

1 Effect of bending-torsion on fracture and fatigue life for 18Ni300 2 steel specimens produced by SLM

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19 **Abstract:** In this study, different fracture surfaces caused by fatigue failure were generated from 18Ni300 steel produced by selective laser melting
20 (SLM). Hollow round bars with a transverse hole were tested under bending-torsion to investigate the crack initiation mechanisms and fatigue life.
21 Next, the post-failure fracture surfaces were examined by optical profilometer and scanning electron microscope. The focus is placed on the
22 relationship between the fatigue features (e.g., bending-torsion ratio, fatigue crack initiation angles, and fatigue life) and the fracture surface
23 topography parameters (e.g., height parameter S_x , volume parameters V_x , maximal pit and valley angles). The analysis was carried out using the
24 entire fracture surface of the tested specimens. It was found that the decrease of the shear stress level significantly reduces the value of the fracture
25 surface parameters. A fatigue life prediction model based on both the surface topography values and the applied load was proposed. Fatigue life
26 predictions for different loading ratios agreed well with the experimental results and were slightly better than those of other existing models. The
27 proposed model can be helpful for post-mortem analysis of engineering components subjected to multiaxial fatigue.

28 **Keywords:** multiaxial fatigue, bending-torsion, notch effect, fatigue fracture, surface topography, SLM, fatigue crack initiation, fatigue life esti-
29 mation, strain energy density.

30 Highlights

- 31 • Effect of bending-torsion loading on fracture surface topography is evaluated.
- 32 • The bending-torsion ratio significantly affects the fracture surface topography.
- 33 • Fatigue life predicted from fracture surface parameters and local von Mises stresses.

34

35 1. Introduction

36 In the literature focused on fatigue design, much experimental studies about the failure mechanisms exist (Azevedo and
37 Marques, 2010; Djukic et al., 2019; Jamali et al., 2016; Walczak and Szala, 2021). In particular, fatigue research attempts to reflect
38 the actual stress state (Meischel et al., 2016; Stanzl-Tschegg, 2017; Strzelecki and Wachowski, 2022) but also attempts to understand

39 the mechanisms associated with pure loadings (Yao et al., 2018). To gain more insight into the failure mechanisms, the investigation
40 of multiaxial fatigue is of high interest (Gosch et al., 2020; Jamali et al., 2019; Pejkowski and Skibicki, 2019; Tomczyk and Seweryn,
41 2017). Fatigue life under mixed-mode loading is very important from a safety point of view (Demir et al., 2019). This is why this
42 problem is often analyzed in scientific works, aiming to develop new research methods and better identify the governing variables.
43 Different types of specimen geometries for mixed-mode loading have been used in literature (Wojciech Macek et al., 2021b;
44 Rozumek et al., 2022, 2018; Vojtek et al., 2013). Furthermore, different models have been introduced to analyse the fracture
45 behaviour under mixed-mode loading (Branco et al., 2018, 2015; Kondo et al., 2019; Pelegatti et al., 2021; Stamoulis and Carrere,
46 2020).

47 Selective laser melting (SLM) is one laser additive manufacturing technique capable of printing metal components (Branco
48 et al., 2021b; Li et al., 2019; Santos et al., 2016; Wang et al., 2019). This technique fabricates three-dimensional objects from laser
49 radiation to powder materials on the powder beds through successive layer bonded to already existing layers under protective at-
50 mosphere (Santos et al., 2016). Despite some interesting advantages, e.g. the geometric freedom and reduced time-to-market, it has
51 some shortcomings, namely internal defects and high surface roughness, which may cause stress concentration effects affecting the
52 fatigue resistance (Branco et al., 2021a; Le et al., 2019). Malekipour et al. (2021) modelled the damage of small-scale porosities on
53 fatigue behaviour in the high-cycle regime of SLM AISI 316 steel specimens (Malekipour et al., 2021). These authors concluded
54 that the inherence of small-scale porosities with a length lower than 5 μm did not accelerate the damage growth, except when these
55 defects were situated in the path of the crack growth. Thus, imperfections, which have a random nature in materials elaborated by
56 additive manufacturing, are challenging to control both in the production process and, later, in the fatigue design stage (Cunha et
57 al., 2022; Elkhateeb et al., 2022; Garcias et al., 2021). The anisotropy of SLM produced materials can affect the fatigue crack growth
58 rates, depending on the relation of the crack growth direction and the grain long axis. The anisotropic behavior of SLM materials
59 was confirmed in several studies (Avanzini, 2022; Fergani et al., 2018), where the fatigue crack propagation was related to the
60 building orientation.

61 Scientists are continually attempting to find more efficient solutions for engineering problems as well as to develop new
62 research techniques. These research techniques can be divided into non-destructive and destructive approaches (Gryguc et al., 2018;
63 Molent et al., 2017). An example of a recent study combining both non-destructive and destructive approaches is the in-depth
64 research of underwater welded S460N steel provided by Tomków et al. (Tomków et al., 2020). They performed non-destructive
65 tests - comprising visual, penetrant, radiographic, and ultrasonic tests - and destructive tests, which included static tensile, bending,
66 hardness, and impact tests. In the context of fatigue analysis, there are also novel fatigue testing methods. An interesting study is,
67 for example, the one carried out by Brodie et al. (2022) on low-cycle-fatigue of small-scale specimens. The introduction of new

68 measurement methods, e.g. Digital Image Correlation (DIC), in the analysis of crack propagation problems is another challenging
69 area. Karen et al. (2022) studied blunt notches by using the DIC measurements (Karen Alavi et al., 2022) and demonstrated its
70 accuracy in the determination of the stress fields for different geometric discontinuities, including V-, O-, and U-notches under
71 mode-I loading.

72 Profilometry began to be applied in the 1940s, pressed for [the need](#) to improve the quality of mechanical components used
73 during [the World War II](#). Therefore, much later than [the study](#) of fatigue and fracture [phenomena](#), but [also](#) intensely (Buljac et al.,
74 2018). The [importance](#) of surface texture [analyses](#) can be seen, among others, by the growing number of parameters contained in
75 the ISO and ASME standards (Krolczyk et al., 2018; Przemysław Podulka, 2021; Todhunter et al., 2017a). Areal surface texture
76 was born in the 1990s by extending profile paramters to 3D. Contemporary, not only in science but especially in industry,
77 profilometers are widely used (Senin et al., 2017; Zhang et al., 2022). Technologically advanced measurement stands, including
78 focus variation microscopy (FVM), are commercially available (W. Macek et al., 2021; Newton et al., 2019). Measurement devices
79 of this type have also found application in the analysis of surface topography of fatigue fractures (Lauschmann et al., 2019; Santus
80 et al., 2022; Wietecha-Reiman et al., 2022).

81 In the scientific literature on fractography, there are many attempts to find a way to quantify fatigue fractures and make them
82 dependent on [damage-generating factors](#) (de Freitas et al., 2017; Deng et al., 2022; Merson et al., 2017; Westermann et al., 2016).
83 One of these ways is the FRASTA method, but it focuses on regions from initiation to final fracture (Kobayashi and Shockey, 2010;
84 Sampath et al., 2018). On the contrary, the method introduced by the authors is based on the entire fracture area and has been
85 successfully tested for different materials and specimens geometries (Wojciech Macek et al., 2021c, 2021a).

86 Models for estimating fatigue life allow engineers to optimise structural and mechanical design ([Deng et al., 2023](#); Masoudi
87 Nejad et al., 2022). However, there are also attempts to use other approaches. Thermodynamics fundamental equation for high-
88 cycle metal fatigue was introduced by [Lee and Basaran](#) (Lee and Basaran, 2022). Another attempt to combine additional parameters
89 involved in the fatigue process was proposed by [Fan and Zhao](#) (Fan and Zhao, 2022) by using quantitative thermography for fatigue
90 life prediction of welded components. In this case, the energy dissipation was taken as an efficient index of fatigue damage [and was](#)
91 [used](#) to develop a nonlinear damage accumulation model.

The possibility of describing the fatigue fracture process and the fatigue durability of three-dimensional metallic parts produced by SLM based on metrological fractographic analysis and fatigue damage parameters was the main motivation to undertake the present study. To the best of the authors' knowledge, studies dealing with this combined approach of fractographic and fatigue damage quantifiers under multiaxial loading for SLMed materials do not exist in the open literature. Thus, first it is examined the influence of mixed-mode loading on fracture and fatigue behavior of 18Ni300 steel specimens produced by SLM

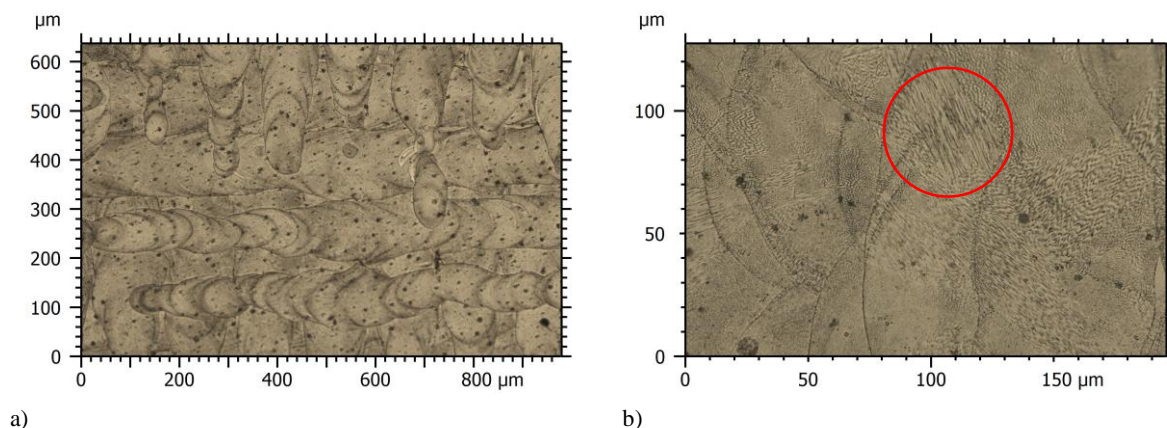
97 using fracture surface parameters. Then, a simple fatigue life prediction model based on post-mortem fracture surface topography
98 results and local stress obtained using the finite element method is proposed. Finally, the predicted lives are compared with the
99 experimental values and those obtained from a well-known energy-based approach.

100

101 2. Materials and Methods

102 2.1. Material and fatigue test procedure

103 The material used in this study was 18Ni300 steel produced by SLM. The nominal chemical composition and the mechanical
104 properties of the tested batch are summarised in Table 1 and Table 2, respectively (Branco et al., 2021b; Macek et al., 2020). The
105 manufacturing process comprehend the deposition of 40 μm thick layers, with a hatch spacing of 100 μm , for a scan speed of 200
106 mm/s. Based on the procedure described in the ASTM E3, and as displayed in Figure 1, the optical examination revealed a lath
107 microstructure, rather coherent, and mainly formed by elongated grains, with about 150 μm long and 30-35 μm width (see Fig 1(a)).
108 It was also observed martensitic needles across the surface (see the circle in Figure 1(b)) as well as small porosities (see the dark
109 dots in Fig. 1).



110
111
112 **Figure 1.** Microstructure of the SLM 18Ni300 examined by optical microscopy from a specimen polished and etched with picral: (a) 100 \times ; and
113 (b) 500 \times magnification.

114
115 The specimens had a circular hollow geometry with an open hole in one side and were fabricated in a vertical orientation on
the base plate using a Concept Laser M3 linear printing system equipped with a Nd:YAG fibre laser. After the additive
manufacturing process, the specimens were machined and the hole region was carefully polished to a scratch-free condition by
means of progressively finer grades of silicon carbide papers (P600-grit, P1200-grit, and P2500-grit) followed by a 6- μm diamond
water-based polishing paste. Figure 2 shows the shape and dimension of the tested specimens.

Table 1. Nominal chemical composition of the SLM AISI 18Ni300 (wt.%) (Branco et al., 2021b; Macek et al., 2020).

C	Ni	Mn	Co	Mo	Ti	Al	Cr	P	Si	Mn	Fe
0.01	18.2	0.65	9.0	5.0	0.6	0.05	0.3	0.01	0.1	0.04	Balance

Table 2. Mechanical properties of the SLM AISI 18Ni300 for the tested batch (Branco et al., 2021b; Macek et al., 2020).

Property	Value
Porosity, ϕ (%)	0.74
Density, ρ (g/cm ³)	7.42
Poisson's ratio, ν (-)	0.33
Young's modulus, E (GPa)	168
Tensile strength, σ_{UTS} (MPa)	1147
Yield strength, σ_{YS} (MPa)	910
Strain at failure, ϵ_f (%)	5.12
Cyclic hardening coefficient, k' (MPa)	1921.21

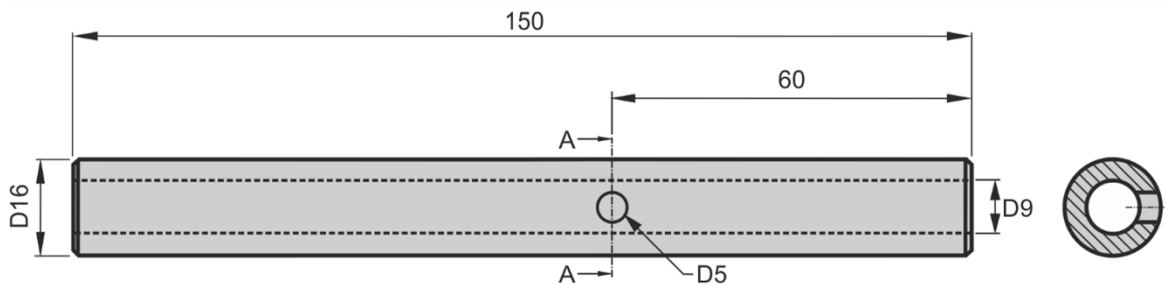


Figure 2. Specimen geometry used in the multiaxial fatigue tests (units: millimetres).

The tests were performed in air, at room temperature, using sinusoidal waves, and cyclic frequencies in the range 3–6 Hz. The bending moment to torsion moment ratios, B/T , also presented in Table 3, were equal to 1, 2 and 2/3. For all tested specimens, the stress ratio, R , was equal to 0. The nominal normal stress amplitude σ_a and shear stress amplitude τ_a applied in the test are also listed in Table 3. Crack detection and crack growth were monitored in situ via a high-resolution digital camera. In this study, the fatigue life associated to crack initiation, N_i , was calculated from the experimental $a-N$ curves (i.e. crack length versus number of cycles) for a fixed crack length of 0.5 mm. Regarding the total life, N_f , it was estimated also from the experimental $a-N$ curves for a crack length of 3 mm.

Table 3. Summary of the multiaxial fatigue testing program.

