

# Equivalent temperature for design of asphalt pavements in Poland

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**Abstract.** The paper presents application of equivalent temperature for design of asphalt pavements. The calculation methods of equivalent temperature: the Shell method, the French method, the methods that use the AASHTO and the Asphalt Institute fatigue criteria were presented. The results of calculations of equivalent temperature for Polish climatic conditions were presented and discussed. It was shown that different asphalt pavement design methods and utilization of Polish climatic data resulted in various calculated values of equivalent temperature that could be used in the design process.

## 1 Introduction

One of the most important factor that influences the behaviour of the road pavements is temperature. In the case of asphalt pavements temperature affects the mechanical characteristics of the pavement [1-3]. Cyclical variations of temperature cause shrinkage cracks in materials treated with hydraulic binders. Also, thermal gradients cause strains in the concrete slabs in rigid pavements. In the practice of asphalt pavements design process, in most cases calculations are carried out with consideration of an equivalent constant temperature. The behaviour of asphalt layers in terms of deformation and fatigue depends on temperature, stress levels and damage level of the asphalt pavement. According to French practice [4] structural design is carried out for the constant temperature, referred to as the equivalent temperature  $\theta_{eq}$ . The equivalent temperature is defined in case when the cumulative damage in the asphalt pavement over a year, for a given temperature distribution, is equal to the damage that the pavement would undergo with the same traffic but for the constant temperature  $\theta_{eq}$ . The equivalent temperature is determined by applying Miner's law [5]. According to the Shell procedure [6, 7] the equivalent temperature can be also called as „effective temperature“. The effective stress generated in the pavement structure characterized by a single temperature model corresponds to the stresses calculated on the basis of models set up in accordance with various temperature values. Calculation can be performed according to the equation (1):

$$N_{eff} = \frac{1}{\frac{1}{n} \sum_{i=1}^n \left( \frac{1}{N_i} \right)} \quad (1)$$

where:

$N_{eff}$  - effective cycle number (the effective design life) in effective single temperature applied for the design pavement according to Miner's hypothesis,

$N_i$  - actual allowed cycle number calculated on the basis of various temperatures,  
 $n$  - number of temperature gradients.

The objective of the paper is to determine the equivalent temperature values on the basis of meteorological data for selected locations in Poland with the use of mechanistic-empirical methods. The temperature data were collected and analysed for the following 32 years period of time: from the beginning of 1985 to the end of 2016. The location of meteorological stations was chosen to represent all the Polish territory.

## 2 Methods

### 2.1 The Shell method

Analysis of equivalent temperature for design of asphalt pavement according to the Shell procedure [6] consisted following steps:

1. Determination of the mean monthly air temperature (MMAT) for each month during entire period: from January 1985 to December 2016.
2. For each MMAT value the „Weighting Factor“ was derived from Figure 1.

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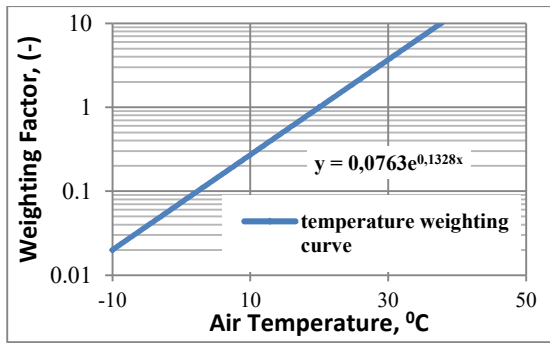


Fig. 1. Temperature weighting curve, according to Shell method [6]

3. Calculation of the annual average weighting factor for each analysed location.
4. Determination of the equivalent temperature values (effective Mean Annual Air Temperature MAAT) on the basis of annual average weighting factor for pavement structure: a) 8 cm asphalt layers and 20 crushed aggregate base course (KR2); b) 20 cm asphalt layers and 20 crushed aggregate base course (KR4); c) 24 cm asphalt layers and 20 crushed aggregate base course (KR6).

