cp}(\mathrm{d} 2)$ | \# | 4.64 | $\mathrm{C} 2 \mathrm{~V}(2-\mathrm{A} 1)$ |
| $\mathrm{H} 2(\mathrm{~s} 2)+\mathrm{Cp}(\mathrm{d} 2)$ | \# | 0.76 | $\mathrm{C} 2 \mathrm{~V}(4-\mathrm{A} 2)$ |
| $\mathrm{H}(\mathrm{d} 2)+\mathrm{HOp}(\mathrm{t} 1$ ) | \# | 5.84 | $\mathrm{C} 2 \mathrm{~V}(2-\mathrm{B} 1)$ |
| $\mathrm{H}(\mathrm{d} 2)+\mathrm{HOp}(\mathrm{t} 1$ ) | \# | 5.47 | $\mathrm{C} 2 \mathrm{~V}(2-\mathrm{B} 1)$ |
| $\mathrm{H}(\mathrm{d} 2)+\mathrm{C} 2 \mathrm{p}(\mathrm{q} 1)$ | \# | 4.07 | $\mathrm{CS}\left(1-\mathrm{A}^{\prime}\right)$ |
| $\mathrm{H}(\mathrm{d} 2)+\mathrm{C} 2 \mathrm{p}(\mathrm{q} 1$ ) | \# | 5.55 | $\mathrm{C} * \mathrm{~V}(3-\mathrm{PI})$ |
| $\mathrm{Hp}(\mathrm{s} 1)+\mathrm{CO}(\mathrm{s} 2)$ | \# | 6.33 | $\mathrm{C} * \mathrm{~V}(1-\mathrm{SG})$ |
| $\mathrm{Hp}(\mathrm{s} 1)+\mathrm{CO}(\mathrm{s} 2)$ | \# | 4.63 | $\mathrm{C} * \mathrm{~V}(1-\mathrm{SG})$ |
| $\mathrm{Hp}(\mathrm{s} 1)+\mathrm{CO}(\mathrm{s} 2)$ | \# | 0.57 | $\mathrm{CS}\left(3-\mathrm{A}^{\prime}\right)$ |
| $\mathrm{Hp}(\mathrm{s} 1)+\mathrm{CO}(\mathrm{s} 2)$ | \# | 0.74 | $\mathrm{CS}\left(3-\mathrm{A}^{\prime}\right)$ |
| $\mathrm{Cp}(\mathrm{d} 2)+\mathrm{C} 2(\mathrm{t} 2)$ | \# | 7.30 | $\mathrm{C} 2 \mathrm{~V}(2-\mathrm{B} 2)$ |
| $\mathrm{Cp}(\mathrm{d} 2)+\mathrm{C} 2(\mathrm{t} 2)$ | \# | 7.06 | $\mathrm{CS}\left(2-\mathrm{A}^{\prime}\right)$ |
| $\mathrm{Cp}(\mathrm{d} 2)+\mathrm{C} 2(\mathrm{t} 2)$ | \# | 5.61 D | D*H(4-PIU) |
| $\mathrm{Cp}(\mathrm{d} 2)+\mathrm{C} 2(\mathrm{t} 2$ ) | \# | 6.66 D | D3H(4-A1') |



| C2O. q1.m2-1.rxyz | -4104.357894 |
| :---: | :---: |
| C2O. $\mathrm{q} 1 . \mathrm{m} 4-2 . \mathrm{rxyz}$ | -4105.663626 |
| H4.q1.m2-1.rxyz | -50.771232 |
| H3C. $\mathrm{q} 1 . \mathrm{m} 1-1 . \mathrm{rxyz}$ | -1074.618094 |
| H3C. $\mathrm{q} 1 . \mathrm{m} 3-1 . \mathrm{rxyz}$ | -1071.017296 |
| H2C2.q1.m2-1.rxyz | -2093.702078 |
| H2C2.q1.m2-2.rxyz | -2091.809253 |
| H2C2.q1.m4-2.rxyz | -2090.207233 |
| H2C2. q1.m4-3.rxyz | -2090.548560 |
| H2C2.q1.m4-4.rxyz | -2090.265931 |
| H2CO. q1.m2-3.rxyz | -3105.479226 |
| H2CO. q1.m2-5.rxyz | -3103.296782 |
| H2CO. q1.m4-1.rxyz | -3100.775774 |
| H2CO. q1.m4-3.rxyz | -3100.339343 |
| HC3. q1.m1-1.rxyz | -3109.736543 |
| HC3.q1.m1-2.rxyz | -3109.736537 |
| HC3. q1.m1-3.rxyz | -3112.161925 |
| HC3.q1.m3-1.rxyz | -3110.621832 |
| HC3.q1.m3-2.rxyz | -3111.285088 |
| HC2O. q1.m1-1.rxyz | -4121.973057 |
| HC2O. q1.m1-2.rxyz | -4120.216950 |
| HC2O. q1.m1-3.rxyz | -4124.295153 |
| HC2O. q1.m1-4.rxyz | -4122.138572 |
| HC2O. q1.m1-5.rxyz | -4123.233575 |
| HC2O. q1.m3-1.rxyz | -4122.110160 |
| HC2O. q1.m3-2.rxyz | -4121.898404 |
| HC2O.q1.m3-4.rxyz | -4122.545145 |
| C4.q1.m2-1.rxyz | -4128.427168 |
| C4.q1.m2-2.rxyz | -4128.147757 |
| C4.q1.m4-1.rxyz | -4127.823323 |
| C4.q1.m4-2.rxyz | -4127.279733 |
| C3O.q1.m2-2.rxyz | -5140.364237 |
| C3O. $\mathrm{q} 1 . \mathrm{m} 2-3 . \mathrm{rxyz}$ | -5144.172766 |
| C3O.q1.m2-4.rxyz | -5139.751725 |
| C3O.q1.m4-4.rxyz | -5140.161008 |
| C3O.q1.m4-5.rxyz | -5140.481765 |
| H4C. q1.m2-1.rxyz | -1090.288860 |
| H3C2. q1.m1-1.rxyz | -2109.777475 |
| H3C2.q1.m1-2.rxyz | -2111.824893 |
| H3C2.q1.m3-2.rxyz | -2109.963286 |
| H3C2.q1.m3-3.rxyz | -2107.878030 |
| H3CO. q1.m1-3.rxyz | -3121.047337 |
| H3CO. q1.m3-2.rxyz | -3120.637235 |
| H3CO. q1.m3-8.rxyz | -3120.496623 |
| H2C3. q1.m2-1.rxyz | -3130.539108 |
| H2C3. q1.m2-2.rxyz | -3128.978905 |
| H2C3.q1.m2-3.rxyz | -3130.707428 |
| H2C3. q1.m4-1.rxyz | -3127.539259 |
| H2C3. q1.m4-2.rxyz | -3127.956762 |
| H2C3.q1.m4-4.rxyz | -3126.590137 |
| H2C3. q1.m4-5.rxyz | -3126.438218 |
| H2C2O. $\mathrm{q} 1 . \mathrm{m} 2-2 . \mathrm{rxyz}$ | -4142.389598 |
| H2C2O. $\mathrm{q} 1 . \mathrm{m} 2-3 . \mathrm{rxyz}$ | -4144.194004 |
| H2C2O. $11 . \mathrm{m} 4-4 . \mathrm{rxyz}$ | -4139.158811 |
| H2C2O. $\mathrm{q} 1 . \mathrm{m} 4-5 . \mathrm{rxyz}$ | -4139.415957 |
| H2C2O. 1 1.m4-6.rxyz | -4139.693669 |
| H2C2O. 1 1.m4-8.rxyz | -4140.150401 |
| HC4.q1.m1-1.rxyz | -4147.382699 |
| HC4.q1.m1-3.rxyz | -4146.442738 |
| HC4.q1.m1-4.rxyz | -4147.414890 |
| HC4.q1.m1-5.rxyz | -4146.382843 |
| HC4.q1.m3-3.rxyz | -4146.538043 |
| HC4.q1.m3-4.rxyz | -4146.291846 |
| HC4.q1.m3-5.rxyz | -4146.538028 |
| HC4.q1.m3-6.rxyz | -4146.662846 |
| HC3O. q1.m1-1.rxyz | -5160.834652 |
| HC3O. q1.m1-2.rxyz | -5161.865620 |
| HC3O. q1.m1-3.rxyz | -5164.304223 |
| HC3O. q1.m3-1.rxyz | -5159.346104 |
| HC3O. q1.m3-2.rxyz | -5159.196692 |
| C4O. q1.m2-1.rxyz | -6179.525308 |
| H4C2.q1.m2-1.rxyz | -2124.041604 |