Specimen	B/T ratio	σ_a/τ_a	σ_a (MPa)	σ_m (MPa)
BT3_2	2/3	4/3	55.27	60.79
BT3_1	2/3	4/3	79.59	87.55
BT1_1	1	2	66.32	72.96
BT1_2	1	2	79.59	87.55
BT1_3	1	2	95.50	105.05

136	BT2_1	2	4	78.26	86.09
137	BT2_2	2	4	79.59	87.55
	BT2_3	2	4	95.50	105.06

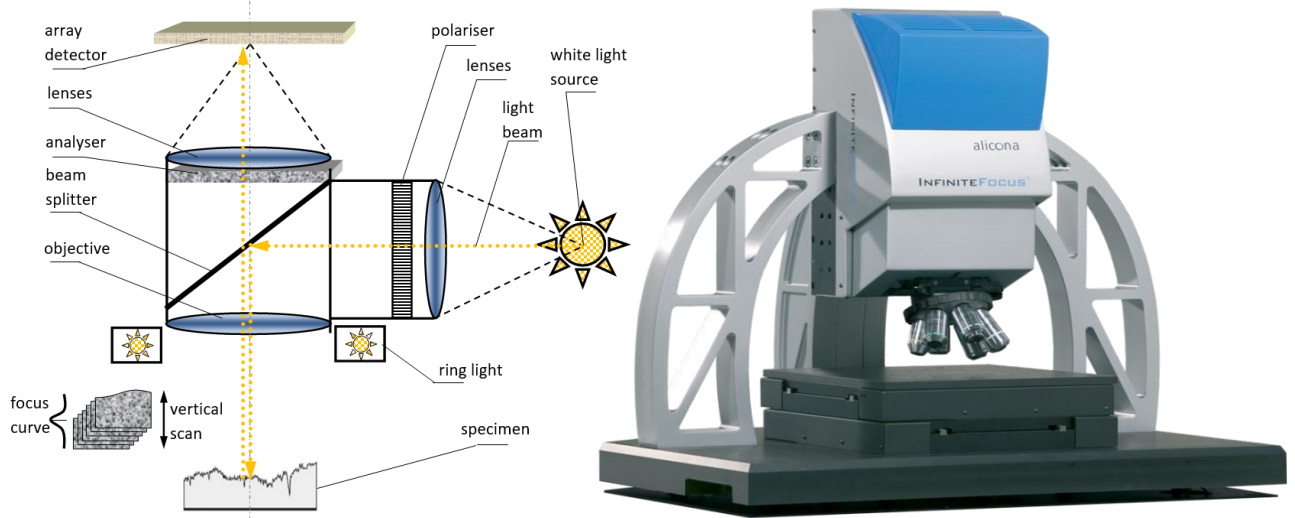
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σ_a : nominal normal stress amplitude; σ_m : nominal normal mean stress; τ_a : nominal shear stress amplitude; τ_m : nominal shear mean stress

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142 **2.2. Fracture surface measurement**

143 A Focus Variation (FV) method, applied in an Alicona profilometer (Alicona Imaging GmbH, Graz, Austria) shown in Figure
144 3, was used to determine the fracture surface parameters (Macek, 2021a; Macek, 2021c). This non-contact measuring system uses
145 a white light source to project light beams onto a specimen's surface. The reflected light rays appear from the measured surface and
146 are processed by means of a precise sensor.



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Figure 3. Alicona IF G4 profilometer used in the fracture surface measurements: (a) operation scheme; (b) picture without accessories.

151 The FV method combines the small depth of focus of an optical system with a vertical scanning to provide topographical
152 information from the focus variation. The measurement device was equipped with a motorized nosepiece using five dedicated mi-
153 croscopic objective lenses with magnifications varying from 2.5× to 100×. For the analysis of the 18Ni300 steel specimens produced
154 by SLM, 10× objective lenses for the entire fracture surface areas, and 100× for local fracture zones, were used. Large areas of the
155 entire fractures were scanned using the “Image field” function across the surface, as shown in Table 4, for a 10× magnification
156 considering 18 rows × 13 columns. Appropriately, also using the “Image field” function local fracture zones were scanned with a
157 100× magnification considering 13 rows × 12 columns. Stitching allowed the measurement of an area of about 14.7 mm × 15.4 mm
for entire fractures. Regarding the vertical measurement range, depending on the skewness of the crack, the maximum z for the
specimen with the most oblique fracture (BT3-2) was equal to 10.6 mm, and minimum z range for the specimen with $B/T = 2$ (BT2-
2) was equal to 5.6 mm. The measurement parameters used during the study are listed in Table 4.

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165 **Table 4.** Alicona G4 measurement device main parameters.

Parameter	Value	
Magnification	10×	100×
Vertical resolution	57.3 nm	4.7 nm
Lateral resolution	3.91 μm	1.46 μm
Number of images	19 rows × 13 columns	13 rows × 12 columns
Exposure time	138.5 μs	300.0 μs
Contrast	0.46	0.50

175 Surface studies were carried out on the fracture area using both height parameters, S_x , and volume parameters, V_x , according
 176 to ISO 25178 standard. The height parameters S_x taken into account were: S_q , S_p , S_v , S_z , and S_a . Concerning the functional param-
 177 eters V_x , the ones considered were: V_m , V_v , V_{mp} , V_{mc} , and V_{vv} (Bartoszuk, 2021; P Podulka, 2021; Todhunter et al., 2017b).
 178 MountainsMap surface topography software was used to analyse and visualize the fractures (Macek, 2021b). The surface charac-
 179 terization also included a Texture Isotropy study which aimed to calculate the isotropy parameters with respect to a user-defined
 180 threshold, assumed here equal to 0.20. This values allowed to quantify the central zones corresponding to the portion of the peaks
 181 that remained after thresholding. The threshold equal to 0.2 is a default value but that for some metrological cases it can be right to
 182 choose an another value, in particular to provide that the central lobes are well defined and does not be in contact with the edges of
 183 the zones.

184 The procedure to extract the areas, called here region of interest (ROI), is summarised in Fig. 4. It can be divided into three
 185 main tasks: (1) extract the circular inside area with a radius of 4.7 mm; (2) extract the circular outside area with a radius of 7.7 mm;
 186 (3) extract the rectangular outside area of the lateral hole with dimensions of 5 mm × 5 mm. The whole surface was reduced to
 187 eliminate the regions associated with the geometric discontinuities and to obtain a uniform dimension for all samples. The lowest
 188 (Min) and highest (Max) points of the Z axis were identified for each fracture surface as well as their angles with respect to the XY
 189 plane.

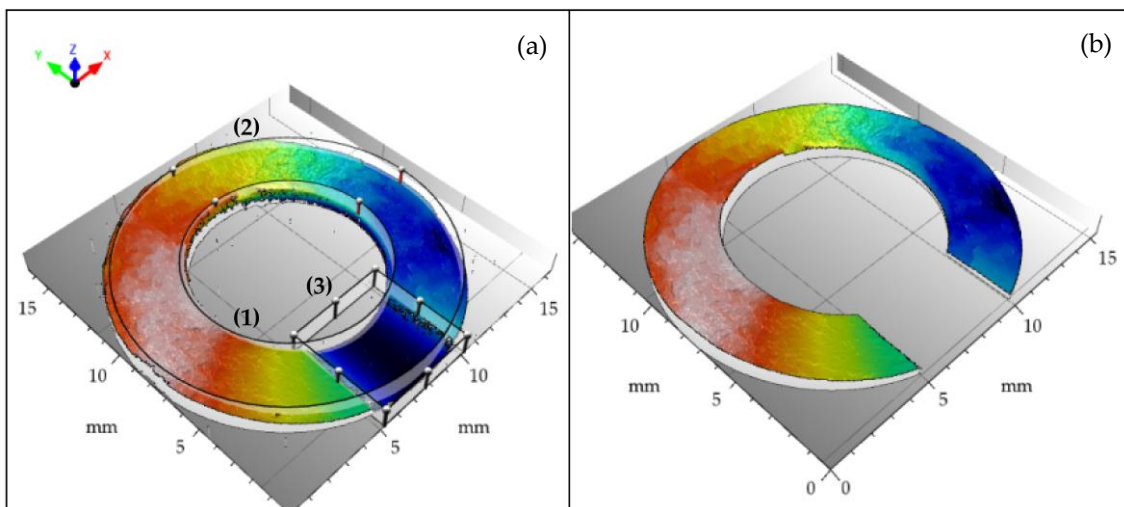


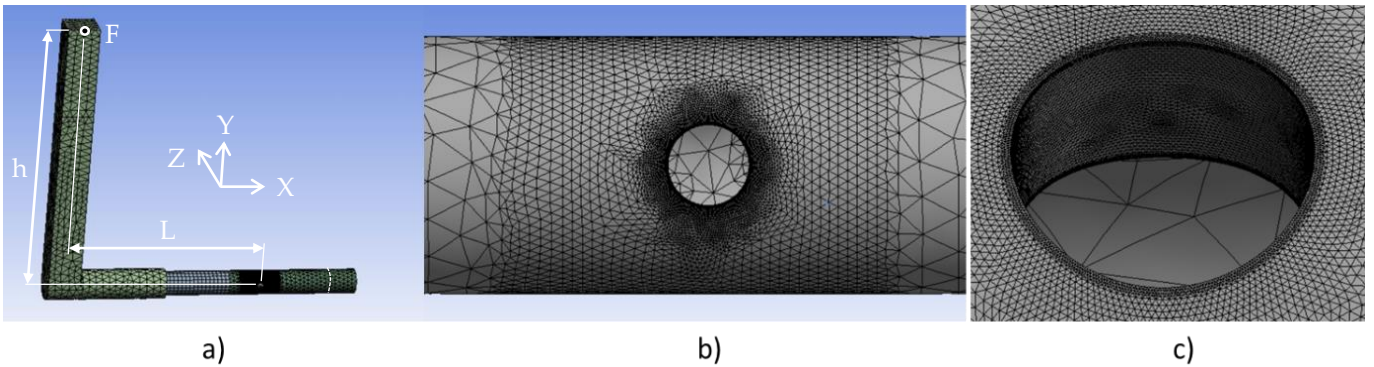
Figure 4. Scheme for determining the extracted area (BT1_2): (a) original surface; (b) region of interest.

195 2.3. Finite element model

196 The finite element model used in this study to obtain the stress field around the hole for the different B/T ratios is shown in
 197 Figure 5. It was created using with 4-node tetrahedral elements in an unstructured framework and contained 642,821 elements and
 198 906,676 nodes. Around the hole, the mesh was much denser, also in the through-the-thickness direction, to better describe the stress-
 199 strain gradients acting in this region (see Fig. 5(b) and Fig. 5(c)). The simulations were conducted assuming a homogeneous, linear-
 200 elastic, and isotropic material. The loading scenarios were defined by applying a single force, F , in the z -axis direction in the end
 201 of the rectangular cross-section arm, while the other end of the model was fixed for an extension of 30 mm from the dashed line to
 202 the right-hand side of the specimen (see Fig. 1(a)). The values of the B/T ratios were adjusted by changing the L/h ratio (h was fixed
 203 while L was determined in a case-by-case basis in order to achieve the tested values) and the magnitude of the applied load. The
 204 relationship between the nominal normal stress amplitude σ_a and the nominal shear stress amplitude τ_a can be obtained from the
 205 following formula:

$$\frac{\sigma_a}{\tau_a} = \frac{32 F_a L}{(d_e^3 - d_i^3)} \Leftrightarrow \frac{\sigma_a}{\tau_a} = \frac{2L}{h} \quad (1)$$

206 where d_e is the outer diameter, d_i is the inner diameter, and F_a is the force amplitude.
 207



209 **Figure 5.** Finite element model of tested specimen made of SLM AISI 18Ni300 steel: (a) assembled model; (b) detail of the hole region; (c) detail
 210 of the mesh topology in the vicinity of the hole.
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213 **3. Results**

214 3.1. Crack and multiaxial fatigue test

215 The different combinations of shear and normal stresses applied in the bending-torsion fatigue tests have a strong influence
 216 on crack growth direction. Depending on the mixed mode relation, as can be seen in Figure 6, various crack paths can be observed.
 In these geometries, the fatigue crack initiation process was characterised by the nucleation of two cracks at the hole surface in
 diametrically opposite locations. A similar cracking behaviour under multiaxial cyclic loading, particularly in the early stage of
 growth, was seen by other researchers (Gryguć et al., 2019, 2020). The crack angles at the early stage of growth, α , as expected,
 were also affected by the B/T ratio, as exhibited in Figure 6 and in Table 5. The crack angle measured on the left side was named
 α_1 , while the crack angle measured on the right side was named α_2 . As can be seen, the increase in the B/T ratio, i.e. the decrease of
 shear stress level, leads to smaller α angles. Overall, although there are some exceptions, it was also found that both α angles of the
 same specimen were relatively similar.

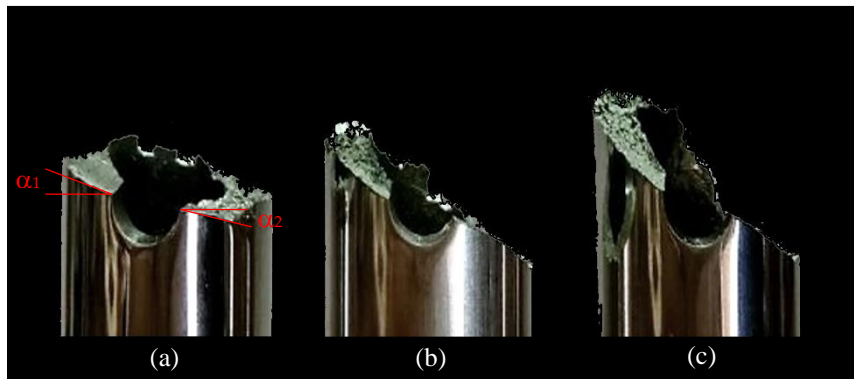


Figure 6. Fatigue crack initiation sites: (a) $B/T=2$; (b) $B/T=1$; and (c) $B/T=2/3$ (α_1 and α_2 represent the crack angles at the early stage of growth of the left side and the right side, respectively).

Table 5. Measured crack angles measured for the different tests in both sides of the hole.

Specimen	α_1 (degrees)	α_2 (degrees)	
BT3_2	21.92	25.26	234
BT3_1	26.16	24.86	235
BT1_1	23.2	20.25	236
BT1_2	11.98	17.01	237
BT1_3	13.98	17.45	238
BT2_1	12.15	12.62	239
BT2_2	13.56	14.11	240
BT2_3	8.13	17.59	241
α_1 : angle of the first crack (left side); α_2 : angle of the second crack (right side)			242
			243

The $a-N$ curves obtained in the experiments for both sides of the hole are shown in Figure 7. The measurements were fitted using third order polynomial functions, also plotted in the figure. The conventional boundaries of the curves defined to calculate N_i and N_f are marked on the graphs with bold black lines. The fatigue lives used in the analysis (both N_i and N_f) were those associated with the first crack detected in the hole. From the analysis of Figure 7, it can be concluded that in most cases, the second crack initiated after a considerable number of cycles relative to the initiation of the first crack. Nevertheless, in general, the second crack propagated faster than the first one and when the tests stopped the crack lengths were relatively similar.