## 2.2 The French method

With application of the French method [4] the calculations of equivalent temperature were conducted according to the following equation (2):

$$\sum_i \frac{n_i(\theta_i)}{N_i(\theta_i)} = \frac{\sum_i n_i(\theta_i)}{N(\theta_{eq})} \quad (2)$$

where:

- $\theta_i$  - pavement temperature distribution during a year,
- $N_i(\theta_i)$  - number of loadings causing failure due to fatigue for the level of strain  $\epsilon(\theta_i)$ ,
- $\epsilon(\theta_i)$  - tensile strain in the pavement under the standard axle,
- $n_i(\theta_i)$  - number of temperature  $\theta_i$  gradients,
- $\theta_{eq}$  - equivalent temperature, [°C].

After calculating the elementary damage  $1/N(\theta_{eq})$ , equivalent temperature  $\theta_{eq}$  was obtained from the curve giving the variation in damage according to temperature distribution  $\theta_i$ . The calculation of the equivalent temperature according to the French method was performed using the following procedure:

1. Determination of the mean monthly air temperature (MMAT) distribution and mean monthly pavement temperature (MMPT) in 5°C intervals. Determination of the stiffness modulus of asphalt base course for each temperature interval.
2. Calculation of horizontal strain at the bottom of asphalt layers at a certain temperature (at certain stiffness modulus of asphalt mixture).
3. Assumption was made according to the literature [8] that the value of strain  $\epsilon_6$  in millionth load cycle (assumed for temperature up to +10°C)  $\epsilon_6 = 115 \times 10^{-6}$ . Other  $\epsilon_6$  strain values for other temperatures were estimated due to the

lack of laboratory results. In addition the laboratory fatigue test method and shape of samples that are typically used in France are different from those used in Poland.

4. Calculation of the weighted average fatigue damage based on pavement temperature distribution and fatigue damage in each temperature interval.

5. Determination of the equivalent temperature based on the calculated average fatigue damage according to a particular function of the temperature and fatigue damage.

## 2.3 Method with use of Asphalt Institute and AASHTO 2004 fatigue criteria

Determination of the equivalent temperature with use of Asphalt Institute [8, 10] and AASHTO 2004 [12] fatigue criteria included the following steps:

1. Determination of mean monthly air temperatures (MMAT) based on the temperature data from meteorological stations.
2. Calculation of the mean monthly pavement temperature according to the equation (3) developed originally by Witczak [10]:

$$MMPT = MMAT \cdot \left[ 1 + \frac{1}{z+4} \right] - \frac{34}{z+4} + 6 \quad (3)$$

where:

- MMPT - mean monthly pavement temperature, (°Fahrenheit),
- MMAT - mean monthly air temperature, (°Fahrenheit),
- z - depth below the pavement surface, (inch).

3. Calculation of fatigue life with the use of the fatigue cracks criteria of the analysed asphalt pavement. The calculations were conducted for the temperature range from -20°C to +30°C with 5°C intervals. Stiffness moduli of asphalt mixtures were determined using the software program Shell-BANDS. To simplify the calculation procedure the wheel load was assumed to 50 kN as the value typically applied during road pavements design process. Frequency of traffic was assumed as uniform flow during entire year. Calculation of fatigue life during entire year was performed using the following equation (4):

$$N_{year} = \frac{100}{\left( \frac{\%traffic1}{N1} + \frac{\%traffic2}{N2} + \dots + \frac{\%traffic12}{N12} \right)} \quad (4)$$

where:

- $N_{year}$  - fatigue life of asphalt pavement during entire year,
  - % traffic1 - percentage of traffic in January (the 1st month),
  - % traffic2 - the same but in February (the 2nd month),
  - % traffic12 - the same but in December (the 12th month),
  - $N1, N2, \dots, N12$  - fatigue life calculated in each month.
4. On the basis of fatigue curve determined for each mean monthly temperature one annual equivalent temperature was assigned as a value in which fatigue life is equal to a value obtained from different temperatures.

## 3 Analysis of temperature data

Temperature data that were required for the calculation of equivalent temperature were obtained from

the Institute of Meteorology and Water Management (IMGW), Polish National Research Institute from period of time from January 1985 to December 2016. The first step of temperature data analysis concerned all the 65 meteorological stations located in Poland. For further analysis 10 meteorological stations were selected. The meteorological stations with gaps in measurement data and located at mountain peaks, for ex. Sniezka or Kasprowy Wierch were excluded from the analysis.. The location of meteorological stations located evenly on the Polish territory is presented in Figure 2.



Fig. 2. The location of meteorological stations, [11]

The results of mean value analysis of air temperature from January 1985 to December 2016 were shown in Table 1.