| H4C2.q1.m2-6.rxyz | -2128.892769 |
| H4C2.q1.m4-1.rxyz | -2123.561926 |
| H4CO. q1.m2-3.rxyz | -3139.418728 |
| H3C3.q1.m1-1.rxyz | -3150.021178 |
| H3C3. q1.m1-3.rxyz | -3146.915732 |
| НЗСЗ.q1.m1-9.rxyz | -3148.923926 |
| H3C3. q1.m3-1.rxyz | -3145.784259 |
| H3C3. q1.m3-2.rxyz | -3144.706435 |
| H3C3.q1.m3-3.rxyz | -3145.888564 |


| (d2) $+\mathrm{CO}(\mathrm{s} 2)$ | \# | 1.37 | I) |
| :---: | :---: | :---: | :---: |
| $\mathrm{Cp}(\mathrm{d} 2)+\mathrm{CO}(\mathrm{s} 2)$ | \# | 2.68 | $\mathrm{C} * \mathrm{~V}(4-\mathrm{SG})$ |
| $\mathrm{H}(\mathrm{d} 2)+\mathrm{H} 3 \mathrm{p}(\mathrm{s} 7$ ) | \# | 0.47 | $\mathrm{C} 2 \mathrm{~V}(2-\mathrm{A} 1)$ |
| $\mathrm{H}(\mathrm{d} 2)+\mathrm{H} 2 \mathrm{Cp}(\mathrm{d} 18)$ | \# | 5.61 | D3H(1-A1') |
| $\mathrm{H}(\mathrm{d} 2)+\mathrm{H} 2 \mathrm{Cp}(\mathrm{d} 18)$ | \# | 2.01 | $\mathrm{CS}\left(3-\mathrm{A}{ }^{\prime}\right)$ |
| $\mathrm{H}(\mathrm{d} 2)+\mathrm{HC} 2 \mathrm{p}(\mathrm{t} 1)$ | \# | 6.35 | $\mathrm{D} * \mathrm{H}(2-\mathrm{PIU})$ |
| $\mathrm{H}(\mathrm{d} 2)+\mathrm{HC} 2 \mathrm{p}(\mathrm{t} 1)$ | \# | 4.46 | $\mathrm{CS}\left(2-\mathrm{A}^{\prime}\right)$ |
| $\mathrm{H}(\mathrm{d} 2)+\mathrm{HC} 2 \mathrm{p}(\mathrm{t} 1)$ | \# | 2.85 | $\mathrm{C} 2 \mathrm{H}(4-\mathrm{BG})$ |
| $\mathrm{H}(\mathrm{d} 2)+\mathrm{HC} 2 \mathrm{p}(\mathrm{t} 1)$ | \# | 3.19 | $\mathrm{C} 2 \mathrm{~V}(4-\mathrm{A} 2)$ |
| $\mathrm{H}(\mathrm{d} 2)+\mathrm{HC} 2 \mathrm{p}(\mathrm{t} 1)$ | \# | 2.91 | $\mathrm{C} 2 \mathrm{~V}(4-\mathrm{A} 2)$ |
| $\mathrm{H}(\mathrm{d} 2)+\mathrm{HCOp}(\mathrm{s} 1)$ | \# | 1.09 | $\mathrm{CS}\left(2-\mathrm{A}^{\prime}\right)$ |
| $\mathrm{H}(\mathrm{d} 2)+\mathrm{HCOp}(\mathrm{s} 2)$ | \# | 0.61 | C2V(2-B2) |
| $\mathrm{Cp}(\mathrm{d} 2)+\mathrm{H} 2 \mathrm{O}(\mathrm{s} 2)$ | \# | 1.63 | $\mathrm{CS}\left(4-\mathrm{A}{ }^{\text {" }}\right.$ ) |
| $\mathrm{Cp}(\mathrm{d} 2)+\mathrm{H} 2 \mathrm{O}(\mathrm{s} 2)$ | \# | 1.20 | C1(4-A) |
| $\mathrm{H}(\mathrm{d} 2)+\mathrm{C} 3 \mathrm{p}(\mathrm{d} 1$ ) | \# | 3.79 | $\mathrm{C} 2 \mathrm{~V}(1-\mathrm{A} 1)$ |
| $\mathrm{H}(\mathrm{d} 2)+\mathrm{C} 3 \mathrm{p}(\mathrm{d} 1)$ | \# | 3.79 | $\mathrm{C} 2 \mathrm{~V}(1-\mathrm{A} 1)$ |
| $\mathrm{H}(\mathrm{d} 2)+\mathrm{C} 3 \mathrm{p}(\mathrm{d} 1)$ | \# | 6.21 | $\mathrm{C} * \mathrm{~V}(1-\mathrm{SG})$ |
| $\mathrm{H}(\mathrm{d} 2)+\mathrm{C} 3 \mathrm{p}(\mathrm{d} 1$ ) | \# | 4.67 | $\mathrm{C} * \mathrm{~V}(3-\mathrm{PI})$ |
| $\mathrm{H}(\mathrm{d} 2)+\mathrm{C} 3 \mathrm{p}(\mathrm{d} 1$ ) | \# | 5.34 | $\mathrm{C} 2 \mathrm{~V}(3-\mathrm{B} 2)$ |
| $\mathrm{C}(\mathrm{t} 1)+\mathrm{HCOp}(\mathrm{s} 1)$ | \# | 1.11 | $\mathrm{CS}\left(1-\mathrm{A}^{\prime}\right)$ |
| $\mathrm{HCp}(\mathrm{t} 1)+\mathrm{CO}(\mathrm{s} 2)$ | \# | 0.26 | $\mathrm{CS}\left(1-\mathrm{A}^{\prime}\right)$ |
| $\mathrm{C}(\mathrm{t} 1)+\mathrm{HCOp}(\mathrm{s} 1)$ | \# | 3.43 | $\mathrm{CS}\left(1-\mathrm{A}^{\prime}\right)$ |
| $\mathrm{C}(\mathrm{t} 1)+\mathrm{HCOp}(\mathrm{s} 1)$ | \# | 1.27 | $\mathrm{C} 1(1-\mathrm{A})$ |
| $\mathrm{C}(\mathrm{t} 1)+\mathrm{HCOp}(\mathrm{s} 1)$ | \# | 2.37 | $\mathrm{CS}\left(1-\mathrm{A}^{\prime}\right)$ |
| $\mathrm{C}(\mathrm{t} 1)+\mathrm{HCOp}(\mathrm{s} 1)$ | \# | 1.24 | $\mathrm{CS}\left(3-\mathrm{A}{ }^{\prime \prime}\right)$ |
| $\mathrm{C}(\mathrm{t} 1)+\mathrm{HCOp}(\mathrm{s} 1)$ | \# | 1.03 | $\mathrm{CS}\left(3-\mathrm{A}{ }^{\prime \prime}\right)$ |
| $\mathrm{C}(\mathrm{t} 1)+\mathrm{HCOp}(\mathrm{s} 1)$ | \# | 1.68 | CS(3-A") |
| $\mathrm{Cp}(\mathrm{d} 2)+\mathrm{C} 3(\mathrm{~s} 1)$ | \# | 5.64 | D*H(2-PIG) |
| $\mathrm{Cp}(\mathrm{d} 2)+\mathrm{C} 3(\mathrm{~s} 1)$ | \# | 5.36 | $\mathrm{CS}\left(2-\mathrm{A}^{\prime}\right)$ |
| $\mathrm{Cp}(\mathrm{d} 2)+\mathrm{C} 3(\mathrm{~s} 1)$ | \# | 5.03 | D2H(4-B3U) |
| $\mathrm{Cp}(\mathrm{d} 2)+\mathrm{C} 3(\mathrm{~s} 1)$ | \# | 4.49 | $\mathrm{C} 2 \mathrm{~V}(4-\mathrm{A} 2)$ |
| $\mathrm{C} 2 \mathrm{p}(\mathrm{q} 1)+\mathrm{CO}(\mathrm{s} 2)$ | \# | 1.51 | $\mathrm{C} * \mathrm{~V}(2-\mathrm{SG})$ |
| $\mathrm{C} 2 \mathrm{p}(\mathrm{q} 1)+\mathrm{CO}(\mathrm{s} 2)$ | \# | 5.32 | $\mathrm{C} * \mathrm{~V}(2-\mathrm{SG})$ |
| $\mathrm{C} 2 \mathrm{p}(\mathrm{q} 1)+\mathrm{CO}(\mathrm{s} 2)$ | \# | 0.90 | C1(2-A) |
| $\mathrm{C} 2 \mathrm{p}(\mathrm{q} 1)+\mathrm{CO}(\mathrm{s} 2)$ | \# | 1.30 | C2V(4-A2) |
| $\mathrm{C} 2 \mathrm{p}(\mathrm{q} 1)+\mathrm{CO}(\mathrm{s} 2)$ |  | 1.63 | C1(4-A) |