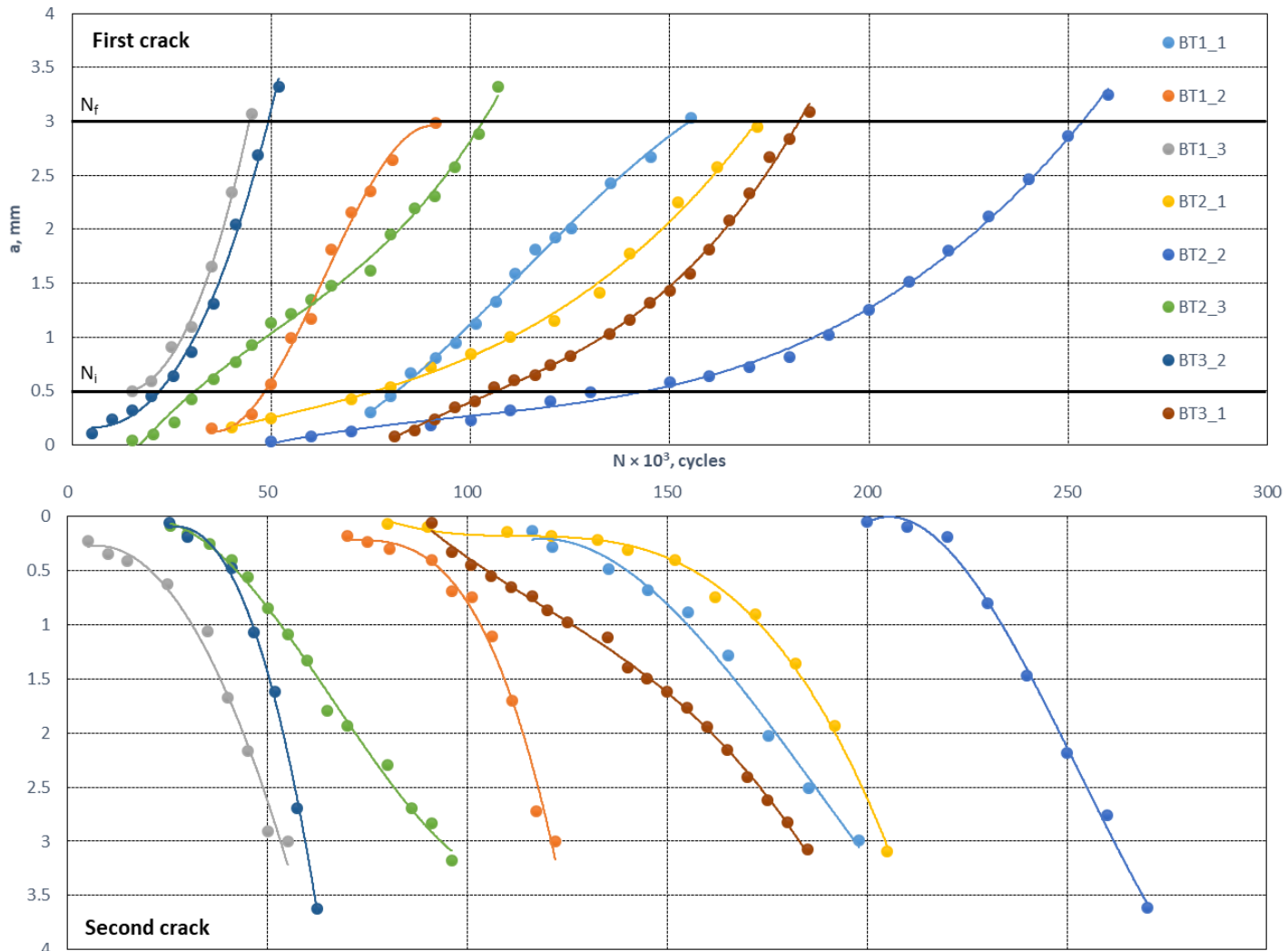


Figure 7. Examples of the a/N curves obtained from the tests for both cracks initiated in the hole region for the different B/T ratios.

The results of the fatigue crack initiation life N_i and the total fatigue life N_f are shown in Table 6. From Table 6, the effect of the B/T ratio on fatigue life is very clear. Figure 8 shows the mutual dependence between the fatigue crack initiation life and the total fatigue life for the tested cases. It is interesting to note that there is a well-defined relationship between both variables. This analysis clearly shows that the crack initiation occurs much earlier than the final fracture but, irrespective of the load conditions, the values of the N_i/N_f ratio are quite similar.

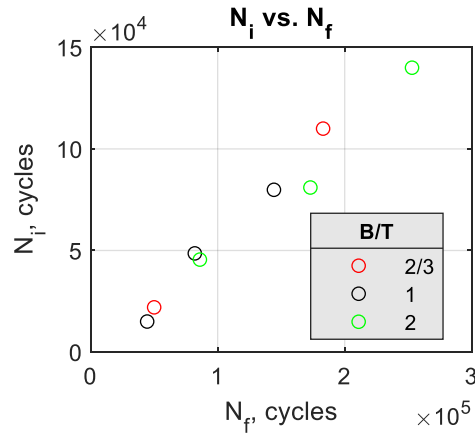
Table 6. Fatigue test results for crack initiation and total life.

Specimen	B/T ratio	N_i (cycles)	N_f (cycles)
BT3_2	2/3	110,000	183,000
BT3_1	2/3	22,000	50,000
BT1_1	1	79,878	144,296
BT1_2	1	48,564	82,000
BT1_3	1	15,000	44,500
BT2_1	2	81,000	173,000
BT2_2	2	140,000	253,000

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BT2_3	2	45,500	86,000
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N_i : fatigue crack initiation life; N_f : total fatigue life.

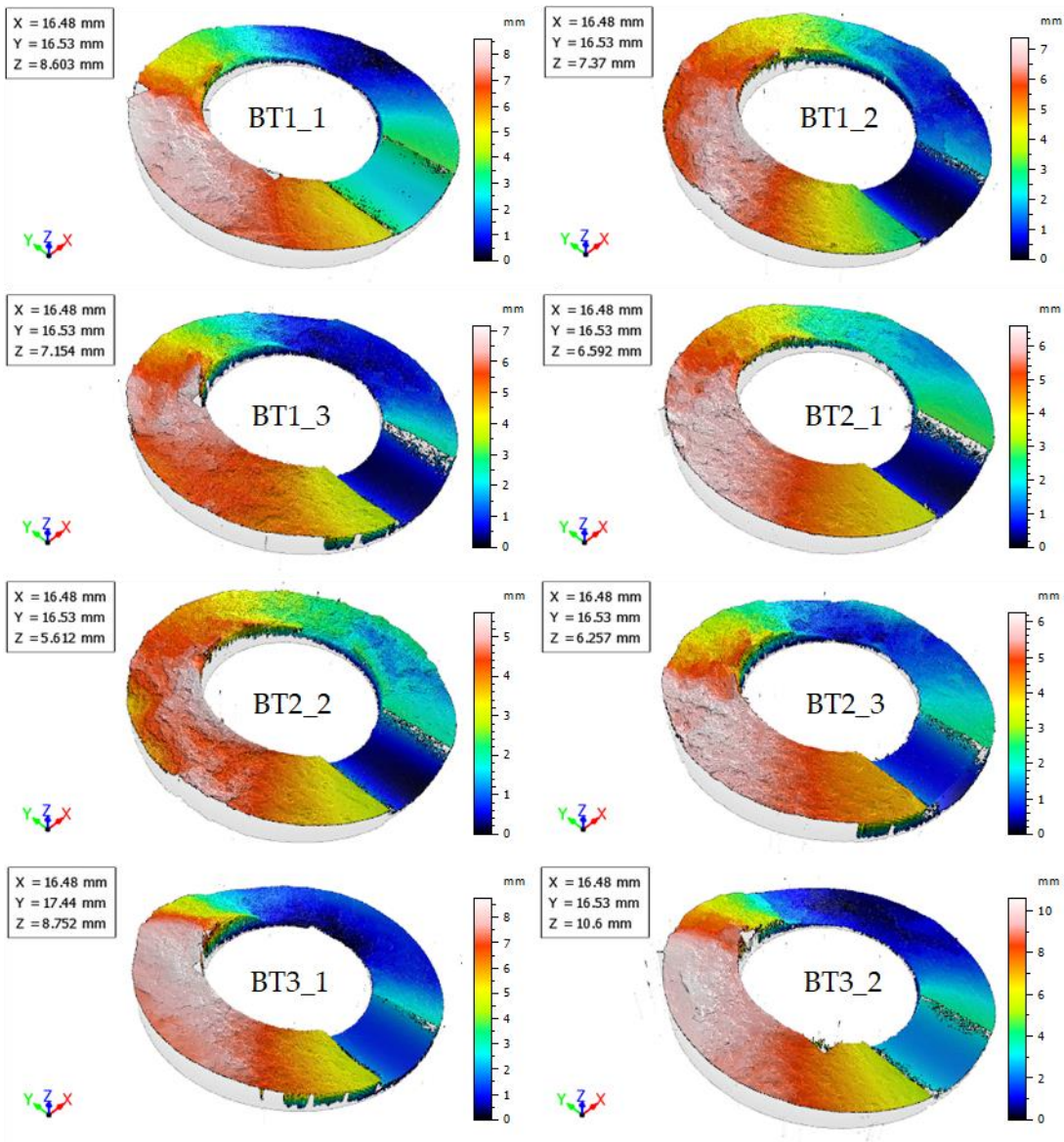


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263

Figure 8. Relationship between N_i and N_f for different B/T ratios.

264 3.2. Fracture surface topography

265 Figure 9 shows the fracture surfaces generated for the loading cases presented in Table 3. Figure 9(a) shows the original
266 surfaces while Fig. 9(b) shows the ROIs. For each B/T ratio, without taking into account the loading level, the general patterns of
267 the surface topography can be noted. The greater differences were noted on the z-axis scale for the cases subjected to higher shear
268 stress levels.



(a)

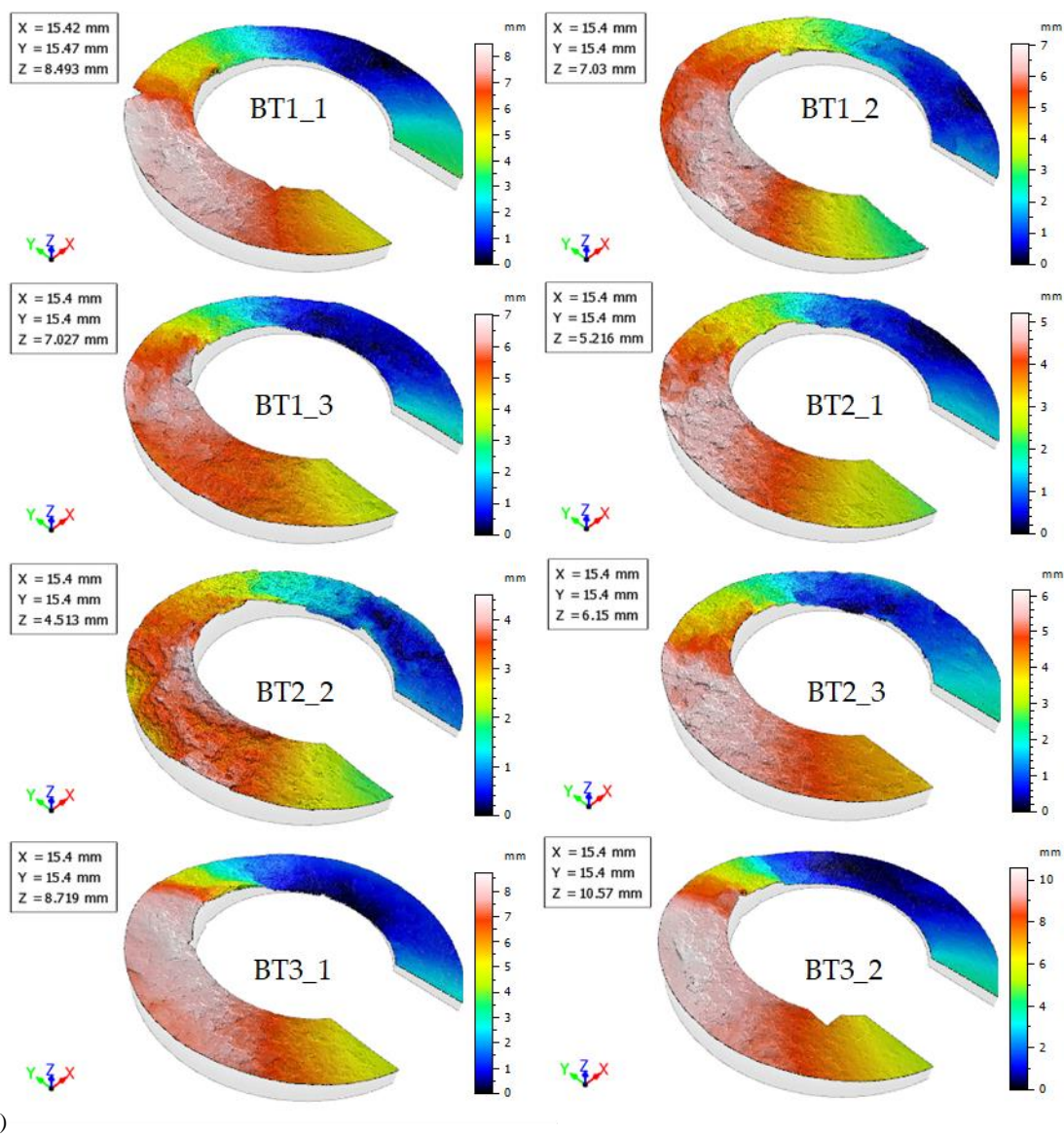


Figure 9. Fracture surfaces acquired after the tests for $B/T=2$, $B/T=1$, $B/T=2/3$: (a) original measured surfaces; and (b) regions of interest (ROI) considered in the analysis

Table 7 summarizes the fracture surface measurements carried out for the tested geometries using both S_x and V_x parameters, respectively. The columns with the parameters of the surface topography of fatigue fractures (S_q and V_v), which were used for further analysis and presented in the discussion, are marked in green. The other parameters were also investigated but revealed to be less interesting from the perspective of developing an accurate fatigue life prediction model. Figure 10 plots all measured S_x and V_x results against the B/T ratios. The results show that the increase of the shear stress level, i.e. the decrease of the B/T ratio, leads to higher values of the fracture surface topography parameters. The loading magnitude for a fixed B/T ratio also has a clear effect on S_x and V_x parameters.

Table 7. Summary of the S_x and V_x results measured for the different loading cases.