Table 1. The results of mean value analysis of air temperature from January 1985 to December 2016, [11]

Location	Mean values of air temperature from 1985 to 2016, °C											
	January	February	March	April	May	June	July	August	September	October	November	December
Bialystok	-3.3	-2.3	1.4	7.6	13.1	16.0	18.2	17.1	12.2	7.2	2.3	-1.5
Elblag	-1.7	-0.7	2.6	8.0	12.9	15.7	18.2	17.7	13.4	8.5	3.6	0.1
Katowice	-1.5	-0.2	3.4	9.0	13.8	16.7	18.8	18.1	13.5	8.8	3.9	-0.1
Krosno	-2.5	-1.3	2.8	8.7	13.5	16.4	18.4	18.0	13.3	8.7	3.7	-1.1
Poznan	-0.8	0.2	3.6	9.1	14.2	16.8	19.2	18.5	13.9	8.9	3.9	0.8
Szczecin	0.2	1.1	4.0	8.9	13.6	16.4	18.8	18.1	14.0	9.4	4.6	1.7
Swinoujscie	0.4	1.1	3.6	7.6	12.1	15.5	18.0	17.8	14.2	9.6	4.8	1.8
Warszawa	-1.6	-0.4	2.9	8.5	13.8	16.7	19.0	18.4	13.6	8.5	3.6	0.2
Wroclaw	-1.9	-0.8	2.9	8.9	14.3	17.1	19.4	18.6	13.6	8.4	3.4	-0.2
Zakopane	-0.5	0.6	4.1	9.3	14.2	17.1	19.3	18.7	14.2	9.3	4.3	1.0

As an example the change of monthly temperature in every month of the analysed period of time from 1985 to 2016 and for Bialystok meteorological station is presented in Figure 3.

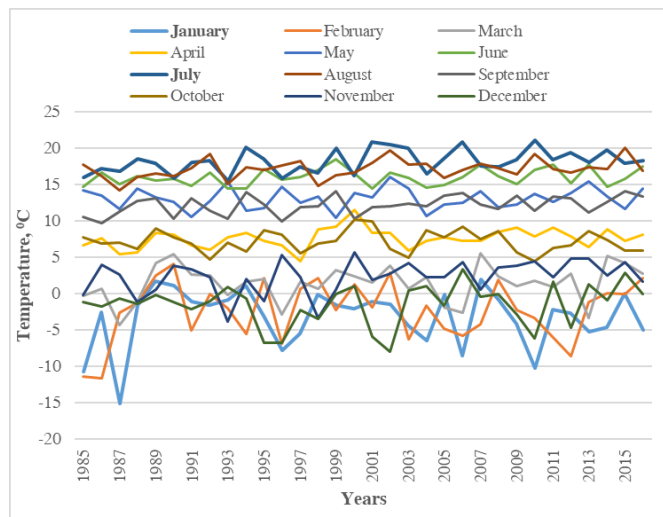


Fig. 3. An example the change of monthly temperature in every month of the analysed period of time from 1985 to 2016 and for Bialystok meteorological station

The results of air temperature measurements from meteorological station in Bialystok shown quite high variability between mean values of monthly temperatures during the past 32 years especially for winter months.

#### 4 Results and discussion

The results of equivalent temperature calculations according to Shell method in the depth of 2/3 of asphalt layers thickness were presented in Table 2.

Table 2. The results of calculation of equivalent temperature according to Shell method

Location	Equivalent temperature, °C		
	KR2 (z = 8 cm)	KR4 (z = 13 cm)	KR4 (z = 19 cm)
Bialystok	8.8	8.5	8.3
Elblag	9.3	10.0	8.7
Katowice	10.3	8.5	9.7
Krosno	10.1	9.7	9.5
Poznan	10.8	10.4	10.2
Szczecin	10.5	10.2	9.9
Swinoujscie	10.1	9.7	9.5
Torun	10.3	10.0	9.7
Warszawa	10.8	10.4	10.2
Wroclaw	10.3	10.0	9.7

The Shell method of calculations has shown that annual equivalent temperature that can be used for asphalt pavement design process is equal to 10°C (rounded to 1,0°C).

In the French method of equivalent temperature calculation, the annual mean distribution of pavement temperature in the depth of 2/3h of asphalt layers is given in Table 3.