| $\mathrm{H}(\mathrm{d} 2)+\mathrm{H} 3 \mathrm{Cp}(\mathrm{s} 1)$ | \# | 2.00 | D2D(2-B2) |
| $\mathrm{H}(\mathrm{d} 2)+\mathrm{H} 2 \mathrm{C} 2 \mathrm{p}(\mathrm{d} 1)$ | \# | 2.41 | C3V(1-A1) |
| $\mathrm{H}(\mathrm{d} 2)+\mathrm{H} 2 \mathrm{C} 2 \mathrm{p}$ (d1) | \# | 4.46 | $\mathrm{C} 2 \mathrm{~V}(1-\mathrm{A} 1)$ |
| $\mathrm{H}(\mathrm{d} 2)+\mathrm{H} 2 \mathrm{C} 2 \mathrm{p}$ (d1) | \# | 2.59 | CS(3-A") |
| $\mathrm{H}(\mathrm{d} 2)+\mathrm{H} 2 \mathrm{C} 2 \mathrm{p}$ (d1) | \# | 0.51 | $\mathrm{CS}\left(3-\mathrm{A}{ }^{\prime \prime}\right)$ |
| H3p ( s7) $+\mathrm{CO}(\mathrm{s} 2)$ | \# | 0.03 | $\mathrm{CS}\left(1-\mathrm{A}^{\prime}\right)$ |
| $\mathrm{H}(\mathrm{d} 2)+\mathrm{H} 2 \mathrm{COp}(\mathrm{d} 3$ ) | \# | 1.49 | $\mathrm{CS}\left(3-\mathrm{A}^{\prime \prime}\right)$ |
| $\mathrm{H}(\mathrm{d} 2)+\mathrm{H} 2 \mathrm{COp}(\mathrm{d} 3$ ) | \# | 1.35 | $\mathrm{CS}\left(3-\mathrm{A}{ }^{\prime \prime}\right)$ |
| $\mathrm{H}(\mathrm{d} 2)+\mathrm{HC3p}(\mathrm{~s} 3)$ | \# | 4.71 | D*H(2-PIG) |
| $\mathrm{H}(\mathrm{d} 2)+\mathrm{HC} 3 \mathrm{p}(\mathrm{s} 3)$ | \# | 3.15 | $\mathrm{CS}\left(2-\mathrm{A}^{\prime}\right)$ |
| $\mathrm{H}(\mathrm{d} 2)+\mathrm{HC3p}(\mathrm{~s} 3)$ | \# | 4.88 | C2V(2-A1) |
| $\mathrm{H}(\mathrm{d} 2)+\mathrm{HC3p}(\mathrm{~s} 3)$ | \# | 1.71 | $\mathrm{C} 2 \mathrm{~V}(4-\mathrm{A} 2)$ |
| $\mathrm{H}(\mathrm{d} 2)+\mathrm{HC3p}(\mathrm{~s} 3)$ | \# | 2.13 | C1(4-A) |
| $\mathrm{H}(\mathrm{d} 2)+\mathrm{HC3p}(\mathrm{~s} 3)$ | \# | 0.76 | $\mathrm{C} 2 \mathrm{~V}(4-\mathrm{A} 2)$ |
| $\mathrm{H}(\mathrm{d} 2)+\mathrm{HC3p}(\mathrm{~s} 3)$ | \# | 0.61 | $\mathrm{CS}\left(4-\mathrm{A}{ }^{\prime \prime}\right)$ |
| $\mathrm{H} 2 \mathrm{Cp}(\mathrm{d} 18)+\mathrm{CO}(\mathrm{s} 2)$ | \# | 2.66 | $6 \mathrm{C} 1(2-\mathrm{A})$ |
| $\mathrm{H} 2 \mathrm{Cp}(\mathrm{d} 18)+\mathrm{CO}(\mathrm{s} 2)$ | \# |  | 7 C1(2-A) |
| $\mathrm{HC}(\mathrm{d} 1)+\mathrm{HCOp}(\mathrm{s} 1)$ | \# | 0.96 | $6 \mathrm{CS}\left(4-\mathrm{A}^{\prime \prime}\right)$ |
| $\mathrm{HC}(\mathrm{d} 1)+\mathrm{HCOp}(\mathrm{s} 1)$ | \# | 1.22 | $2 \mathrm{CS}\left(4-\mathrm{A}^{\prime \prime}\right)$ |
| $\mathrm{HC}(\mathrm{d} 1)+\mathrm{HCOp}(\mathrm{s} 1)$ | \# | 1.50 | 0 CS(4-A") |
| H2Cp(d18)+CO(s2) | \# | 0.42 | $2 \mathrm{CS}\left(4-\mathrm{A}^{\prime \prime}\right)$ |
| $\mathrm{C}(\mathrm{t} 1)+\mathrm{HC} 3 \mathrm{p}(\mathrm{s} 3)$ | \# | 5.07 | $\mathrm{C} 2 \mathrm{~V}(1-\mathrm{A} 1)$ |
| $\mathrm{C}(\mathrm{t} 1)+\mathrm{HC3p}(\mathrm{~s} 3)$ | \# | 4.13 | $\mathrm{CS}\left(1-\mathrm{A}^{\prime}\right)$ |
| $\mathrm{C}(\mathrm{t} 1)+\mathrm{HC3p}(\mathrm{~s} 3)$ | \# | 5.10 | $\mathrm{C} * \mathrm{~V}(1-\mathrm{SG})$ |
| $\mathrm{C}(\mathrm{t} 1)+\mathrm{HC3p}(\mathrm{~s} 3)$ | \# | 4.07 | $\mathrm{C} 2 \mathrm{~V}(1-\mathrm{A} 1)$ |
| $\mathrm{C}(\mathrm{t} 1)+\mathrm{HC3p}(\mathrm{~s} 3)$ | \# | 4.23 | $\mathrm{CS}\left(3-\mathrm{A}{ }^{\prime \prime}\right)$ |
| $\mathrm{C}(\mathrm{t} 1)+\mathrm{HC3p}(\mathrm{~s} 3)$ | \# | 3.98 | $\mathrm{C} 2 \mathrm{~V}(3-\mathrm{A} 2)$ |
| $\mathrm{C}(\mathrm{t} 1)+\mathrm{HC3p}(\mathrm{~s} 3)$ | \# | 4.23 | CS(3-A") |
| $\mathrm{C}(\mathrm{t} 1)+\mathrm{HC3p}(\mathrm{~s} 3)$ | \# | 4.35 | $\mathrm{CS}\left(3-\mathrm{A}^{\prime \prime}\right)$ |
| HC2p(t1) $+\mathrm{CO}(\mathrm{s} 2)$ | \# | 2.76 | $\mathrm{C} 1(1-\mathrm{A})$ |
| HC2p(t1) $+\mathrm{CO}(\mathrm{s} 2)$ | \# | 3.79 | $\mathrm{CS}\left(1-\mathrm{A}^{\prime}\right)$ |
| HC2p(t1) $+\mathrm{CO}(\mathrm{s} 2)$ | \# | 6.23 | $\mathrm{C} * \mathrm{~V}(1-\mathrm{SG})$ |
| HC2p(t1) $+\mathrm{CO}(\mathrm{s} 2)$ | \# | 1.27 | $\mathrm{CS}\left(3-\mathrm{A}^{\prime}\right)$ |
| HC2p(t1) $+\mathrm{CO}(\mathrm{s} 2)$ | \# | 1.12 | C1(3-A) |
| $\mathrm{CO}(\mathrm{s} 2)+\mathrm{C} 3 \mathrm{p}(\mathrm{d} 1)$ | \# | 2.86 | $\mathrm{CS}\left(2-\mathrm{A}^{\prime}\right)$ |
| H2(s2) + $\mathrm{H} 2 \mathrm{C} 2 \mathrm{p}(\mathrm{d} 2)$ | \# | 0.13 | $\mathrm{CS}\left(2-\mathrm{A}^{\prime}\right)$ |
| H2(s2) + $\mathrm{H} 2 \mathrm{C} 2 \mathrm{p}(\mathrm{d} 1)$ | \# | 3.09 | D2(2-B3) |
| $\mathrm{H}(\mathrm{d} 2)+\mathrm{H} 3 \mathrm{C} 2 \mathrm{p}$ ( s 1$)$ | \# | 0.12 | $\mathrm{C} 1(4-\mathrm{A})$ |
| $\mathrm{H} 2(\mathrm{~s} 2)+\mathrm{H} 2 \mathrm{COp}(\mathrm{d} 3$ ) | \# | 1.84 | $\mathrm{CS}\left(2-\mathrm{A}{ }^{\prime}\right)$ |
| $\mathrm{H}(\mathrm{d} 2)+\mathrm{H} 2 \mathrm{C} 3 \mathrm{p}(\mathrm{d} 3)$ | \# | 5.65 | D3H(1-A1') |