Specimen	S_q (μm)	S_p (μm)	S_v (μm)	S_z (μm)	S_a (μm)	V_m ($\mu\text{m}^3/\mu\text{m}^2$)	V_v ($\mu\text{m}^3/\mu\text{m}^2$)	V_{mc} ($\mu\text{m}^3/\mu\text{m}^2$)	V_{vc} ($\mu\text{m}^3/\mu\text{m}^2$)	V_{vv} ($\mu\text{m}^3/\mu\text{m}^2$)
BT3_2	3.71	5.46	5.10	10.57	3.45	0.024	4.764	4.289	4.695	0.069
BT3_1	3.03	4.40	4.32	8.72	2.85	0.022	3.764	3.346	3.696	0.068

BT1_1	2.68	4.40	4.09	8.49	2.41	0.020	3.750	3.010	3.650	0.106 ²⁸²
BT1_2	2.03	3.31	3.72	7.03	1.80	0.021	2.536	2.491	2.436	0.102 ²⁸³
BT1_3	2.15	3.79	3.23	7.03	1.99	0.030	2.720	2.510	2.670	0.050
BT2_1	1.56	2.68	2.54	5.22	1.40	0.015	2.073	1.808	2.015	0.058 ²⁸⁴
BT2_2	1.22	2.25	2.26	4.51	1.10	0.020	1.450	1.440	1.390	0.060
BT2_3	1.87	3.11	3.04	6.15	1.73	0.016	2.502	2.105	2.449	0.053 ²⁸⁵

Height parameters, S_x , and volume parameters, V_x , according to ISO 25178 standard.

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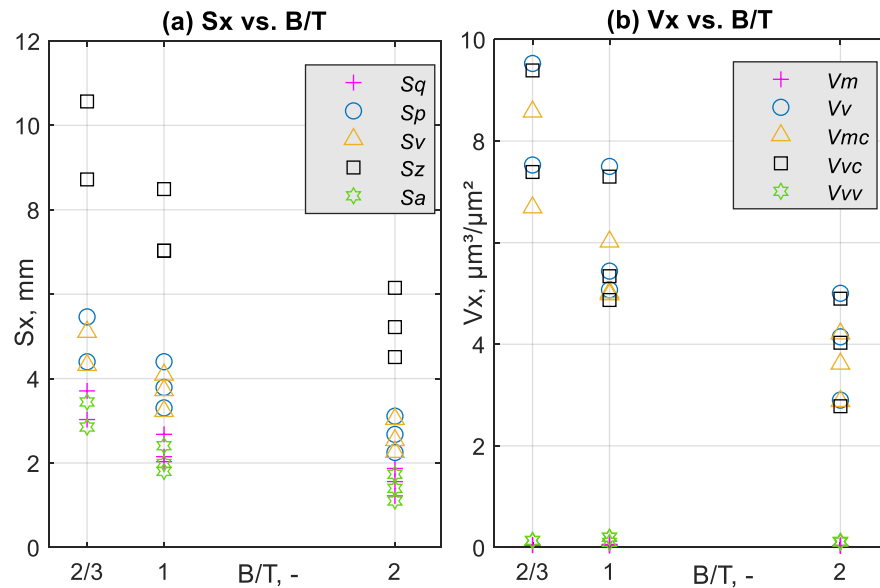


Figure 10. Surface topography parameters versus B/T ratio: (a) S_x ; and (b) V_x .

3.3. Maximum pit and valley locations

Figure 11 shows the location of the highest (Max) and lowest (Min) points for the extracted areas. The difference between the highest peak and the deepest valley also corresponds to the value of the S_z parameter, as reflected by the maximum scale value for each of the surfaces. The angles A and B associated with these two points relative to the specimen axis were also identified in the figure. It may be noticed that most of the extreme points were on the edges (inside or outside). Moreover, for the left side, the points were located in the second quadrant, while the position of the point on the right side varied between the first and the fourth quadrants.

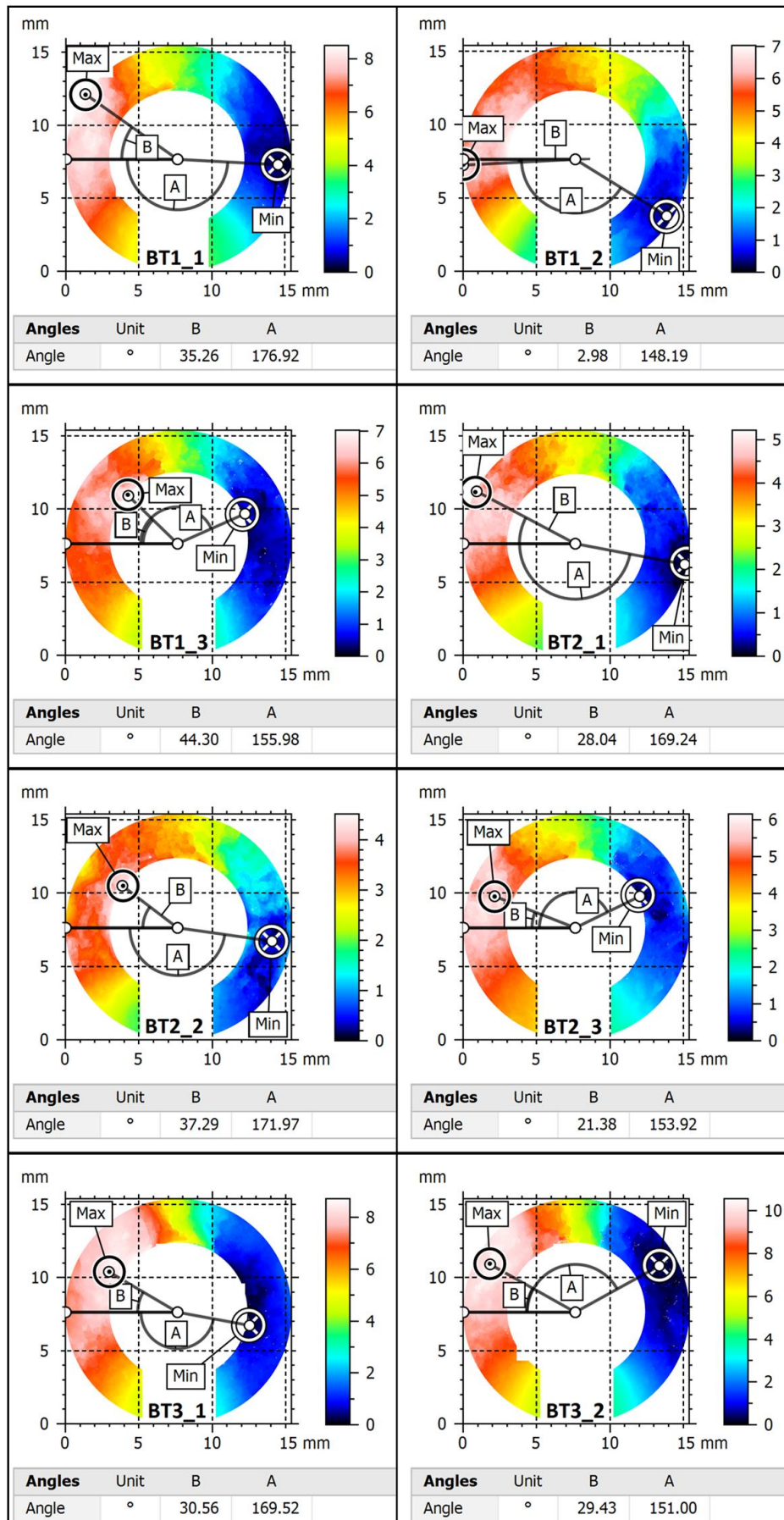


Figure 11. Maximum and minimum height of the extracted areas with their angles A and B for the different loading cases.

298 **Table 8.** Maximum and minimum height angles measured for the different loading cases.

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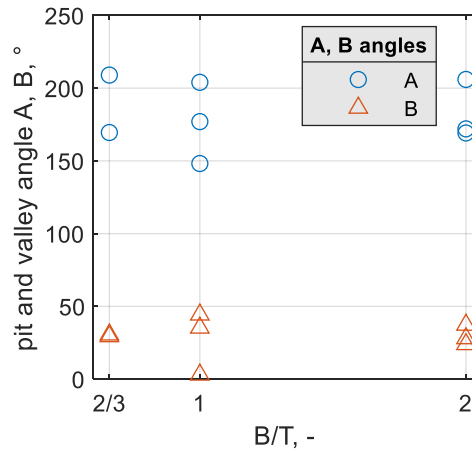
Specimen	A angle (degrees)	B angle (degrees)
BT3_2	209.0	29.4
BT3_1	169.5	30.6
BT1_1	177.0	35.3
BT1_2	148.2	3.0
BT1_3	204.0	44.3
BT2_1	169.2	28.0
BT2_2	172.0	37.3
BT2_3	206.0	23.9

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A: angle between the highest (Max) point and the x-axis of the extracted areas; B: angle between the lowest (Min) point and the x-axis of the extracted areas.

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301 Figure 12 presents a 2-D scatter plot of the data relating the A and B angles with the B/T ratios. There is a relatively high
 302 agreement of the results, either for the A angle or the B angle, regardless of the B/T ratio. This may suggest that all specimens had a
 303 similar shape distribution of the fracture features, only differing in terms of pits and valleys, as well as in terms of broadly understood
 304 roughness.



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306 **Figure 12.** Maximum B and minimum A angles versus B/T ratio.

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307 **3.4. Equivalent von Mises stress range**

308 The equivalent von Mises stress range $\Delta\sigma_{VM}$ used to reduce the multiaxial loading case to an equivalent uniaxial loading case
 309 was calculated numerically, near the hole region, using the FEM models developed in this study (see Section 2.3). These values
 were calculated for the node with maximum value of the first principal stress, which was assumed to be the crack initiation site. The
 values obtained for the different B/T ratios and loading magnitudes are summarised in Table 9. Figure 13 plots $\Delta\sigma_{VM}$ against N_i (Fig.
 13(a)) and against N_f (Fig. 13(b)) for the various B/T ratios. As can be seen, in both cases, these two variables correlate well, which
 is a good indication concerning the identification of an adequate fatigue damage quantifier for this material when subjected to these
 loading cases.

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Table 9. Equivalent von Mises stress range $\Delta\sigma_{VM}$ for the different loading cases.

Specimen	<i>B/T ratio</i>	$\Delta\sigma_{VM}$ (MPa)
BT3_1	2/3	587.6
BT3_2	2/3	846.1
BT1_1	1	574.1
BT1_2	1	704.9
BT1_3	1	845.8
BT2_1	2	584.7
BT2_2	2	584.0
BT2_3	2	713.5

$\Delta\sigma_{VM}$: local von Mises equivalent stress range

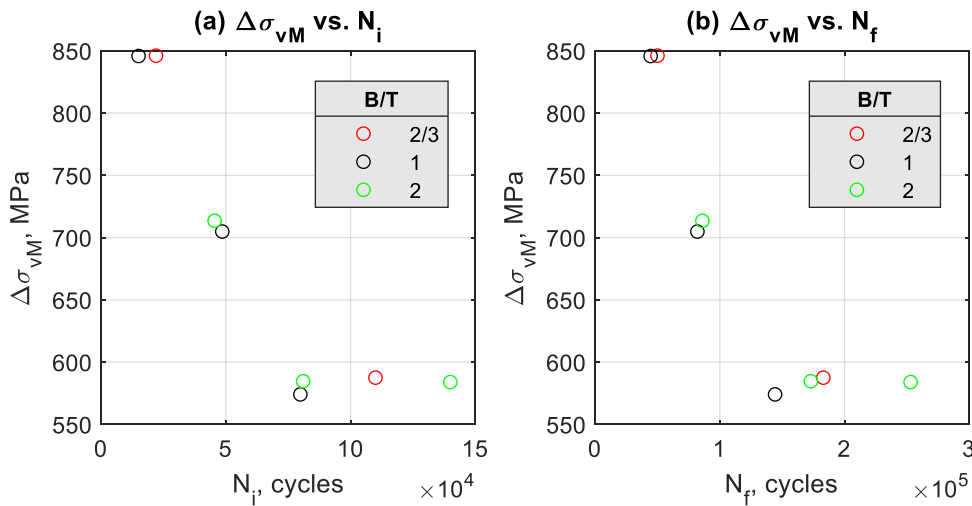


Figure 13. Equivalent von Mises stress range $\Delta\sigma_{VM}$ for different *B/T* ratios versus: (a) N_i ; and (b) N_f .

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4. Discussion

The analysis of the tested 18Ni300 steel specimens produced by SLM based on the *B/T* ratio, crack initiation life N_i , total life N_f , crack angles α , equivalent von Mises stress σ_{VM} , maximum and minimum height of the extracted areas and the associated angles *A* and *B*, and surface parameters *Sq* and *Vv* was conducted to quantitatively identify the fracture mechanisms and an adequate fatigue damage quantifier from the post-mortem fatigued surfaces. Moreover, qualitative SEM examination and surface topography analysis of characteristic fracture areas was also taken into consideration.

4.1. Cracking mechanisms

To investigate the effects of the *B/T* ratio and both the N_i and N_f values on the fracture surface topography in terms of the total fracture area, it is important to analyse the failure mechanisms in individual fracture zones. Examples of typical defects existing in

337 the samples introduced during the manufacturing process are presented in Fig. 14. The three views were reconstructed from SEM
338 micrographs taken with different magnifications to illustrate the main types of defects present in the AISI 18NI300 processed by
339 SLM, namely un-melted powder particles (Fig. 14(a)); an internal void (Figure 14(b)); and a lack of fusion (Fig. 14(c)). For any
340 material, but particularly for a SLMed material, defects play a principal role in crack initiation. Characteristic defects are indicated
341 in the 3D views with red arrows. In addition, a magnified image showing un-melted powder particles is presented (see red rectangle)
342 in the upper part of Figure 14 (see the red rectangle). For the sake of clarity, common topography (z-axis) scales for the individual
343 3D views are also exhibited in the right-hand side. Voids and cavities during the cyclic loadings introduce micro stresses, possibly
344 larger than the yield stress, leading to local plastic deformation and easing the fatigue crack initiation. Obviously, if defects are
345 nearer the surface, they have a greater possibility to cause failure, since there is a smaller way for an open space.