**Table 3.** Annual mean distribution of pavement temperature according to the French method

Temperature, °C	-20	-15	-10	-5	0	5	10	15	20	25	30
Duration in year, %	0.3	0.7	2.4	6.0	14.7	17.1	15.2	17.4	17.0	8.2	1.0

The stiffness moduli of asphalt base course  $E(\theta_i)$  were calculated with the use of Shell-BISAR program. It was assumed that bitumen content in asphalt mixture  $V_a$  is 9,5% v/v and voids content  $V_v$  is 7% v/v. To simplify the calculation procedure the wheel load was assumed 50 kN as the value typically use during road pavements design.

The elementary damage was calculated according to French fatigue law from the equation (5):

$$d(\theta_i) = \left( \frac{\varepsilon_6(\theta_i)}{\varepsilon(\theta_i)} \right)^{\frac{1}{b}} \cdot 10^{-6} \quad (5)$$

where:

- $d(\theta_i)$  – elementary damage at the temperature  $\theta$ ,
- $\varepsilon_6(\theta_i)$  – strain after  $10^6$  cycles,
- $\varepsilon(\theta_i)$  – tensile strain at the bottom of asphalt layers,
- $b$  – slope of fatigue curve ( $b = -0,2$ )

The results of calculation of elementary damage were presented in Table 4.

**Table 4.** Results of calculation of elementary damage according to French method

Temperature	Duration in year	Stiffness modulus of asphalt base course	Tensile strain at the bottom of asphalt layers	Strain after $10^6$ cycles	Elementary damage
$\theta_i$ [°C]	$\frac{n_i(\theta_i)}{\sum n_i(\theta_i)}$ [%]	$E(\theta_i)$ [MPa]	$\varepsilon(\theta_i)$ [ $\mu$ strain]	$\varepsilon_6(\theta_i)$ [ $\mu$ strain]	$d(\theta_i)$ [-]
-20	0.3%	31000	20	71	0.00161
-15	0.7%	29000	21	73	0.00181
-10	2.4%	26400	22	77	0.00213
-5	6.0%	22600	26	83	0.00279
0	14.7%	18600	30	91	0.00389
5	17.1%	14800	36	102	0.00568
10	15.2%	11700	44	115	0.00829
15	17.4%	9310	53	129	0.01185
20	17.0%	6540	70	154	0.02001
25	8.2%	4330	97	189	0.03510
30	1.0%	2710	137	239	0.06128

The elementary damage for equivalent temperature  $1/N(\theta_{eq})$  was calculated from the equation (6):

$$\frac{1}{N(\theta_{eq})} = \sum_i \frac{n_i(\theta_i)}{\sum_i n_i(\theta_i)} d(\theta_i) \quad (6)$$

where:

- $1/N(\theta_{eq})$  – elementary damage for equivalent temperature,
- $n_i(\theta_i)$  – number of temperature  $\theta_i$  gradients,

$d(\theta_i)$  – elementary damage in temperature  $\theta_i$ .

The value of equivalent temperature for Polish temperature conditions according to calculations made with use of the French procedure is equal to 15°C.

The results of calculation of asphalt mixture stiffness moduli according to method with use of the Asphalt Institute (IA) and AASHTO 2004 fatigue laws were presented in Table 5.

**Table 5.** The results of calculation of asphalt mixture stiffness moduli according to method with use of the IA and AASHTO 2004 fatigue laws

Temperature, °C	Stiffness modulus of bitumen, MPa		Stiffness modulus of asphalt mixture, MPa		
	35/50	50/70	Wearing course AC11S 50/70	Binder course AC16W 35/50	Base course AC22P 35/50
-20	1550	1480	27500	27700	29600
-15	1250	1160	25200	25700	27600
-10	953	858	22000	23200	25100
-5	679	605	18300	19400	21200
0	451	388	14400	15700	17300
+5	278	240	11200	12200	13700
+10	169	144	8500	9380	10700
+15	103	78.1	5840	7240	8390
+20	57.5	39.3	3530	4900	5800
+25	29.4	18.2	2010	3120	3780
+30	13.7	8.22	1120	1860	2320