| $\mathrm{H}(\mathrm{d} 2)+\mathrm{H} 2 \mathrm{C} 3 \mathrm{p}(\mathrm{d} 3)$ | \# | 2.54 | $\mathrm{CS}\left(1-\mathrm{A}^{\prime}\right)$ |
| $\mathrm{H}(\mathrm{d} 2)+\mathrm{H} 2 \mathrm{C} 3 \mathrm{p}(\mathrm{d} 3)$ | \# | 4.55 | $\mathrm{CS}\left(1-\mathrm{A}^{\prime}\right)$ |
| $\mathrm{H}(\mathrm{d} 2)+\mathrm{H} 2 \mathrm{C} 3 \mathrm{p}(\mathrm{d} 3)$ | \# | 1.41 | $\mathrm{CS}\left(3-\mathrm{A}{ }^{\prime \prime}\right)$ |
| $\mathrm{H}(\mathrm{d} 2)+\mathrm{H} 2 \mathrm{C} 3 \mathrm{p}(\mathrm{d} 3)$ | \# | 0.33 | C1(3-A) |
| $\mathrm{H}(\mathrm{d} 2)+\mathrm{H} 2 \mathrm{C} 3 \mathrm{p}(\mathrm{d} 3)$ | \# | 1.51 | CS(3-A ${ }^{\prime}$ ) |



| H3C2O.q1.m1-1.rxyz | -4162.518505 |
| :---: | :---: |
| H3C2O.q1.m1-2.rxyz | -4157.002116 |
| H3C2O.q1.m1-4.rxyz | -4157.922363 |
| H3C2O. q1.m1-5.rxyz | -4160.058913 |
| H3C2O.q1.m1-6.rxyz | -4160.813824 |
| H3C2O. q1.m3-2.rxyz | -4159.101114 |
| H2C4.q1.m2-2.rxyz | -4163.312914 |
| H2C4.q1.m2-3.rxyz | -4166.211464 |
| H2C4.q1.m2-4.rxyz | -4165.296177 |
| H2C4.q1.m2-7.rxyz | -4165.749950 |
| H2C4.q1.m2-9.rxyz | -4166.637317 |
| H2C4.q1.m4-1.rxyz | -4163.851070 |
| H2C4.q1.m4-2.rxyz | -4165.183449 |
| H2C4.q1.m4-4.rxyz | -4164.684310 |
| H2C4.q1.m4-5.rxyz | -4160.918679 |
| H2C4.q1.m4-6.rxyz | -4163.844843 |
| H2C4.q1.m4-7.rxyz | -4164.150404 |
| H2C4.q1.m4-8.rxyz | -4164.454721 |
| H2C4.q1.m4-9.rxyz | -4164.024964 |
| H2C3O. q1.m4-3.rxyz | -5171.490564 |
| HC4O. q1.m1-1.rxyz | -6198.625165 |
| HC4O. q1.m1-2.rxyz | -6194.570185 |
| HC4O. q1.m1-3.rxyz | -6194.243864 |
| HC4O. q1.m1-6.rxyz | -6196.543504 |
| HC4O. q1.m1-7.rxyz | -6192.642583 |
| H4C3.q1.m2-1.rxyz | -3164.567164 |
| H4C3.q1.m2-2.rxyz | -3164.776746 |
| H4C3. $\mathrm{q} 1 . \mathrm{m} 2-3 . \mathrm{rxyz}$ | -3162.954141 |
| H4C3. 1 1.m2-4.rxyz | -3164.472414 |
| H4C3.q1 m2-6.rxyz | -3164.472414 |
| H4C3.q1.m4-1.rxyz | -3161.753281 |
| H4C3. q1.m4-2.rxyz | -3162.740820 |
| H4C3. q1.m4-3.rxyz | -3161.515806 |
| H4C3. q1.m4-4.rxyz | -3162.606689 |
| H4C3.q1.m4-5.rxyz | -3161.194663 |
| H4C3.q1.m4-6.rxyz | -3161.702336 |
| H3C4.q1.m1-1.rxyz | -4183.779001 |
| H3C4.q1.m1-2.rxyz | -4185.752393 |
| H3C4.q1.m1-3.rxyz | -4182.647615 |
| H3C4.q1.m1-5.rxyz | -4184.785199 |
| H3C4.q1.m1-7.rxyz | -4184.234426 |
| H3C4.q1.m1-10.rxyz | -4180.551637 |
| H3C4.q1.m1-11.rxyz | -4180.573191 |
| H3C4.q1.m1-13.rxyz | -4184.804281 |
| H3C4.q1.m1-15.rxyz | -4184.274931 |
| H3C4.q1.m3-1.rxyz | -4182.032425 |
| H3C4.q1.m3-2.rxyz | -4184.392526 |
| H3C4.q1.m3-3.rxyz | -4182.744498 |
| H3C4.q1.m3-4.rxyz | -4181.582626 |
| H3C4.q1.m3-5.rxyz | -4184.083303 |
| H3C4.q1.m3-7.rxyz | -4183.745815 |
| H3C4.q1.m3-8.rxyz | -4180.820135 |
| H3C4.q1.m3-10.rxyz | -4182.420230 |
| H3C4.q1.m3-11.rxyz | -4181.605034 |
| H3C4.q1.m3-12.rxyz | -4183.433032 |
| H3C4.q1.m3-13.rxyz | -4182.214560 |
| H3C4.q1.m3-14.rxyz | -4182.184756 |
| H3C4.q1.m3-15.rxyz | -4181.772141 |
| НЗСЗО.q1.m1-1.rxyz | -5195.202750 |
| НЗСЗО.q1.m1-2.rxyz | -5198.096938 |
| НЗСЗО.q1.m1-5.rxyz | -5197.675208 |
| НЗСЗО.q1.m1-6.rxyz | -5197.675210 |
| H2C4O. q1.m2-1.rxyz | -6211.029970 |
| H2C4O. q1.m2-2.rxyz | -6211.029970 |
| H2C4O.q1.m2-4.rxyz | -6211.029970 |
| H2C4O.q1.m2-5.rxyz | -6211.029970 |
| H2C4O. q1.m2-6.rxyz | -6211.029970 |
| H2C4O.q1.m4-1.rxyz | -6214.214654 |
| H4C4. 1 1.m2-1.rxyz | -4199.981298 |
| H4C4.q1.m2-2.rxyz | -4201.883229 |
| H4C4.q1.m2-3.rxyz | -4201.746386 |
| H4C4.q1.m2-4.rxyz | -4202.874576 |
| H4C4.q1.m2-5.rxyz | -4199.552871 |
| H4C4.q1.m2-6.rxyz | -4202.617769 |
| H4C4.q1.m2-7.rxyz | -4200.520881 |
| H4C4.q1.m2-8.rxyz | -4201.111169 |
| H4C4.q1.m2-9.rxyz | -4198.349090 |
| H4C4.q1.m2-10.rxyz | -4198.349088 |
| H4C4.q1.m2-11.rxyz | -4199.471006 |
| H4C4.q1.m2-12.rxyz | -4200.414074 |
| H4C4.q1.m2-13.rxyz | -4202.486088 |


| H3Cp(s1)+CO(s2) | \# | 3.51 | C3V(1-A1) |
| :---: | :---: | :---: | :---: |
| H2C(t7) + $\mathrm{HCOp}(\mathrm{s} 1)$ | \# | 0.52 | $\mathrm{CS}\left(1-\mathrm{A}^{\prime}\right)$ |
| $\mathrm{H}(\mathrm{d} 2)+\mathrm{H} 2 \mathrm{C} 2 \mathrm{Op}(\mathrm{d} 3$ ) | \# | 0.06 | $\mathrm{CS}\left(1-\mathrm{A}^{\prime}\right)$ |
| H3Cp(s1)+CO(s2) | \# | 1.05 | $\mathrm{CS}\left(1-\mathrm{A}^{\prime}\right)$ |
| H3Cp(s1)+CO(s2) | \# | 1.81 | $\mathrm{CS}\left(1-\mathrm{A}^{\prime}\right)$ |
| H3Cp(s1)+CO(s2) | \# | 0.10 | $\mathrm{CS}\left(3-\mathrm{A}^{\prime \prime}\right)$ |
| $\mathrm{H}(\mathrm{d} 2)+\mathrm{HC4p}(\mathrm{~s} 4)$ | \# | 2.23 | $\mathrm{C} 2 \mathrm{~V}(2-\mathrm{A} 2)$ |
| $\mathrm{H}(\mathrm{d} 2)+\mathrm{HC4p}(\mathrm{~s} 4)$ | \# | 5.13 | $\mathrm{C} 2 \mathrm{~V}(2-\mathrm{B} 1)$ |