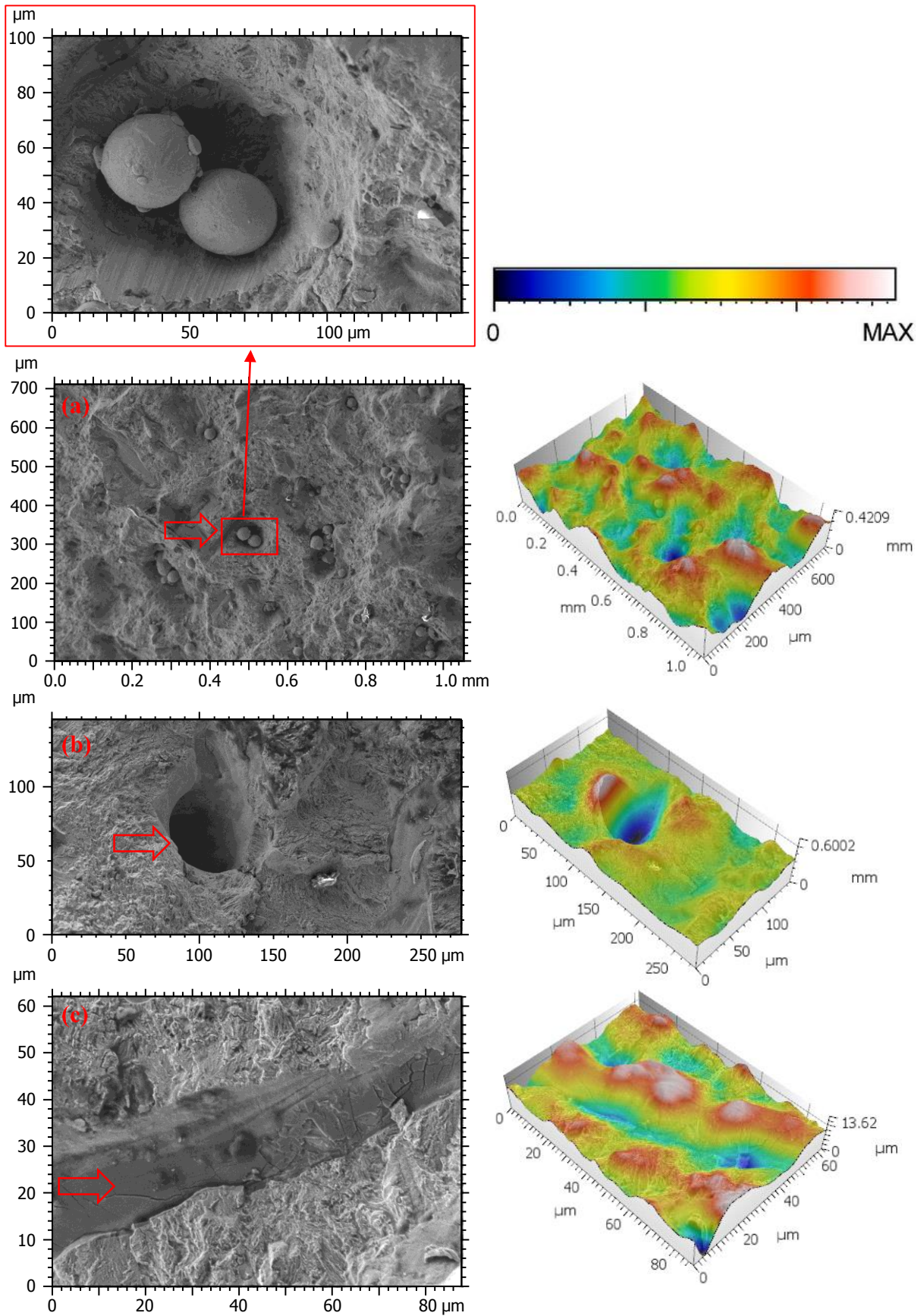


Figure 14. SEM micrograph with 3D pseudo-colour views of the reconstructed areas containing: (a) un-melted powder particles; (b) internal void; and (c) lack of fusion.

349 Surface roughness is the result of the simultaneous interaction of many independent factors, both random and determined,
350 and as a result, it has a very complex microgeometry. There are obvious differences between individual fracture zones, as shown in
351 Figure 15, if we compare initiation sites or propagation regions. Although these differences are obvious, the methodology proposed
352 here considers the fractured surfaces as a total area, not distinguishing the specificities of the individual regions.

353 The microstructural and mechanical anisotropy, for materials produced by AM methods, occurs by itself in the process of
354 grain formation along the build-up direction. However, the occurrence of isotropy/anisotropy on the fracture surface is rarely con-
355 sidered. An important property of a material or structure failure is the form of the elasto-plasticity coupled with isotropic or aniso-
356 tropic damage. Nevertheless, this property is strictly related to the isotropy/anisotropy of the measured fracture surface. The di-
357 rectivity of the geometric structure of the surface depends on the fracture zone and it results from the kinematics of the fracture
358 process. The isotropy of a medium is generally based on the fact that it exhibits the same physical or geometric properties in all
359 directions. The isotropy of a surface, therefore, means that the surface has the same structure in all directions. It is also a perfectly
360 symmetrical structure with respect to all possible axes of symmetry.

361 In the examined case, the isotropy was determined by analyzing the autocorrelation function (see Fig. 15). For the initiation
362 zone, represented in the pink background of Figure 15(b), the shape of this function is asymmetric, slender, and elongated in one
363 direction for anisotropic surfaces. The isotropy in this case was approximately 27%. On the other hand, the circular and symmetrical
364 function graphs for isotropic surfaces reached the isotropy value of almost 83% (see Fig. 15(c), green colour).

365 Figure 15 also presents general information (see the top of Fig. 15) generated via MountainsMap software depending on the
366 data supported by the AL3D file format, where information on the entire measured surface is presented on a white background (see
367 Fig. 15(a)), and the lower part of Fig. 15 shows the distribution of slope and orientation of all triangular tiles formulating the surface
368 with their computed values. Both histograms related to the distribution of slope and orientation of the surface have left-side concen-
369 trated distributions, especially for the initiation area. The highest value for the circular mean parameter was found for the propagation
370 surface (26.512°) whereas the lower value (19.382°) was associated with the initiation region. The mean resultant length parameter
371 has a value of about 0.9 for both zones. Moreover, the main parameter had the highest value for the initiation zone (11.534°) whereas
372 for the propagation region it was equal to 5.215° .

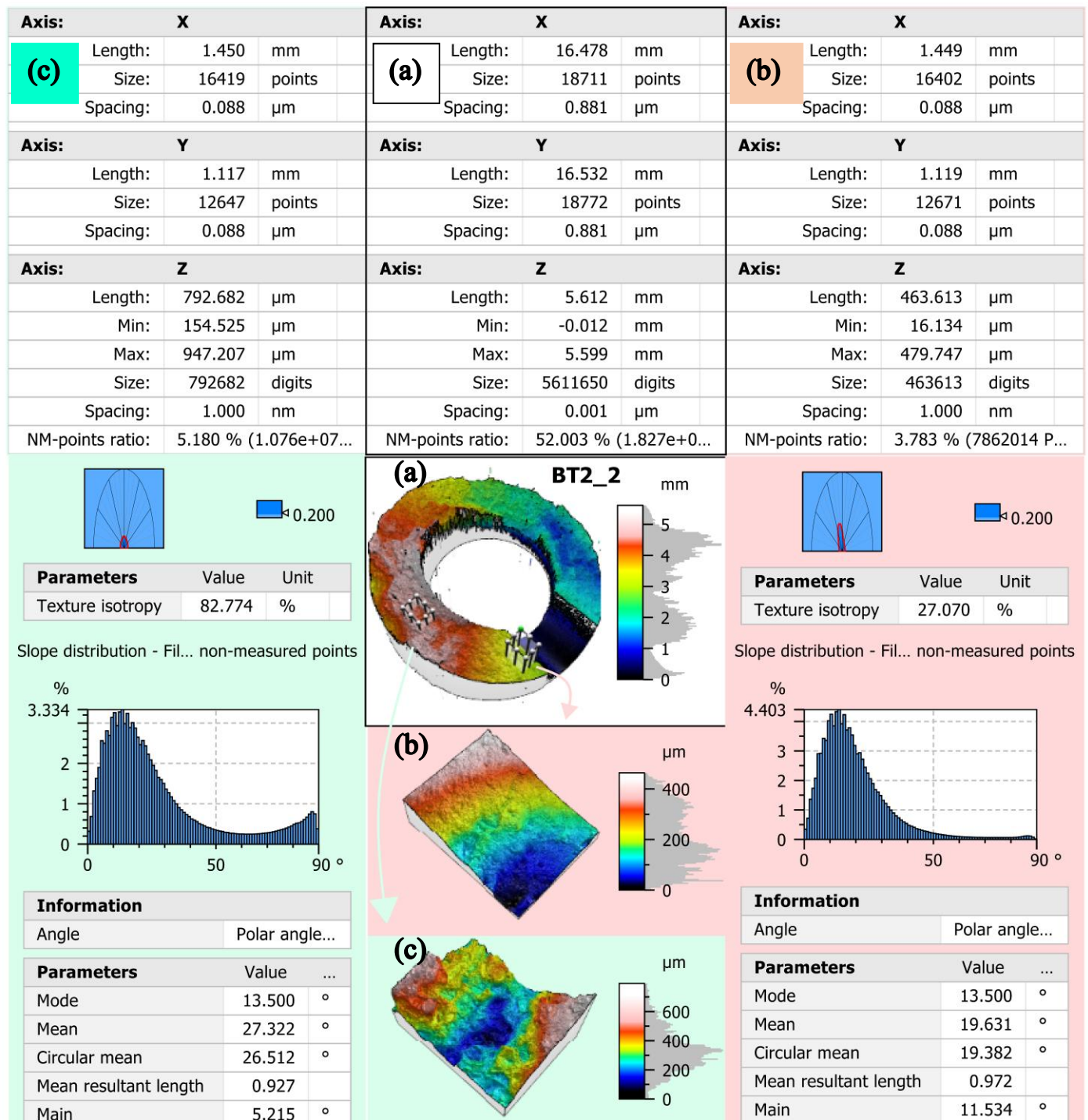


Figure 15. Identification cards for the measured data files, slope distribution histograms and (a) total fractured surface views with marked and magnified (b) initiation and (c) propagation crack zones (BT2_2 specimen).

4.2. Effect of loading conditions on fatigue crack behaviour

Fig. 16 shows four subplots regarding the relation between the: α_1 and angles α_2 (Fig. 16(a)); maximum pit A and minimum valley B (Fig. 16(b)); α angles and the equivalent von Mises stress range $\Delta\sigma_{vM}$ (Fig. 16(c)); and maximum pit and minimum valley and the equivalent von Mises stress range $\Delta\sigma_{vM}$ (Fig. 16(d)). It can be seen that both α angles increase with the shear stress component according to the sequence $B/T = 2, 1, 2/3$ (see Fig. 16(a)). Concerning the values of the maximum pit and minimum valley, see Fig. 16(b), the main trends are not evident. For the lower subplots, either Fig. 16(c) or Fig. 16(d), there is no clear dependence of the analysed angles on the von Mises equivalent stress range $\Delta\sigma_{vM}$.

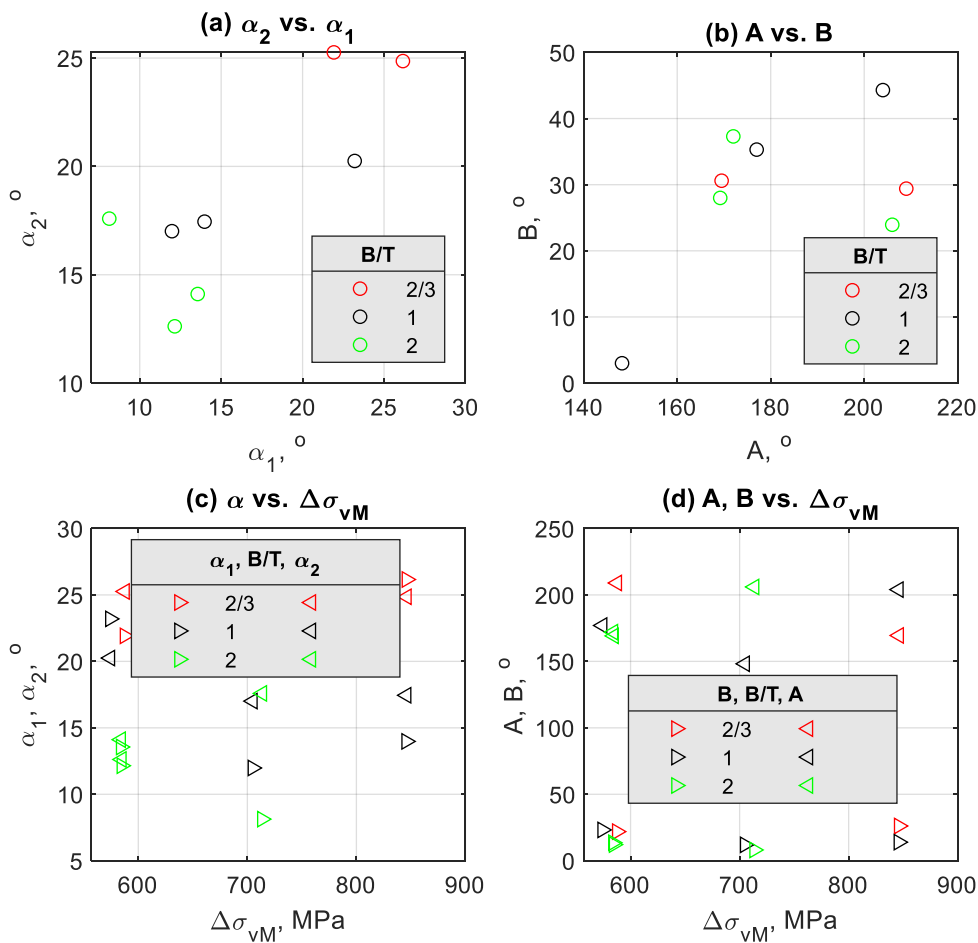
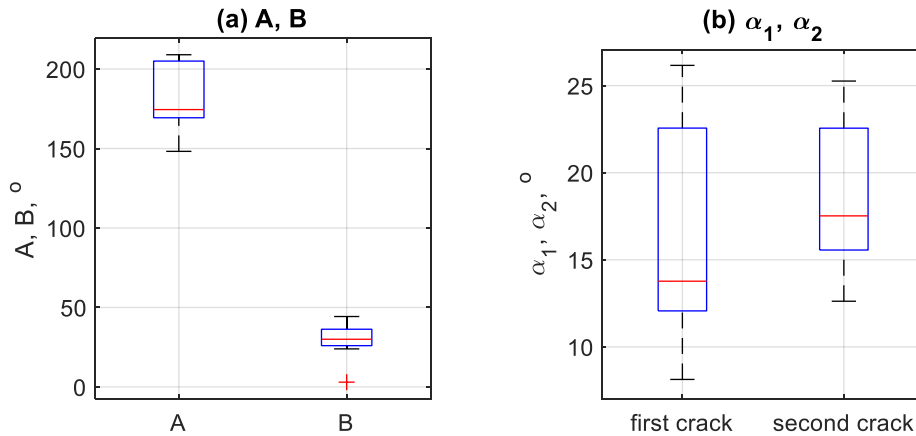


Figure 16. Relationship between: (a) α_1 and angles α_2 ; (b) maximum pit A and minimum valley B; (c) α angles and the equivalent von Mises stress range $\Delta\sigma_{vM}$; and (d) maximum pit A and minimum valley B and the equivalent von Mises stress range $\Delta\sigma_{vM}$.

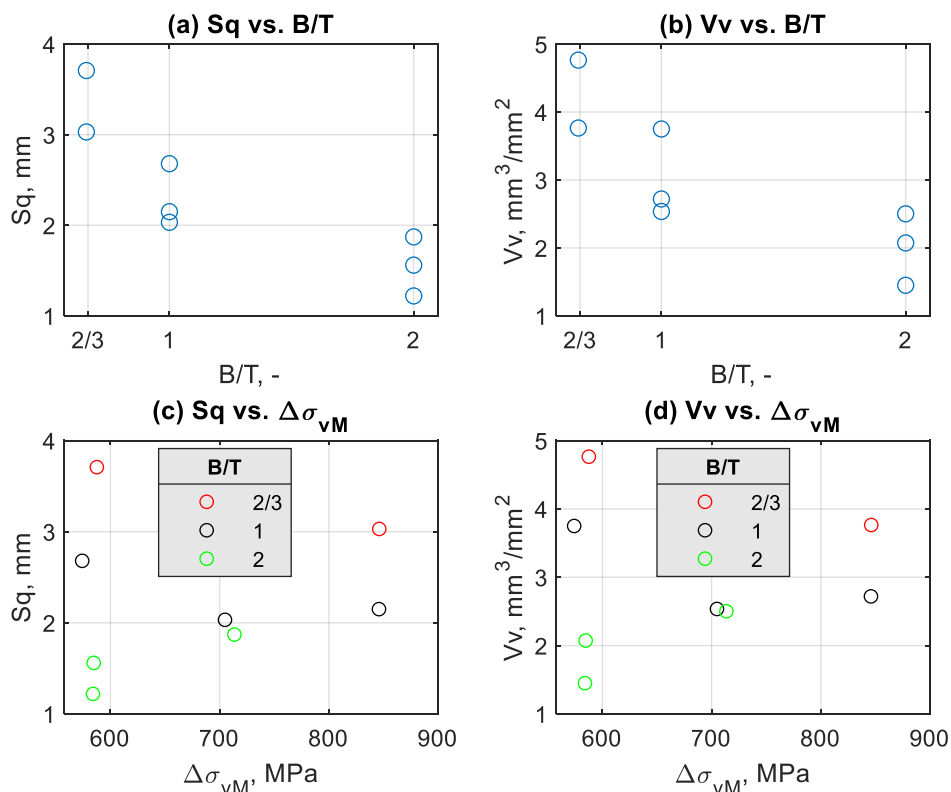
In each boxplot of Fig. 17, the central mark (red line) indicates the median value, and the bottom and top edges of the box indicate the 25th and 75th percentiles, respectively. The whiskers extend to the most extreme data points not considered outliers, and the outliers are plotted individually using the '+' marker symbol. Based on the analysis of all specimen, according to Fig. 17(a), the median values of angles A and B, were 174.5° and 30°. the minimum values were 148.2° and 3°, and the maximum values were about 209° and 44.3°, respectively. In Fig. 17(b), for α_1 and α_2 angles, the median values were 13.77° and 17.52°, respectively. The minimum and maximum values of the crack angles were already listed in Table 5.



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394 **Figure 17.** Boxplot: (a) maximum pit A and minimum valley B ; (b) α_1 and α_2 angles.

395 *4.3. Effect of B/T ratio, crack angles and equivalent stress range on fracture surface parameters*

396 In order to better understand the effect of the B/T ratio on fracture surface features, a detailed analysis based on the Sq and Vv
 397 parameters was performed. These parameters turned out to be the most adequate based on the linear fitting analysis. Fig. 18 shows
 398 the relationship between the selected height and functional parameters (Sq and Vv) and the B/T ratio. The same figure shows the
 399 dependencies of the same surface topography parameters on the equivalent von Mises stress range $\Delta\sigma_{vM}$. The surface topography
 400 parameters (Sq , and Vv) decreased with increasing values of the B/T ratio. Fig. 19 analyses the relationship between the fracture
 401 surface parameters (Sq and Vv) and the fatigue life parameters (N_i and N_f). It is clear from these two above-mentioned figures, i.e.
 402 Fig. 18 and Fig. 19, that these parameters and the B/T ratio do not show satisfactory consistency in terms of linear functions for all
 403 tested specimens. Therefore, in the subsequent analysis, a combined model encompassing various parameters is used. The general
 404 tendency found from both Fig. 18 and Fig. 19 is that the smaller the B/T ratio, the greater the roughness.



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Figure 18. Relationship between the selected height Sq and volume Vv surface parameters, B/T ratio, and the equivalent von Mises stress range $\Delta\sigma_{vM}$; (a) Sq versus B/T ; (b) Vv versus B/T ; (c) Sq versus $\Delta\sigma_{vM}$; and (d) Vv versus $\Delta\sigma_{vM}$.

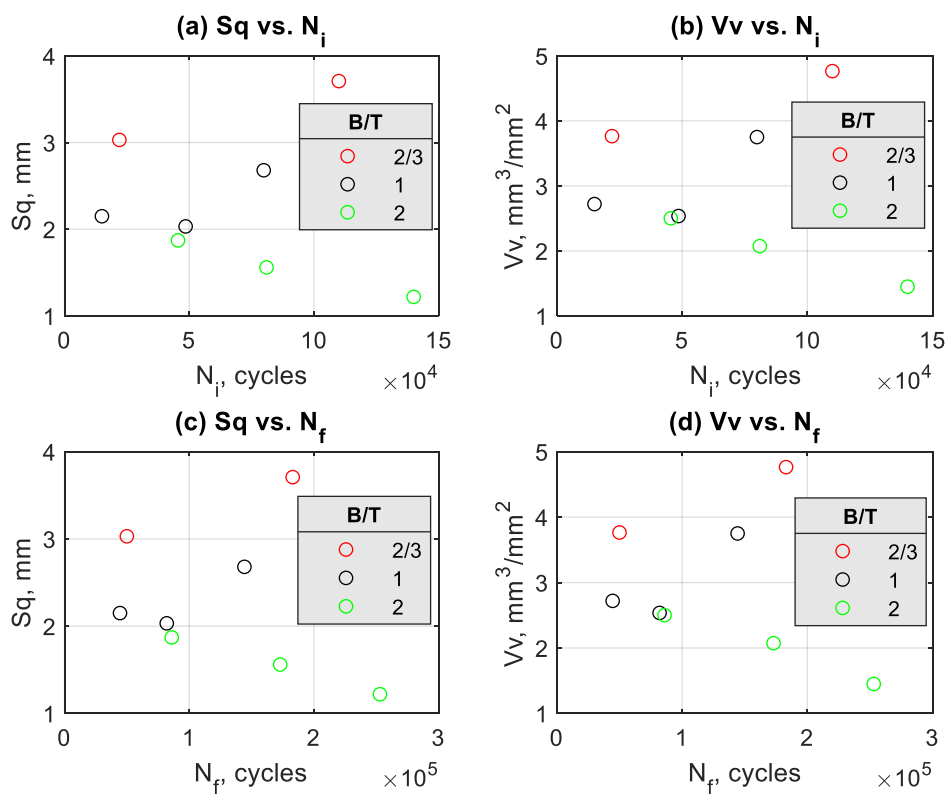


Figure 19. Relationship between the selected height Sq and volume Vv surface parameters, fatigue crack initiation life N_i , and the total fatigue life N_f ; (a) Sq versus N_i ; (b) Vv versus N_i ; (c) Sq versus N_f ; and (d) Vv versus N_f .

411 4.4. Fatigue life prediction from fracture surface parameters and equivalent von Mises stress

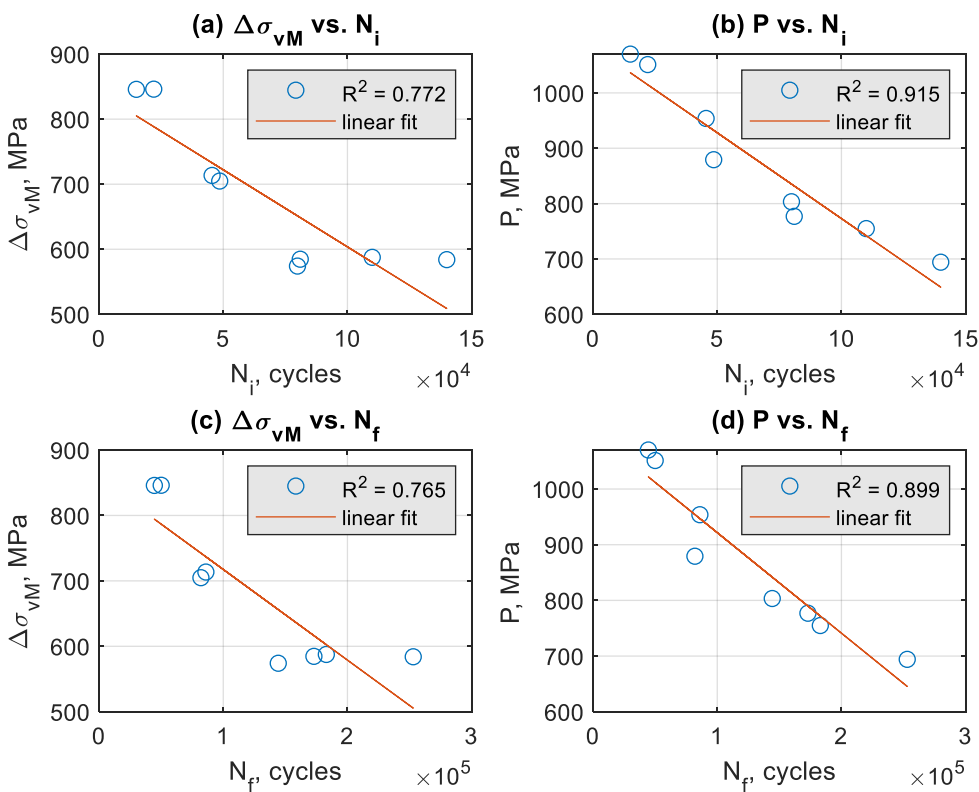
412 Due to the complexity of multiaxial fatigue, it is fundamental to identify robust fatigue damage parameters to effectively
 413 assess the fatigue lifetime. Thus, in this study, the multiaxial fatigue life is predicted by using the novel fracture surface state
 414 parameter P (see Eq. (2)) which combines two topography characteristics (the height parameter Sq , and the functional parameter
 415 Vv) with the equivalent von Mises stress range, $\Delta\sigma_{VM}$. Fig. 20 plots, respectively, the equivalent von Mises stress range $\Delta\sigma_{VM}$ and
 416 the P parameter against the fatigue life in terms of crack initiation life N_i (Figure 20(a) and Figure 20(b)) and total fatigue life N_f
 417 (Figure 20(c) and Figure 20(d)). Through the values of the coefficient of determination R^2 , it can be observed a better correlation
 418 for the P parameter than for the equivalent local von Mises stress range $\Delta\sigma_{VM}$.

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$$P = \frac{Vv}{Sq} \Delta\sigma_{VM} \quad (2)$$

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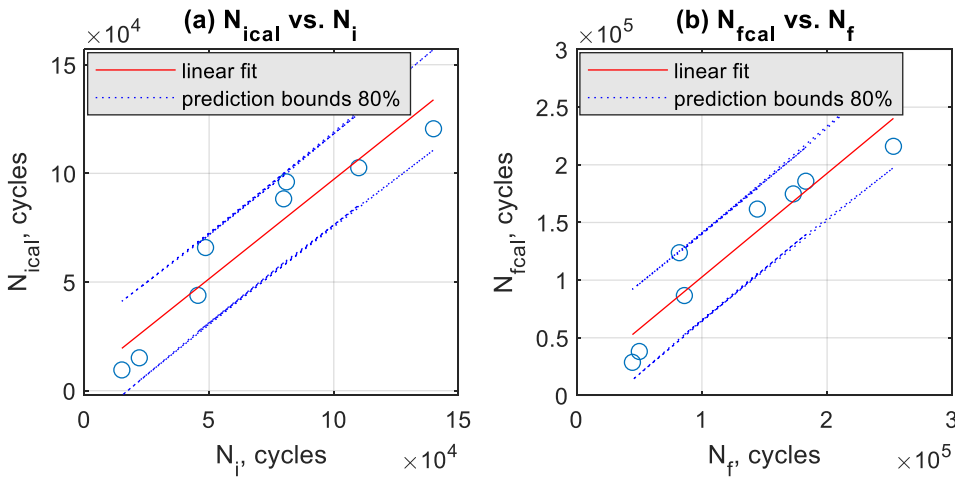
Figure 20. Equivalent local von Mises stress range $\Delta\sigma_{VM}$ and topographic stress factor P versus fatigue crack initiation life N_i and total fatigue life N_f with a linear fit: (a) $\Delta\sigma_{VM}$ versus N_i ; (b) P versus N_i ; (c) $\Delta\sigma_{VM}$ versus N_f ; and (d) P versus N_f .

The fatigue crack initiation life N_i and the fitted fatigue crack initiation life N_{ical} computed from the fracture surface parameter function obtained from the experimental data (see Eq. (3)), i.e. a simple linear function, is compared in Fig. 21(a). The same comparison but in terms of total fatigue life N_f , carried out using the linear function defined in Eq. (4)), is presented in Fig. 21(b). As can be seen, the calculations correlate well with the experimental results for this geometry under bending-torsion loading.

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$$N_{ical} = -295.2 \times P + 325449 \quad (3)$$

$$N_{fcal} = -498.2 \times P + 561920 \quad (4)$$



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Figure 21. Comparison of predicted and experimental lives carried out in terms of N_i and N_f ; (a) N_{ical} versus N_i ; and (b) N_{ical} versus N_f .

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The prediction bounds define the lower and upper values of the associated interval and define the width of the interval. The width of the interval indicates how uncertain are the fitted coefficients, the predicted observation, or the predicted fit. The bounds are defined with a level of certainty of 80%. It gives a 20% chance of being incorrect about predicting a new observation. This interval indicates 80% chance that the new fatigue test result is actually contained within the lower and upper prediction bounds. In order to better analyse the accuracy of the proposed approach, the crack initiation lives calculated with new P parameter, called here $N_{ical}(P)$, were compared to those obtained with the Smith-Watson-Topper (SWT) parameter, called here $N_{ical}(SWT)$, following the methodology introduced by Branco et al. (Branco et al., 2021a). Nevertheless, it should be noted that the Branco's approach is designed to deal with a crack length defined from the El-Haddad parameter but here, for the sake of comparability, it was applied for a crack length equal to 0.5 mm, as defined in Section 2.