| $\mathrm{H}(\mathrm{d} 2)+\mathrm{HC4p}(\mathrm{~s} 4)$ | \# | 4.21 | C1(2-A) |
| $\mathrm{H}(\mathrm{d} 2)+\mathrm{HC} 4 \mathrm{p}(\mathrm{s} 4)$ | \# | 4.67 | $\mathrm{CS}\left(2-\mathrm{A}{ }^{\prime \prime}\right)$ |
| $\mathrm{H}(\mathrm{d} 2)+\mathrm{HC} 4 \mathrm{p}(\mathrm{s} 4)$ | \# | 5.56 | $\mathrm{C} 2 \mathrm{H}(2-\mathrm{AG})$ |
| $\mathrm{H}(\mathrm{d} 2)+\mathrm{HC} 4 \mathrm{p}(\mathrm{s} 4)$ | \# | 2.77 | $\mathrm{CS}\left(4-\mathrm{A}{ }^{\text {" }}\right.$ ) |
| $\mathrm{H}(\mathrm{d} 2)+\mathrm{HC} 4 \mathrm{p}(\mathrm{s} 4)$ | \# | 4.10 | $\mathrm{C} 2 \mathrm{~V}(4-\mathrm{B} 1)$ |
| $\mathrm{H}(\mathrm{d} 2)+\mathrm{HC4p}(\mathrm{~s} 4)$ | \# | 3.60 | C2V(4-A2) |
| $\mathrm{C}(\mathrm{t} 1)+\mathrm{H} 2 \mathrm{C} 3 \mathrm{p}(\mathrm{d} 3)$ | \# | 0.06 | C1(4-A) |
| $\mathrm{H}(\mathrm{d} 2)+\mathrm{HC4p}(\mathrm{~s} 4)$ | \# | 2.76 | C1(4-A) |
| $\mathrm{H}(\mathrm{d} 2)+\mathrm{HC} 4 \mathrm{p}(\mathrm{s} 4)$ | \# | 3.07 | $\mathrm{CS}\left(4-\mathrm{A}{ }^{\text {" }}\right.$ ) |
| $\mathrm{H}(\mathrm{d} 2)+\mathrm{HC4p}(\mathrm{~s} 4)$ | \# | 3.37 | C1(4-A) |
| $\mathrm{H}(\mathrm{d} 2)+\mathrm{HC} 4 \mathrm{p}(\mathrm{s} 4)$ | \# | 2.94 | $\mathrm{C} 2 \mathrm{~V}(4-\mathrm{A} 2)$ |
| $\mathrm{H} 2 \mathrm{Cp}(\mathrm{d} 18)+\mathrm{C} 2 \mathrm{O}(\mathrm{s} 2)$ | \# | 0.02 | C1(4-A) |
| $\mathrm{CO}(\mathrm{s} 2)+\mathrm{HC} 3 \mathrm{p}(\mathrm{s} 3)$ | \# | 2.08 | $\mathrm{CS}\left(1-\mathrm{A}^{\prime}\right)$ |
| $\mathrm{C}(\mathrm{t} 1)+\mathrm{HC3Op}(\mathrm{~s} 3)$ | \# | 0.12 | $\mathrm{CS}\left(1-\mathrm{A}^{\prime}\right)$ |
| $\mathrm{CO}(\mathrm{s} 2)+\mathrm{HC3p}(\mathrm{~s} 1)$ | \# | 0.12 | C1(1-A) |
| $\mathrm{CO}(\mathrm{s} 2)+\mathrm{HC3p}(\mathrm{t} 2)$ | \# | 0.87 | $\mathrm{CS}\left(1-\mathrm{A}^{\prime}\right)$ |
| HCOp(s2)+C3(t1) | \# | 0.27 | C1(1-A) |
| $\mathrm{H}(\mathrm{d} 2)+\mathrm{H} 3 \mathrm{C} 3 \mathrm{p}$ ( s 1 ) | \# | 0.88 | C1(2-A) |
| $\mathrm{H}(\mathrm{d} 2)+\mathrm{H} 3 \mathrm{C} 3 \mathrm{p}$ (s1) | \# | 1.09 | C1(2-A) |
| $\mathrm{H} 2(\mathrm{~s} 2)+\mathrm{H} 2 \mathrm{C} 3 \mathrm{p}(\mathrm{d} 3$ ) | \# | 0.15 | $\mathrm{CS}\left(2-\mathrm{A}{ }^{\prime \prime}\right)$ |
| $\mathrm{H}(\mathrm{d} 2)+\mathrm{H} 3 \mathrm{C} 3 \mathrm{p}$ ( s 1$)$ | \# | 0.78 | $\mathrm{CS}\left(2-\mathrm{A}^{\prime}\right)$ |
| $\mathrm{H}(\mathrm{d} 2)+\mathrm{H} 3 \mathrm{C} 3 \mathrm{p}$ ( s 1 ) | \# | 0.78 | C2(2-B) |
| $\mathrm{H} 2(\mathrm{~s} 2)+\mathrm{H} 2 \mathrm{C} 3 \mathrm{p}(\mathrm{d} 2)$ | \# | 0.68 | $\mathrm{CS}\left(4-\mathrm{A}{ }^{\prime \prime}\right)$ |
| $\mathrm{H} 2(\mathrm{~s} 2)+\mathrm{H} 2 \mathrm{C} 3 \mathrm{p}(\mathrm{d} 1)$ | \# | 0.10 | $\mathrm{C} 2 \mathrm{~V}(4-\mathrm{B} 2)$ |
| $\mathrm{H} 2(\mathrm{~s} 2)+\mathrm{H} 2 \mathrm{C} 3 \mathrm{p}(\mathrm{d} 2)$ | \# | 0.44 | $\mathrm{CS}\left(4-\mathrm{A}{ }^{\text {" }}\right.$ ) |
| $\mathrm{H}(\mathrm{d} 2)+\mathrm{H} 3 \mathrm{C} 3 \mathrm{p}$ ( s 9 ) | \# | 0.02 | C1(4-A) |
| $\mathrm{H} 2(\mathrm{~s} 2)+\mathrm{H} 2 \mathrm{C} 3 \mathrm{p}(\mathrm{d} 2)$ | \# | 0.12 | $\mathrm{CS}\left(4-\mathrm{A}{ }^{\prime \prime}\right)$ |
| $\mathrm{H} 2(\mathrm{~s} 2)+\mathrm{H} 2 \mathrm{C} 3 \mathrm{p}(\mathrm{d} 2)$ | \# | 0.63 | C2(4-B) |
| $\mathrm{H}(\mathrm{d} 2)+\mathrm{H} 2 \mathrm{C} 4 \mathrm{p}(\mathrm{d} 9)$ | \# | 3.47 | $\mathrm{C} 3 \mathrm{~V}(1-\mathrm{A} 1)$ |
| $\mathrm{H}(\mathrm{d} 2)+\mathrm{H} 2 \mathrm{C} 4 \mathrm{p}(\mathrm{d} 9)$ | \# | 5.45 | $\mathrm{C} 2 \mathrm{~V}(1-\mathrm{A} 1)$ |
| $\mathrm{H}(\mathrm{d} 2)+\mathrm{H} 2 \mathrm{C} 4 \mathrm{p}$ (d9) | \# | 2.34 | $\mathrm{C} 1(1-\mathrm{A})$ |
| $\mathrm{H}(\mathrm{d} 2)+\mathrm{H} 2 \mathrm{C} 4 \mathrm{p}$ (d9) | \# | 4.48 | $\mathrm{CS}\left(1-\mathrm{A}^{\prime}\right)$ |
| $\mathrm{H}(\mathrm{d} 2)+\mathrm{H} 2 \mathrm{C} 4 \mathrm{p}$ (d9) | \# | 3.93 | $\mathrm{C} 1(1-\mathrm{A})$ |
| H(d2) + H 2 C 4 p (d9) | \# | 0.25 | $\mathrm{CS}\left(1-\mathrm{A}^{\prime}\right)$ |
| $\mathrm{H}(\mathrm{d} 2)+\mathrm{H} 2 \mathrm{C} 4 \mathrm{p}$ (d9) | \# | 0.27 | $\mathrm{C} 1(1-\mathrm{A})$ |
| $\mathrm{H}(\mathrm{d} 2)+\mathrm{H} 2 \mathrm{C} 4 \mathrm{p}$ (d9) | \# | 4.50 | $\mathrm{C} 2 \mathrm{~V}(1-\mathrm{A} 1)$ |
| $\mathrm{H}(\mathrm{d} 2)+\mathrm{H} 2 \mathrm{C} 4 \mathrm{p}$ (d9) | \# | 3.97 | $\mathrm{C} 1(1-\mathrm{A})$ |
| $\mathrm{H}(\mathrm{d} 2)+\mathrm{H} 2 \mathrm{C} 4 \mathrm{p}$ (d9) | \# | 1.73 | $\mathrm{CS}\left(3-\mathrm{A}{ }^{\prime \prime}\right)$ |