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Figure 22 compares the fatigue lives obtained from the two different approaches. The dashed lines correspond to a life scatter factor of 1.5, and the dotted lines correspond to a life scatter factor of 2. It can be seen that for both computational approaches, $N_{ical}(P)$ and $N_{ical}(SWT)$, there is a high agreement with the experimental values. Furthermore, the proposed model has a good agreement with the experiment data, all point fall within the ± 2 scatter bands and most of them fall within ± 1.5 scatter bands. The cases of the SWT-based approach that do not fall within the ± 1.5 scatter bands are samples with higher crack initiation life values, near 10^5 cycles, which can be seen as non-conservative exceedance. The P -based approach also has some points out of the ± 1.5 scatter bands for the minimum N_i values which can be interpreted as conservative exceedance.

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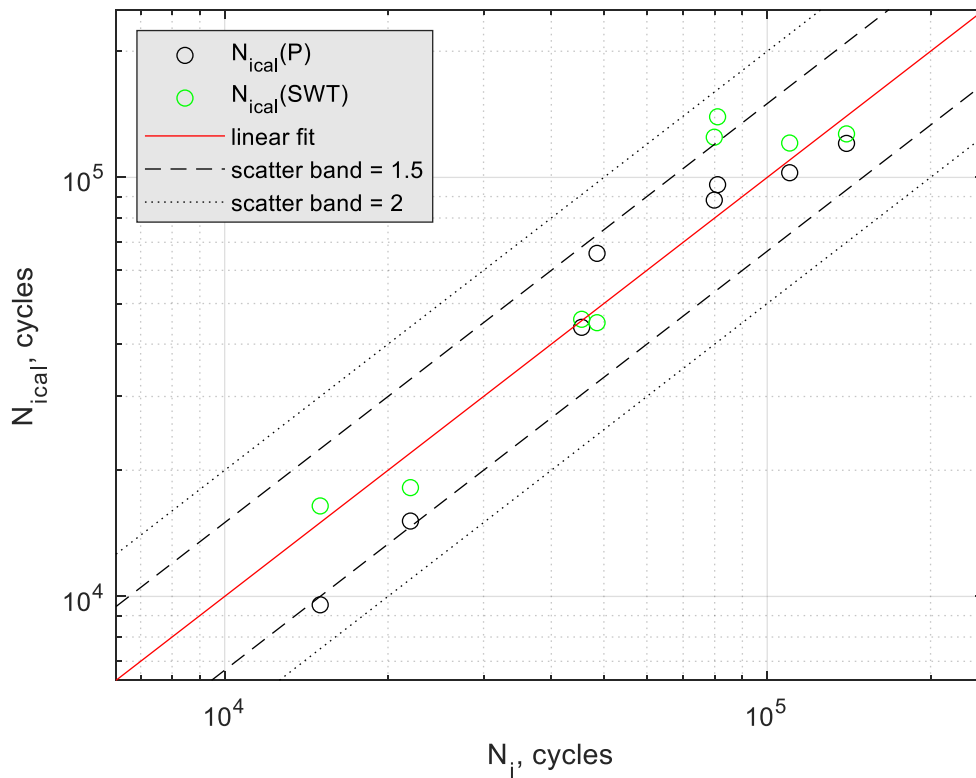
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454 **Figure 22.** Comparison in log-log scales between the predicted N_{ical} and the experimental N_i .

455 **5. Conclusions**

456 The effect of the bending-torsion ratio B/T on fracture surface parameters has been studied for hollow geometries with a lateral
457 hole made of 18Ni300 steel produced by SLM. Fatigue failure was characterised by the initiation and growth of two cracks at
458 diametrically opposite sites around the hole surface. A quantitative analysis of the entire fracture areas of the tested specimens was
459 performed for each loading case. A new equivalent fracture damage parameter based on the local von Mises stress range and
460 fracture surface parameters is proposed in this study. The conclusions can be summarized as follows:

- 461 - The shear stress level had a strong influence not only on crack angles and fatigue life but also on surface topography measurements,
462 either based on area S_x or volume V_x parameters;
- 463 - The maximum pits (**Max**) and the minimum valleys (**Min**) were located on the edges of the fracture surfaces and their distributions
464 were similar for all specimens, irrespective of the B/T ratio and stress amplitude;
- 465 - For the initiation zone, the surface showed the properties of an anisotropic surface. On the contrary, for the propagation zone, the
466 surface exhibited an isotropic property;
- 467 - The equivalent local von Mises stress range $\Delta\sigma_{vM}$ turned out to be a good **fatigue damage** quantifier, reason why it was used as the
468 main component of the new P parameter, allowing to estimate the fatigue life;
- The model based on the SWT parameter exhibited almost similar predictive capabilities than the model based on the P parameter,
which demonstrates the accuracy of the proposed parameter;
- The new post-failure equivalent damage parameter P , which accounts for the fracture surface state and the local von Mises stress
range, seems to reflect the physical failure conditions of this material under bending-torsion loading;
- The fatigue lives predicted using the proposed model agreed well with the experiments, with most predictions within scatter bands
with factors of ± 1.5 and all points within scatter bands with factors of ± 2 .

475 **Nomenclature**

476	a	mm	crack length
477	A	°	Minimum point for Z axis in the XY plane angle
478	B	°	Maximum point for Z axis in the XY plane angle
479	B/T	-	bending moment to torsion moment ratio
480	E	GPa	Young's modulus
481	F	N	force
482	L/h	mm	finite element model dimensions ratio
483	N_i	cycles	number of cycles to crack initiation
484	N_f	cycles	number of cycles to failure
485	P	MPa	topographic stress factor
486	R	-	stress ratio
487	R^2	-	coefficient of determination
488	S_a	μm	arithmetical mean height
489	S_k	μm	core height
490	S_q	μm	root mean square height
491	S_z	μm	maximum height
492	V_{mc}	μm ³ /μm ²	core material volume
493	V_{mp}	μm ³ /μm ²	peak material volume
494	V_v	μm ³ /μm ²	void volume
495	V_{vc}	μm ³ /μm ²	core void volume
496	V_{vv}	μm ³ /μm ²	pit void volume
497	k'	MPa	cyclic hardening coefficient
498	α	°	crack angle
499	ε_i	%	strain at failure
500	ϕ	%	porosity
501	ρ	g/cm ³	density
502	σ_{YS}	MPa	yield strength
503	σ_{UTS}	MPa	tensile strength
504	ν	-	Poisson's ratio
505	σ_a	MPa	nominal normal stress amplitude
506	σ_m	MPa	nominal normal mean stress
507	$\Delta\sigma_{vM}$	MPa	local von Mises equivalent stress range
508	τ	MPa	nominal shear stress
509	τ_a	MPa	nominal shear stress amplitude
510	τ_m	MPa	nominal shear mean stress

512 **Acknowledgement:** Financial support of these studies from Gdańsk University of Technology by the DEC-10/2021/IDUB/IV.2/EUROPIUM
 513 grant under the European Short-Term Outgoing visit—"Excellence Initiative—Research University" program is gratefully acknowledged. This
 514 research is sponsored by FEDER funds through the program COMPETE—Programa Operacional Factores de Competitividade—and by national
 funds through FCT—Fundação para a Ciência e a Tecnologia—under the project UIDB/00285/2020.

References

Avanzini, A., 2022. Fatigue Behavior of Additively Manufactured Stainless Steel 316L. *Materials* 2023, Vol. 16, Page 65 16, 65. <https://doi.org/10.3390/MA16010065>

Azevedo, C.R.F., Marques, E.R., 2010. Three-dimensional analysis of fracture, corrosion and wear surfaces. *Eng Fail Anal* 17, 286–300. <https://doi.org/10.1016/J.ENGFAILANAL.2009.06.010>

- 522 Bartoszuk, M., 2021. Approximately Model of the Maximum Temperature on the Chip Surface. *Materials* 2021, Vol. 14, Page 2592 14, 2592.
523 <https://doi.org/10.3390/MA14102592>
- 524 Branco, R., Antunes, F.V., Costa, J.D., 2015. A review on 3D-FE adaptive remeshing techniques for crack growth modelling. *Eng Fract Mech*
525 141, 170–195. <https://doi.org/10.1016/J.ENGFRACMECH.2015.05.023>
- 526 Branco, R., Costa, J.D., Borrego, L.P., Berto, F., Razavi, S.M.J., Macek, W., 2021a. Comparison of different one-parameter damage laws and
527 local stress-strain approaches in multiaxial fatigue life assessment of notched components. *Int J Fatigue* 151, 106405.
528 <https://doi.org/10.1016/J.IJFATIGUE.2021.106405>
- 529 Branco, R., Costa, J.D., Martins Ferreira, J.A., Capela, C., Antunes, F. v., Macek, W., 2021b. Multiaxial fatigue behaviour of maraging steel
530 produced by selective laser melting. *Mater Des* 201, 109469. <https://doi.org/10.1016/j.matdes.2021.109469>
- 531 Branco, R., Prates, P.A., Costa, J.D., Berto, F., Kotousov, A., 2018. New methodology of fatigue life evaluation for multiaxially loaded notched
532 components based on two uniaxial strain-controlled tests. *Int J Fatigue* 111, 308–320. <https://doi.org/10.1016/j.ijfatigue.2018.02.027>
- 533 Brodie, E.G., Richter, J., Wegener, T., Molotnikov, A., Niendorf, T., 2022. Influence of a remelt scan strategy on the microstructure and fatigue
534 behaviour of additively manufactured biomedical Ti65Ta efficiently assessed using small scale specimens. *Int J Fatigue* 162, 106944.
535 <https://doi.org/10.1016/J.IJFATIGUE.2022.106944>
- 536 Buljac, A., Helfen, L., Hild, F., Morgener, T.F., 2018. Effect of void arrangement on ductile damage mechanisms in nodular graphite cast iron:
537 In situ 3D measurements. *Eng Fract Mech* 192, 242–261. <https://doi.org/10.1016/J.ENGFRACMECH.2018.01.008>
- 538 Cunha, Â., Marques, A., Silva, M.R., Bartolomeu, F., Silva, F.S., Gasik, M., Trindade, B., Carvalho, Ó., 2022. Laser powder bed fusion of the
539 steels used in the plastic injection mould industry: a review of the influence of processing parameters on the final properties. *The*
540 *International Journal of Advanced Manufacturing Technology* 2022 121:7 121, 4255–4287. <https://doi.org/10.1007/S00170-022-09588-0>
- 541 de Freitas, M., Reis, L., Meggiolaro, M.A., de Castro, J.T.P., 2017. Stress scale factor and critical plane models under multiaxial proportional
542 loading histories. *Eng Fract Mech* 174, 104–116. <https://doi.org/10.1016/J.ENGFRACMECH.2016.12.016>
- 543 Demir, O., Ayhan, A.O., İriç, S., 2019. A novel test system for mixed mode-I/II/III fracture tests – Part 2: Experiments and criterion development.
544 *Eng Fract Mech* 220, 106671. <https://doi.org/10.1016/J.ENGFRACMECH.2019.106671>
- 545 Deng, Q.Y., Zhu, S.P., He, J.C., Li, X.K., Carpinteri, A., 2022. Multiaxial fatigue under variable amplitude loadings: review and solutions.
546 *International Journal of Structural Integrity* 13, 349–393. <https://doi.org/10.1108/IJSI-03-2022-0025/FULL/XML>
- 547 Deng, Q.Y., Zhu, S.P., Niu, X., Lesiuk, G., Macek, W., Wang, Q., 2023. Load path sensitivity and multiaxial fatigue life prediction of metals
548 under non-proportional loadings. *Int J Fatigue* 166, 107281. <https://doi.org/10.1016/J.IJFATIGUE.2022.107281>
- 549 Djukic, M.B., Bakic, G.M., Sijacki Zeravcic, V., Sedmak, A., Rajcic, B., 2019. The synergistic action and interplay of hydrogen embrittlement
550 mechanisms in steels and iron: Localized plasticity and decohesion. *Eng Fract Mech* 216, 106528.
551 <https://doi.org/10.1016/J.ENGFRACMECH.2019.106528>
- 552 Elkhateeb, M.G., Liu, S., Shin, Y.C., 2022. Extended mechanics of structural genome for predicting mechanical properties of additively
553 manufactured Ti6Al4V considering porosity and microstructure. *Mechanics of Materials* 169, 104300.
554 <https://doi.org/10.1016/J.MECHMAT.2022.104300>
- 555 Fan, J., Zhao, Y., 2022. Quantitative thermography for fatigue damage assessment and life prediction of welded components. *Mechanics of*
556 *Materials* 164, 104120. <https://doi.org/10.1016/J.MECHMAT.2021.104120>
- 557 Fergani, O., Bratli Wold, A., Berto, F., Brotan, V., Bambach, M., 2018. Study of the effect of heat treatment on fatigue crack growth behaviour of
316L stainless steel produced by selective laser melting. *Fatigue Fract Eng Mater Struct* 41, 1102–1119. <https://doi.org/10.1111/FFE.12755>
- Garcias, J.F., Martins, R.F., Branco, R., Marciniak, Z., Macek, W., Pereira, C., Santos, C., 2021. Quasistatic and fatigue behavior of an AISI H13
steel obtained by additive manufacturing and conventional method. *Fatigue Fract Eng Mater Struct* ffe.13565.
<https://doi.org/10.1111/FFE.13565>
- Golewski, G.L., 2022. Comparative measurements of fracture toughness combined with visual analysis of cracks propagation using the DIC
technique of concretes based on cement matrix with a highly diversified composition. *Theoretical and Applied Fracture Mechanics* 121,
103553. <https://doi.org/10.1016/J.TAFMEC.2022.103553>

- 565 Gosch, A., Berer, M., Hutař, P., Slávik, O., Vojtek, T., Arbeiter, F.J., Pinter, G., 2020. Mixed Mode I/III fatigue fracture characterization of
566 Polyoxymethylene. *Int J Fatigue* 130, 105269. <https://doi.org/10.1016/J.IJFATIGUE.2019.105269>
- 567 Gryguć, A., Behraves, S.B., Shaha, S.K., Jahed, H., Wells, M., Williams, B., Su, X., 2018. Low-cycle fatigue characterization and texture induced
568 ratcheting behaviour of forged AZ80 Mg alloys. *Int J Fatigue* 116, 429–438. <https://doi.org/10.1016/J.IJFATIGUE.2018.06.028>
- 569 Gryguć, A., Behraves, S.B., Shaha, S.K., Jahed, H., Wells, M., Williams, B., Su, X., 2019. Multiaxial cyclic behaviour of extruded and forged
570 AZ80 Mg alloy. *Int J Fatigue* 127, 324–337. <https://doi.org/10.1016/J.IJFATIGUE.2019.06.015>
- 571 Gryguć, A., Behraves, S.B., Jahed, H., Wells, M., Williams, B., Su, X., 2020. Multiaxial Fatigue and Cracking Orientation of Forged AZ80
572 Magnesium Alloy. *Procedia Structural Integrity* 25, 486–495. <https://doi.org/10.1016/J.PROSTR.2020.04.055>
- 573 Jamali, J., Mahmoodi, M.J., Hassanzadeh-Aghdam, M.K., Wood, J.T., 2019. A mechanistic criterion for the mixed-mode fracture of unidirectional
574 polymer matrix composites. *Compos B Eng* 176, 107316. <https://doi.org/10.1016/J.COMPOSITESB.2019.107316>
- 575 Jamali, J., Mourad, A.-H.I., Fan, Y., Wood, J.T., 2016. Through-thickness fracture behavior of unidirectional glass fibers/epoxy composites under
576 various in-plane loading using the CTS test. *Eng Fract Mech* 156, 83–95. <https://doi.org/10.1016/J.ENGFRACMECH.2016.01.016>
- 577 Karen Alavi, S., Ayatollahi, M.R., Jamali, J., Petru, M., 2022. On the applicability of digital image correlation method in extracting the higher
578 order terms in stress field around blunt notches. *Theoretical and Applied Fracture Mechanics* 121, 103436.
579 <https://doi.org/10.1016/J.TAFMEC.2022.103436>
- 580 Kobayashi, T., Shockey, D.A., 2010. Fracture surface topography analysis (FRASTA)—Development, accomplishments, and future applications.
581 *Eng Fract Mech* 77, 2370–2384. <https://doi.org/10.1016/J.ENGFRACMECH.2010.05.016>
- 582 Kondo, T., Miki, D., Hirakata, H., Minoshima, K., 2019. Effects of surface oxide layer on fracture toughness of submicrometer-thick freestanding
583 copper films. *Eng Fract Mech* 220, 106652. <https://doi.org/10.1016/J.ENGFRACMECH.2019.106652>
- 584 Krolczyk, G.M., Maruda, R.W., Krolczyk, J.B., Nieslony, P., Wojciechowski, S., Legutko, S., 2018. Parametric and nonparametric description of
585 the surface topography in the dry and MQCL cutting conditions. *Measurement (Lond)* 121, 225–239.
586 <https://doi.org/10.1016/j.measurement.2018.02.052>
- 587 Lauschmann, H., Tesář, K., Jiroušková, K., 2019. Quantitative fractography of fatigue cracks: a new solution in 3D. *Procedia Structural Integrity*
588 23, 107–112. <https://doi.org/10.1016/J.PROSTR.2020.01.071>
- 589 Lee, H.W., Basaran, C., 2022. Predicting high cycle fatigue life with unified mechanics theory. *Mechanics of Materials* 164, 104116.
590 <https://doi.org/10.1016/J.MECHMAT.2021.104116>
- 591 Le, V.-D., Pessard, E., Morel, F., Edy, F., 2019. Interpretation of the fatigue anisotropy of additively manufactured TA6V alloys via a fracture
592 mechanics approach. *Eng Fract Mech* 214, 410–426. <https://doi.org/10.1016/J.ENGFRACMECH.2019.03.048>
- 593 Li, J., Wang, X., Qi, W., Tian, J., Gong, S., 2019. Laser nanocomposites-reinforcing/manufacturing of SLM 18Ni300 alloy under aging treatment.
594 *Mater Charact* 153, 69–78. <https://doi.org/10.1016/J.MATCHAR.2019.04.038>
- 595 Macek, W., 2021a. Fracture Areas Quantitative Investigating of Bending-Torsion Fatigued Low-Alloy High-Strength Steel. *Metals* 2021, Vol. 11,
596 Page 1620 11, 1620. <https://doi.org/10.3390/MET11101620>
- 597 Macek, W., 2021b. Fracture surface formation of notched 2017A-T4 aluminium alloy under bending fatigue. *International Journal of Fracture*
598 2021 1–17. <https://doi.org/10.1007/S10704-021-00579-Y>
- 599 Macek, Wojciech, Branco, R., Costa, J.D., Pereira, C., 2021a. Strain sequence effect on fatigue life and fracture surface topography of 7075-T651
600 aluminium alloy. *Mechanics of Materials* 160, 103972. <https://doi.org/10.1016/j.mechmat.2021.103972>
- Macek, Wojciech, Branco, R., Costa, J.D., Trembacz, J., 2021b. Fracture Surface Behavior of 34CrNiMo6 High-Strength Steel Bars with Blind
Holes under Bending-Torsion Fatigue. *Materials* 2022, Vol. 15, Page 80 15, 80. <https://doi.org/10.3390/MA15010080>
- Macek, Wojciech, Branco, R., Korpyś, M., Łagoda, T., 2021c. Fractal dimension for bending–torsion fatigue fracture characterisation.
Measurement 184, 109910. <https://doi.org/10.1016/J.MEASUREMENT.2021.109910>
- Macek, W., Branco, R., Trembacz, J., Costa, J.D., Ferreira, J.A.M., Capela, C., 2020. Effect of multiaxial bending-torsion loading on fracture
surface parameters in high-strength steels processed by conventional and additive manufacturing. *Eng Fail Anal* 118.
<https://doi.org/10.1016/j.engfailanal.2020.104784>

- 608 Macek, W., 2021c. Correlation between Fractal Dimension and Areal Surface Parameters for Fracture Analysis after Bending-Torsion Fatigue.
609 Metals 2021, Vol. 11, Page 1790 11, 1790. <https://doi.org/10.3390/MET11111790>
- 610 Macek, W., Marciniak, Z., Branco, R., Rozumek, D., Królczyk, G.M., 2021. A fractographic study exploring the fracture surface topography of
611 S355J2 steel after pseudo-random bending-torsion fatigue tests. Measurement 178, 109443.
612 <https://doi.org/10.1016/j.measurement.2021.109443>
- 613 Malekipour, K., Mashayekhi, M., Badrossamay, M., 2021. Meso-scale damage mechanics modeling for high cycle fatigue behavior of additively
614 manufactured components. Mechanics of Materials 160, 103951. <https://doi.org/10.1016/J.MECHMAT.2021.103951>
- 615 Masoudi Nejad, R., Sina, N., Ghahremani Moghadam, D., Branco, R., Macek, W., Berto, F., 2022. Artificial neural network based fatigue life
616 assessment of friction stir welding AA2024-T351 aluminum alloy and multi-objective optimization of welding parameters. Int J Fatigue
617 160, 106840. <https://doi.org/10.1016/J.IJFATIGUE.2022.106840>
- 618 Meischel, M., Stanzl-Tschegg, S.E., Arcari, A., Iyyer, N., Phan, N., 2016. Influence of Corrosive NaCl solution on Life times of 7075 Aluminum
619 alloy under Combined Fatigue loading in the VHCF Regime. Procedia Structural Integrity 2, 1077–1084.
620 <https://doi.org/10.1016/J.PROSTR.2016.06.138>
- 621 Merson, E., Danilov, V., Merson, D., Vinogradov, A., 2017. Confocal laser scanning microscopy: The technique for quantitative fractographic
622 analysis. Eng Fract Mech. <https://doi.org/10.1016/j.engfracmech.2017.04.026>
- 623 Molent, L., Spagnoli, A., Carpinteri, A., Jones, R., 2017. Using the lead crack concept and fractal geometry for fatigue lifing of metallic structural
624 components. Int J Fatigue 102, 214–220. <https://doi.org/10.1016/J.IJFATIGUE.2017.04.001>
- 625 Newton, L., Senin, N., Gomez, C., Danzl, R., Helml, F., Blunt, L., Leach, R., 2019. Areal topography measurement of metal additive surfaces
626 using focus variation microscopy. Addit Manuf 25, 365–389. <https://doi.org/10.1016/J.ADDMA.2018.11.013>
- 627 Pejkowski, L., Skibicki, D., 2019. Stress-strain response and fatigue life of four metallic materials under asynchronous loadings: Experimental
628 observations. Int J Fatigue 128, 105202. <https://doi.org/10.1016/J.IJFATIGUE.2019.105202>
- 629 Pelegatti, M., Lanzutti, A., Salvati, E., Novak, J.S., de Bona, F., Benasciutti, D., 2021. Cyclic plasticity and low cycle fatigue of an aisi 316l
630 stainless steel: Experimental evaluation of material parameters for durability design. Materials 14. <https://doi.org/10.3390/MA14133588>
- 631 Podulka, Przemysław, 2021. The Effect of Surface Topography Feature Size Density and Distribution on the Results of a Data Processing and
632 Parameters Calculation with a Comparison of Regular Methods. Materials 2021, Vol. 14, Page 4077 14, 4077.
633 <https://doi.org/10.3390/MA14154077>
- 634 Podulka, P., 2021. Reduction of the end-effect in surface texture analysis. J Phys Conf Ser 1736, 012013. <https://doi.org/10.1088/1742-6596/1736/1/012013>
- 635
- 636 Rozumek, D., Lewandowski, J., Lesiuk, G., Marciniak, Z., Correia, J.A., Macek, W., 2022. The energy approach to fatigue crack growth of S355
637 steel welded specimens subjected to bending. Theoretical and Applied Fracture Mechanics 121, 103470.
638 <https://doi.org/10.1016/J.TAFMEC.2022.103470>
- 639 Rozumek, D., Marciniak, Z., Lesiuk, G., Correia, J.A., de Jesus, A.M.P., 2018. Experimental and numerical investigation of mixed mode I + II
640 and I + III fatigue crack growth in S355J0 steel. Int J Fatigue 113, 160–170. <https://doi.org/10.1016/J.IJFATIGUE.2018.04.005>
- 641 Sampath, D., Akid, R., Morana, R., 2018. Estimation of crack initiation stress and local fracture toughness of Ni-alloys 945X (UNS N09946) and
642 718 (UNS N07718) under hydrogen environment via fracture surface topography analysis. Eng Fract Mech 191, 324–343.
643 <https://doi.org/10.1016/j.engfracmech.2017.12.010>
- Santos, L.M.S., Ferreira, J.A.M., Jesus, J.S., Costa, J.M., Capela, C., 2016. Fatigue behaviour of selective laser melting steel components.
Theoretical and Applied Fracture Mechanics 85, 9–15. <https://doi.org/10.1016/j.tafmec.2016.08.011>
- Santus, C., Romanelli, L., Grossi, T., Neri, P., Romoli, L., Lutey, A.H.A., Pedranz, M., Benedetti, M., 2022. Torsional-loaded notched specimen
fatigue strength prediction based on mode I and mode III critical distances and fracture surface investigations with a 3D optical profilometer.
Int J Fatigue 161, 106913. <https://doi.org/10.1016/J.IJFATIGUE.2022.106913>
- Senin, N., Thompson, A., Leach, R.K., 2017. Characterisation of the topography of metal additive surface features with different measurement
technologies. Meas Sci Technol. <https://doi.org/10.1088/1361-6501/aa7ce2>

- 651 Stamoulis, G., Carrere, N., 2020. Linear elastic analysis of the loading rate dependency of the fracture properties of structural adhesives in the
652 mixed mode I+II plane. *Eng Fract Mech* 106840. <https://doi.org/10.1016/J.ENGFRACMECH.2019.106840>
- 653 Stanzl-Tschegg, S.E., 2017. Influence of material properties and testing frequency on VHCF and HCF lives of polycrystalline copper. *Int J Fatigue*
654 105, 86–96. <https://doi.org/10.1016/J.IJFATIGUE.2017.08.014>
- 655 Strzelecki, P., Wachowski, M., 2022. Effect of the stress concentration factor on the final fracture zone of aluminium AW 6063 T6 for rotating
656 bending specimens. *Mater Today Commun* 31, 103766. <https://doi.org/10.1016/J.MTCOMM.2022.103766>
- 657 Todhunter, L.D., Leach, R.K., Lawes, S.D.A., Blateyron, F., 2017a. Industrial survey of ISO surface texture parameters. *CIRP J Manuf Sci Technol*
658 19, 84–92. <https://doi.org/10.1016/J.CIRPJ.2017.06.001>
- 659 Todhunter, L.D., Leach, R.K., Lawes, S.D.A., Blateyron, F., 2017b. Industrial survey of ISO surface texture parameters. *CIRP J Manuf Sci Technol*
660 19, 84–92. <https://doi.org/10.1016/J.CIRPJ.2017.06.001>
- 661 Tomczyk, A., Seweryn, A., 2017. Fatigue life of EN AW-2024 alloy accounting for creep pre-deformation at elevated temperature. *Int J Fatigue*
662 103, 488–507. <https://doi.org/10.1016/j.ijfatigue.2017.06.037>
- 663 Tomków, J., Janeczek, A., Rogalski, G., Wolski, A., 2020. Underwater Local Cavity Welding of S460N Steel. *Materials* 2020, Vol. 13, Page 5535
664 13, 5535. <https://doi.org/10.3390/MA13235535>
- 665 Wojtek, T., Pokluda, J., Hohenwarter, A., Pippan, R., 2013. Three-dimensional morphology of fracture surfaces generated by modes II and III
666 fatigue loading in ferrite and austenite. *Eng Fract Mech* 108, 285–293. <https://doi.org/10.1016/J.ENGFRACMECH.2013.02.022>
- 667 Walczak, M., Szala, M., 2021. Effect of shot peening on the surface properties, corrosion and wear performance of 17-4PH steel produced by
668 DMLS additive manufacturing. *Archives of Civil and Mechanical Engineering* 21, 1–20. [https://doi.org/10.1007/S43452-021-00306-](https://doi.org/10.1007/S43452-021-00306-3/FIGURES/13)
669 [3/FIGURES/13](https://doi.org/10.1007/S43452-021-00306-3/FIGURES/13)
- 670 Wang, Z., Wu, W., Qian, G., Sun, L., Li, X., Correia, J.A.F.O., 2019. In-situ SEM investigation on fatigue behaviors of additive manufactured Al-
671 Si10-Mg alloy at elevated temperature. *Eng Fract Mech* 214, 149–163. <https://doi.org/10.1016/J.ENGFRACMECH.2019.03.040>
- 672 Westermann, I., Pedersen, K.O., Børvik, T., Hopperstad, O.S., 2016. Work-hardening and ductility of artificially aged AA6060 aluminium alloy.
673 *Mechanics of Materials* 97, 100–117. <https://doi.org/10.1016/J.MECHMAT.2016.02.017>
- 674 Wietecha-Reiman, I.J., Segall, A., Zhao, X., Palmer, T.A., 2022. Combining Fractal and Topological Analyses to Quantify Fracture Surfaces in
675 Additively Manufactured Ti-6Al-4V. *Int J Fatigue* 107232. <https://doi.org/10.1016/J.IJFATIGUE.2022.107232>
- 676 Yao, M., Wang, H., Zhao, Y., Sha, J., 2018. Tension-tension fatigue behaviours of notched freestanding pure Ti foils with different thicknesses.
677 *Int J Fatigue* 114, 65–73. <https://doi.org/10.1016/J.IJFATIGUE.2018.05.009>
- 678 Zhang, N., Guo, S., He, G., Jiang, B., Zhou, L., Chen, Y., Liu, Y., 2022. Failure analysis of the carburized 20MnCr5 gear in fatigue working
679 condition. *Int J Fatigue* 161, 106938. <https://doi.org/10.1016/J.IJFATIGUE.2022.106938>