| $\mathrm{H}(\mathrm{d} 2)+\mathrm{H} 2 \mathrm{C} 4 \mathrm{p}$ (d9) | \# | 4.09 | $\mathrm{C} 2 \mathrm{~V}(3-\mathrm{A} 2)$ |
| $\mathrm{H}(\mathrm{d} 2)+\mathrm{H} 2 \mathrm{C} 4 \mathrm{p}$ (d9) | \# | 2.44 | $\mathrm{CS}\left(3-\mathrm{A}{ }^{\text {" }}\right.$ ) |
| $\mathrm{H}(\mathrm{d} 2)+\mathrm{H} 2 \mathrm{C} 4 \mathrm{p}$ (d9) | \# | 1.28 | $\mathrm{CS}\left(3-\mathrm{A}{ }^{\prime \prime}\right)$ |
| $\mathrm{H}(\mathrm{d} 2)+\mathrm{H} 2 \mathrm{C} 4 \mathrm{p}$ (d9) | \# | 3.78 | $\mathrm{CS}\left(3-\mathrm{A}{ }^{\prime \prime}\right)$ |
| $\mathrm{H}(\mathrm{d} 2)+\mathrm{H} 2 \mathrm{C} 4 \mathrm{p}(\mathrm{d} 9)$ | \# | 3.44 | $\mathrm{CS}\left(3-\mathrm{A}^{\prime \prime}\right)$ |
| $\mathrm{H}(\mathrm{d} 2)+\mathrm{H} 2 \mathrm{C} 4 \mathrm{p}(\mathrm{d} 9)$ | \# | 0.52 | C1(3-A) |
| $\mathrm{H}(\mathrm{d} 2)+\mathrm{H} 2 \mathrm{C} 4 \mathrm{p}(\mathrm{d} 9)$ | \# | 2.12 | C1(3-A) |
| $\mathrm{H}(\mathrm{d} 2)+\mathrm{H} 2 \mathrm{C} 4 \mathrm{p}(\mathrm{d} 9)$ | \# | 1.30 | C1(3-A) |
| $\mathrm{H}(\mathrm{d} 2)+\mathrm{H} 2 \mathrm{C} 4 \mathrm{p}(\mathrm{d} 9)$ | \# | 3.13 | CS(3-A") |
| H(d2) +H 2 C 4 p (d9) | \# | 1.91 | $\mathrm{CS}\left(3-\mathrm{A}^{\prime \prime}\right)$ |
| $\mathrm{H}(\mathrm{d} 2)+\mathrm{H} 2 \mathrm{C} 4 \mathrm{p}(\mathrm{d} 9)$ | \# | 1.88 | C1(3-A) |
| $\mathrm{H}(\mathrm{d} 2)+\mathrm{H} 2 \mathrm{C} 4 \mathrm{p}$ (d9) | \# | 1.47 | $\mathrm{CS}\left(3-\mathrm{A}^{\prime}\right)$ |
| H3C2p(t2) +CO( s2) | \# | 0.85 | $\mathrm{CS}\left(1-\mathrm{A}^{\prime}\right)$ |
| H2 (s2) + $\mathrm{HC3Op}(\mathrm{~s} 3$ ) | \# | 1.69 | $\mathrm{CS}\left(1-\mathrm{A}^{\prime}\right)$ |
| H2 (s2) + $\mathrm{HC3Op}(\mathrm{~s} 3$ ) | \# | 1.27 | $\mathrm{CS}\left(1-\mathrm{A}^{\prime}\right)$ |
| $\mathrm{H} 2(\mathrm{~s} 2)+\mathrm{HC3Op}(\mathrm{~s} 3)$ | \# | 1.27 | $\mathrm{CS}\left(1-\mathrm{A}^{\prime}\right)$ |
| $\mathrm{CO}(\mathrm{s} 2)+\mathrm{H} 2 \mathrm{C} 3 \mathrm{p}(\mathrm{q} 4)$ | \# | 0.05 | C1(2-A) |
| $\mathrm{CO}(\mathrm{s} 2)+\mathrm{H} 2 \mathrm{C} 3 \mathrm{p}(\mathrm{q} 4)$ | \# | 0.05 | CS(2-A") |
| $\mathrm{CO}(\mathrm{s} 2)+\mathrm{H} 2 \mathrm{C} 3 \mathrm{p}(\mathrm{q} 4)$ | \# | 0.05 | C1(2-A) |
| $\mathrm{CO}(\mathrm{s} 2)+\mathrm{H} 2 \mathrm{C} 3 \mathrm{p}(\mathrm{q} 4)$ | \# | 0.05 | C1(2-A) |
| $\mathrm{CO}(\mathrm{s} 2)+\mathrm{H} 2 \mathrm{C} 3 \mathrm{p}(\mathrm{q} 4)$ | \# | 0.05 | C1(2-A) |
| $\mathrm{CO}(\mathrm{s} 2)+\mathrm{H} 2 \mathrm{C} 3 \mathrm{p}(\mathrm{d} 2)$ | \# | 0.85 | C1(4-A) |
| $\mathrm{H}(\mathrm{d} 2)+\mathrm{H} 3 \mathrm{C} 4 \mathrm{p}$ ( s 2$)$ | \# | 0.56 | C1(2-A) |
| $\mathrm{H}(\mathrm{d} 2)+\mathrm{H} 3 \mathrm{C} 4 \mathrm{p}$ ( s 2 ) | \# | 2.46 | $\mathrm{CS}\left(2-\mathrm{A}^{\prime \prime}\right)$ |
| $\mathrm{H}(\mathrm{d} 2)+\mathrm{H} 3 \mathrm{C} 4 \mathrm{p}(\mathrm{s} 2)$ | \# | 2.33 | C1(2-A) |
| $\mathrm{H}(\mathrm{d} 2)+\mathrm{H} 3 \mathrm{C} 4 \mathrm{p}$ ( s 2$)$ | \# | 3.46 | $\mathrm{C} 2 \mathrm{~V}(2-\mathrm{B} 1)$ |
| $\mathrm{H}(\mathrm{d} 2)+\mathrm{H} 3 \mathrm{C} 4 \mathrm{p}$ ( s 2$)$ | \# | 0.13 | C1(2-A) |
| $\mathrm{H}(\mathrm{d} 2)+\mathrm{H} 3 \mathrm{C} 4 \mathrm{p}(\mathrm{s} 2)$ | \# | 3.20 | $\mathrm{CS}\left(2-\mathrm{A}{ }^{\prime \prime}\right)$ |
| $\mathrm{H}(\mathrm{d} 2)+\mathrm{H} 3 \mathrm{C} 4 \mathrm{p}$ ( s 2$)$ | \# | 1.10 | C1(2-A) |
| $\mathrm{H}(\mathrm{d} 2)+\mathrm{H} 3 \mathrm{C} 4 \mathrm{p}(\mathrm{s} 2)$ | \# | 1.69 | $\mathrm{CS}\left(2-\mathrm{A}^{\prime}\right)$ |
| H2 ( s2 ) + $\mathrm{H} 2 \mathrm{C} 4 \mathrm{p}(\mathrm{d} 3$ ) | \# | 0.04 | $\mathrm{C} 1(2-\mathrm{A})$ |
| $\mathrm{H} 2(\mathrm{~s} 2)+\mathrm{H} 2 \mathrm{C} 4 \mathrm{p}(\mathrm{d} 3)$ | \# | 0.04 | C1(2-A) |
| $\mathrm{H}(\mathrm{d} 2)+\mathrm{H} 3 \mathrm{C} 4 \mathrm{p}$ ( s 2$)$ | \# | 0.05 | $\mathrm{C} 1(2-\mathrm{A})$ |
| $\mathrm{H}(\mathrm{d} 2)+\mathrm{H} 3 \mathrm{C} 4 \mathrm{p}$ ( s 2$)$ | \# | 0.99 | $\mathrm{CS}\left(2-\mathrm{A}{ }^{\prime \prime}\right)$ |
| $\mathrm{H}(\mathrm{d} 2)+\mathrm{H} 3 \mathrm{C} 4 \mathrm{p}$ ( s 2$)$ | \# | 3.07 | D2H(2-B2G) |


| 462 | H4C4p(d14) | 1 | 2 | 1 | 1 |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 463 | H4C4p(d15) | 1 | 2 | 1 | 1 |
| 464 | H4C4p(d17) | 1 | 2 | 1 | 2 |
| 465 | H4C4p(d18) | 1 | 2 | 1 | 4 |
| 466 | H4C4p(d19) | 1 | 2 | 1 | 4 |
| 467 | H4C4p(q1) |  | 4 | 1 | 1 |
| 468 | H4C4p(q2) | 1 | 4 | 1 | 1 |
| 469 | H4C4p(q3) | 1 | 4 | 1 | 1 |
| 470 | H4C4p(q4) | 1 | 4 | 1 | 1 |
| 471 | H4C4p(q5) | 1 | 4 | 1 | 1 |
| 472 | H4C4p(q6) | 1 | 4 | 1 | 1 |
| 473 | H4C4p(q7) | 1 | 4 | 1 | 2 |
| 474 | H4C4p(q8) | 1 | 4 | 1 | 1 |
| 475 | H4C4p(q9) | 1 | 4 | 1 | 1 |
| 476 | H4C4p(q10) | 1 | 4 | 1 | 1 |
| 477 | H4C4p(q11) | 1 | 4 | 1 | 1 |
| 478 | H4C4p(q12) | 1 | 4 | 1 | 1 |
| 479 | H4C4p(q13) | 1 | 4 | 1 | 2 |
| 480 | H4C4p(q14) | 1 | 4 | 1 | 1 |
| 481 | H4C4p(q15) | 1 | 4 | 1 | 2 |
| 482 | H4C4p(q16) | 1 | 4 | 1 | 2 |
| 483 | H4C4p(q17) | 1 | 4 | 1 | 2 |
| 484 | H4C4p(q18) | 1 | 4 | 1 | 1 |
| 485 | H4C4p(q19) | 1 | 4 | 1 | 4 |
| 486 | H4C3Op(d2) | 1 | 2 | 1 | 1 |
| 487 | H4C3Op(d4) | 1 | 2 | 1 | 1 |
| 488 | H4C3Op(q1) | 1 | 4 | 1 | 1 |
| 489 | H4C3Op(q2) | 1 | 4 | 1 | 1 |
| 490 | H4C3Op(q3) | 1 | 4 | 1 | 1 |
| 491 | H3C4Op(s1) | 1 | 1 | 1 | 1 |
| 492 | H3C4Op(s2) | 1 | 1 | 1 | 1 |
| 493 | H3C4Op(s3) | 1 | 1 | 1 | 1 |
| 494 | H3C4Op(s4) | 1 | 1 | 1 | 1 |
| 495 | H3C4Op(s5) | 1 | 1 | 1 | 1 |
| 496 | C4H4Op(d1) | 1 | 2 | 1 | 1 |
| 497 | C4H4Op(d2) | 1 | 2 | 1 | 1 |
| 498 | C4H4Op(d3) | 1 | 2 | 1 | 2 |
| 499 | C4H4Op(d4) | 1 | 2 | 1 | 1 |
| 500 | C4H4Op(d5) | 1 | 2 | 1 | 1 |
| 501 | C4H4Op(d6) | 1 | 2 | 1 | 1 |
| 502 | C4H4Op (d7) | 1 | 2 | 1 | 1 |
| 503 | C4H4Op(d8) | 1 | 2 | 1 | 1 |
| 504 | C4H4Op (d9) | 1 | 2 | 1 | 1 |
| 505 | C4H4Op(d10) | 1 | 2 |  |  |
| 506 | C4H4Op(d11) | 1 | 2 |  |  |
| 507 | C4H4Op(d12) | 1 | 2 |  |  |
| 508 | C4H4Op(d13) | 1 | 2 |  |  |
| 509 | C4H4Op(d14) | 1 | 2 |  |  |
| 510 | C4H4Op(d15) | 1 | 2 |  |  |
| 511 | C4H4Op(d16) | 1 | 2 |  |  |
| 512 | C4H4Op(d19) | 1 | 2 |  |  |
| 513 | C4H4Op(d20) | 1 | 2 |  |  |
| 514 | \# |  |  |  |  |

H4C4.q1.m2-14.rxyz
H4C4.q1.m2-15.rxyz H4C4.q1.m2-17.rxyz H4C4.q1.m2-18.rxyz H4C4.q1.m2-19.rxyz H4C4.q1.m4-1.rxyz H4C4.q1.m4-2.rxyz H4C4.q1.m4-3.rxyz H4C4. q1.m4-4.rxyz H4C4. q1.m4-5.rxyz H4C4.q1.m4-6.rxyz H4C4.q1.m4-7.rxyz H4C4. q1.m4-8.rxyz H4C4.q1.m4-9.rxyz H4C4. q1.m4-10.rxyz H4C4. q1.m4-11.rxyz H4C4.q1.m4-12.rxyz H4C4.q1.m4-13.rxyz H4C4. q1.m4-14.rxyz H4C4. q1.m4-15.rxyz H4C4.q1.m4-16.rxyz H4C4. q1.m4-17.rxyz H4C4.q1.m4-18.rxyz
H4C4.q1.m4-19.rxyz H4C3O.q1.m2-2.rxyz H4C3O. q1.m2-4.rxyz H4C3O. q1.m4-1.rxyz H4C3O. q1.m4-2.rxyz H4C3O. q1.m4-3.rxyz H3C4O. q1.m1-1.rxyz H3C4O. q1.m1-2.rxyz H3C4O. q1.m1-3.rxyz H3C4O. q1.m1-4.rxyz H3C4O. q1.m1-5.rxyz C4H4O.q1.m2-1.rxyz C4H4O.q1.m2-2.rxyz C4H4O. q1.m2-3.rxyz C4H4O. q1.m2-4.rxyz C4H4O.q1.m2-5.rxyz C4H4O. q1.m2-6.rxyz C4H4O. q1.m2-7.rxyz C4H4O.q1.m2-8.rxyz C4H4O.q1.m2-9.rxyz C4H4O. q1.m2-10.rxyz C4H4O. q1.m2-11.rxyz C4H4O.q1.m2-12.rxyz C4H4O.q1.m2-13.rxyz C4H4O. q1.m2-14.rxyz C4H4O. q1.m2-15.rxyz C4H4O.q1.m2-16.rxyz C4H4O.q1.m2-19.rxyz C4H4O. q1.m2-20.rxyz

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| -6251.097207 |
| -6251.078759 |
| -6250.169761 |
| -6250.605822 |


| $\mathrm{H}(\mathrm{d} 2)+\mathrm{H} 3 \mathrm{C} 4 \mathrm{p}(\mathrm{s} 2)$ | \# | 2.21 | $\mathrm{C} 1(2-\mathrm{A})$ |
| :---: | :---: | :---: | :---: |
| $\mathrm{H}(\mathrm{d} 2)+\mathrm{H} 3 \mathrm{C} 4 \mathrm{p}$ ( s 2$)$ | \# | 1.69 | $\mathrm{CS}\left(2-\mathrm{A}^{\prime}\right)$ |
| $\mathrm{H}(\mathrm{d} 2)+\mathrm{H} 3 \mathrm{C} 4 \mathrm{p}(\mathrm{s} 2)$ | \# | 0.34 | $\mathrm{C} 2 \mathrm{H}(2-\mathrm{BU})$ |
| $\mathrm{H}(\mathrm{d} 2)+\mathrm{H} 3 \mathrm{C} 4 \mathrm{p}(\mathrm{s} 2)$ | \# | 1.72 | $\mathrm{D} 2 \mathrm{D}(2-\mathrm{A} 1)$ |
| $\mathrm{H}(\mathrm{d} 2)+\mathrm{H} 3 \mathrm{C} 4 \mathrm{p}$ ( s 2$)$ | \# | 3.38 | D2(2-B2) |
| $\mathrm{H}(\mathrm{d} 2)+\mathrm{H} 3 \mathrm{C} 4 \mathrm{p}(\mathrm{t} 2)$ | \# | 0.10 | C1(4-A) |
| H2 ( 22 ) + $\mathrm{H} 2 \mathrm{C} 4 \mathrm{p}(\mathrm{d} 9$ ) | \# | 0.42 | C1(4-A) |
| $\mathrm{H}(\mathrm{d} 2)+\mathrm{H} 3 \mathrm{C} 4 \mathrm{p}(\mathrm{t} 12)$ | \# | 0.16 | C1(4-A) |
| $\mathrm{H}(\mathrm{d} 2)+\mathrm{H} 3 \mathrm{C} 4 \mathrm{p}(\mathrm{s} 2)$ | \# | 0.33 | C1(4-A) |
| HC2(d1)+H3C2p(s2) | \# | 0.01 | CS(4-A") |
| H2 ( s 2$)+\mathrm{H} 2 \mathrm{C} 4 \mathrm{p}(\mathrm{d} 9)$ | \# | 0.56 | C1(4-A) |
| $\mathrm{H}(\mathrm{d} 2)+\mathrm{H} 3 \mathrm{C} 4 \mathrm{p}(\mathrm{s} 2)$ | \# | 0.32 | $\mathrm{C} 2 \mathrm{H}(4-\mathrm{AU})$ |
| $\mathrm{H} 2(\mathrm{~s} 2)+\mathrm{H} 2 \mathrm{C} 4 \mathrm{p}(\mathrm{d} 7)$ | \# | 0.00 | C1(4-A) |
| $\mathrm{H}(\mathrm{d} 2)+\mathrm{H} 3 \mathrm{C} 4 \mathrm{p}(\mathrm{t} 12)$ | \# | 0.14 | CS(4-A") |
| HC(q24) + $\mathrm{H} 3 \mathrm{C} 3 \mathrm{p}(\mathrm{s} 1)$ | \# | 0.04 | C1(4-A) |
| $\mathrm{H}(\mathrm{d} 2)+\mathrm{H} 3 \mathrm{C} 4 \mathrm{p}(\mathrm{t} 12)$ | \# | 0.15 | C1(4-A) |
| H2( 22 ) $+\mathrm{H} 2 \mathrm{C} 4 \mathrm{p}(\mathrm{d} 9)$ | \# | 0.22 | CS(4-A") |
| H2(s2) + H 2 C 4 p (d9) | \# | 0.40 | $\mathrm{C} 2 \mathrm{H}(4-\mathrm{AU})$ |
| H2 (s2) + H 2 C 4 p (d9) | \# | 0.09 | C1(4-A) |
| $\mathrm{H} 2(\mathrm{~s} 2)+\mathrm{H} 2 \mathrm{C} 4 \mathrm{p}(\mathrm{d} 9)$ | \# | 0.28 | $\mathrm{C} 2 \mathrm{~V}(4-\mathrm{B} 2)$ |
| H2(s2) + $\mathrm{H} 2 \mathrm{C} 4 \mathrm{p}(\mathrm{d} 3)$ | \# | 0.13 | $\mathrm{C} 2 \mathrm{~V}(4-\mathrm{A} 2)$ |
| $\mathrm{H}(\mathrm{d} 2)+\mathrm{H} 3 \mathrm{C} 4 \mathrm{p}(\mathrm{s} 15)$ | \# | 0.07 | $\mathrm{C} 2 \mathrm{~V}(4-\mathrm{B} 1)$ |
| H2(s2) + H 2 C 4 p (d9) | \# | 0.22 | C1(4-A) |
| $\mathrm{H}(\mathrm{d} 2)+\mathrm{H} 3 \mathrm{C} 4 \mathrm{p}(\mathrm{s} 2)$ | \# | 0.36 | D2 (4-B3) |
| $\mathrm{H} 2 \mathrm{C} 2 \mathrm{p}(\mathrm{d} 1)+\mathrm{H} 2 \mathrm{CO}(\mathrm{s} 1)$ | \# | 0.31 | $\mathrm{C} 1(2-\mathrm{A})$ |
| $\mathrm{CO}(\mathrm{s} 2)+\mathrm{H} 4 \mathrm{C} 2 \mathrm{p}(\mathrm{d} 6)$ | \# | 0.78 | $\mathrm{CS}\left(2-\mathrm{A}^{\prime \prime}\right)$ |
| H3C2(d2)+HCOp(s2) | \# | 0.30 | C1(4-A) |
| H2C2p(d2)+ $\mathrm{H} 2 \mathrm{CO}(\mathrm{s} 1)$ | \# | 0.13 | C1(4-A) |
| $\mathrm{H} 2 \mathrm{C} 2 \mathrm{p}(\mathrm{d} 1)+\mathrm{H} 2 \mathrm{CO}(\mathrm{s} 1)$ | \# | 0.23 | C1(4-A) |
| $\mathrm{CO}(\mathrm{s} 2)+\mathrm{H} 3 \mathrm{C} 3 \mathrm{p}(\mathrm{s} 3)$ | \# | 1.05 | C1(1-A) |
| $\mathrm{CO}(\mathrm{s} 2)+\mathrm{H} 3 \mathrm{C} 3 \mathrm{p}(\mathrm{s} 3)$ | \# | 0.95 | C1(1-A) |
| H 2 ( s2) $+\mathrm{HC4Op}(\mathrm{~s} 1)$ | \# | 0.53 | C1(1-A) |
| $\mathrm{CO}(\mathrm{s} 2)+\mathrm{H} 3 \mathrm{C} 3 \mathrm{p}(\mathrm{s} 9)$ | \# | 0.83 | C1(1-A) |
| $\mathrm{CO}(\mathrm{s} 2)+\mathrm{H} 3 \mathrm{C} 3 \mathrm{p}(\mathrm{s} 1)$ | \# | 0.17 | C1(1-A) |
| $\mathrm{HCO}(\mathrm{d} 7)+\mathrm{H} 3 \mathrm{C} 3 \mathrm{p}(\mathrm{s} 1)$ | \# | 1.24 | $\mathrm{CS}\left(2-\mathrm{A}^{\prime}\right)$ |
| H2C2(s2)+H2C2Op(d3) | \# | 1.85 | C1(2-A) |
| H2C2 (s2) + $\mathrm{H} 2 \mathrm{C} 2 \mathrm{Op}(\mathrm{d} 3)$ | \# | 3.05 | $\mathrm{C} 2 \mathrm{~V}(2-\mathrm{A} 2)$ |
| H2C2(s2)+H2C2Op(d3) | \# | 0.75 | $\mathrm{CS}\left(2-\mathrm{A}^{\prime}\right)$ |
| $\mathrm{HCO}(\mathrm{d} 7)+\mathrm{H} 3 \mathrm{C} 3 \mathrm{p}(\mathrm{s} 1)$ | \# | 1.46 | CS(2-A") |
| H2C2(s2)+H2C2Op(d3) | \# | 0.85 | C1(2-A) |
| H2C2 (s2) + $\mathrm{H} 2 \mathrm{C} 2 \mathrm{Op}(\mathrm{d} 3)$ | \# | 2.18 | $\mathrm{CS}\left(2-\mathrm{A}^{\prime}\right)$ |
| $\mathrm{HCO}(\mathrm{d} 7$ ) $+\mathrm{H} 3 \mathrm{C} 3 \mathrm{p}(\mathrm{s} 1)$ | \# | 0.40 | $\mathrm{CS}\left(2-\mathrm{A}^{\prime \prime}\right)$ |
| H2C2 (s2) + $\mathrm{H} 2 \mathrm{C} 2 \mathrm{Op}(\mathrm{d} 3)$ | \# | 3.02 | CS(2-A") |
| $\mathrm{HCO}(\mathrm{d} 7)+\mathrm{H} 3 \mathrm{C} 3 \mathrm{p}(\mathrm{s} 1)$ | \# | 1.57 | $\mathrm{CS}\left(2-\mathrm{A}^{\prime}\right)$ |
| H2C2 (s2) + $\mathrm{H} 2 \mathrm{C} 2 \mathrm{Op}(\mathrm{d} 3)$ | \# | 1.21 | C1(2-A) |
| H2C2 (s2) + $\mathrm{H} 2 \mathrm{C} 2 \mathrm{Op}(\mathrm{d} 3)$ | \# | 1.29 | C1(2-A) |
| H2C2 (s2) + $\mathrm{H} 2 \mathrm{C} 2 \mathrm{Op}(\mathrm{d} 3)$ | \# | 1.28 | C1(2-A) |
| H2C2 (s2) + $\mathrm{H} 2 \mathrm{C} 2 \mathrm{Op}(\mathrm{d} 3)$ | \# | 0.53 | $\mathrm{CS}\left(2-\mathrm{A}^{\prime}\right)$ |
| H2C2(s2)+ ${ }^{\text {2 }} 2 \mathrm{C} 2 \mathrm{Op}(\mathrm{d} 3)$ | \# | 1.92 | C1(2-A) |
| $\mathrm{HCO}(\mathrm{d} 7)+\mathrm{H} 3 \mathrm{C} 3 \mathrm{p}(\mathrm{s} 1)$ | \# | 1.92 | C1(2-A) |
| H2C2 (s2) + $\mathrm{H} 2 \mathrm{C} 2 \mathrm{Op}(\mathrm{d} 3$ ) | \# | 0.99 | $\mathrm{CS}\left(2-\mathrm{A}^{\prime}\right)$ |
| $\mathrm{H} 2 \mathrm{C} 2(\mathrm{~s} 2)+\mathrm{H} 2 \mathrm{C} 2 \mathrm{Op}(\mathrm{d} 3)$ | \# | 1.43 | C1(2-A) |

END FRAGMENTS_DATABASE
BEGIN EXPERIMENTAL_BRANCHING_RATIOS
error = absolute
diagram $=$ S.vs.E

| \# C Channel | BR | error $\quad \mathrm{q} / \mathrm{n}$ |  |
| :--- | :---: | :---: | :---: |
| \# <br> Hp | 0.0 | 0.0 | 1.0 |
| H2p | 0.0 | 0.0 | 2.0 |
| H3p | 0.0 | 0.0 | 3.0 |
| Cp | 0.0 | 0.0 | 12.0 |
| HCp | 0.0 | 0.0 | 13.0 |
| H2Cp | 0.0 | 0.0 | 14.0 |
| H3Cp | 0.0 | 0.0 | 15.0 |
| H4Cp | 0.0 | 0.0 | 16.0 |
| HOp | 0.0 | 0.0 | 17.0 |
| H2Op | 0.0 | 0.0 | 18.0 |
| H3Op | 0.0 | 0.0 | 19.0 |
| H4Op | 0.0 | 0.0 | 20.0 |
| C2p | 3.70 | 0.0 | 24.0 |
| HC2p | 1.88 | 0.0 | 25.0 |
| H2C2p | 1.56 | 0.0 | 26.0 |
| H3C2p | 0.27 | 0.0 | 27.0 |
| COp | 2.71 | 0.0 | 28.0 |
| HCOp | 9.49 | 0.0 | 29.0 |
| H2COp | 0.0 | 0.0 | 30.0 |
| H3COp | 0.0 | 0.0 | 31.0 |



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