The equivalent temperature calculations were conducted according to method with use of the Asphalt Institute fatigue criterion, from the equation (7):

$$N_{bit} = 18,4 \cdot 6,167 \cdot 10^{-5} \cdot (10)^{4,84 \cdot \left( \frac{V_a}{V_a + V_v} - 0,69 \right)} \cdot S_m^{-0,854} \cdot \varepsilon_{bit}^{-3,291} \quad (7)$$

where:

- $V_a$  – bitumen content, [%, v/v]
- $V_v$  – voids content, [%, v/v]
- $S_m$  – stiffness modulus of asphalt mixture, [MPa]
- $\varepsilon_{bit}$  – strain at the bottom of asphalt layers, [ $\mu$ strain  $\times 10^{-6}$ ]

In the next step of analysis the AASHTO 2004 fatigue criterion [12] was applied. It was assumed that the level of crack failure FC is equal to 15% and calculations were conducted according to equations (8-11):

$$N_{bit} = 7,3557 \cdot 10^{-6} \cdot C \cdot k'_1 \cdot \left( \frac{1}{\varepsilon_{asf}} \right)^{3,9492} \cdot \left( \frac{1}{S_m} \right)^{1,281} \quad (8)$$

where:

$$C = 10^M \quad (9)$$

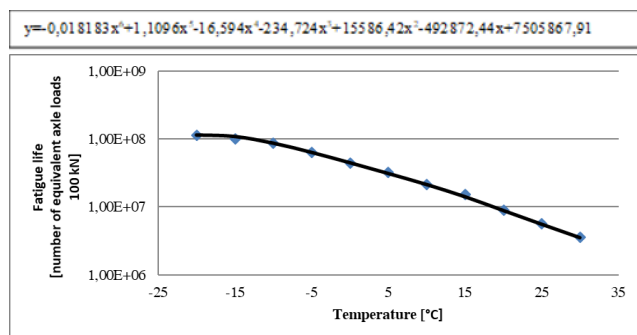
$$M = 4,84 \cdot \left( \frac{V_a}{V_a + V_v} - 0,69 \right) \quad (10)$$

$$k'_1 = \frac{1}{0,000398 + \frac{0,003602}{1 + e^{11,02 - 1,374 \cdot h}}} \quad (11)$$

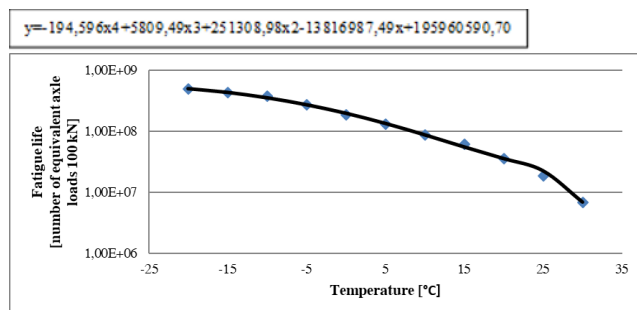
where:

- $V_a$  – bitumen content, [%, v/v]
- $V_v$  – voids content, [%, v/v]
- $S_m$  – stiffness modulus of asphalt mixture, [MPa]
- $\varepsilon_{bit}$  – strain at the bottom of asphalt layers, [ $\mu$ strain  $\times 10^{-6}$ ]

For the base course layer made of unbound crushed aggregate it was assumed that the value of modulus of elasticity is 400 MPa and the Poisson ratio is equal to 0,3. The resulting fatigue curve for traffic levels: KR2, KR4 and KR6 with use of the Asphalt Institute criterion was presented in Figure 5 and respectively with use of the AASHTO 2004 criterion was presented in Figure 6.



**Fig. 5.** The resulting fatigue curve from the calculations with use of Asphalt Institute criterion



**Fig. 6.** The resulting fatigue curve from the calculations with use of AASHTO 2004 criterion

The annual equivalent temperature values calculated with the use of the Asphalt Institute fatigue criterion for different locations of meteorological station were presented in Table 6.

**Table 6.** The annual equivalent temperature values calculated with the use of the Asphalt Institute fatigue criterion for different locations of meteorological station

Location	Equivalent temperature [°C]		
	KR2	KR4	KR6
Bialystok	16.9	15.4	15.7
Elblag	17.2	16.0	16.2
Katowice	17.9	16.6	16.8
Krosno	17.6	16.3	16.5
Poznan	18.2	16.9	17.1
Szczecin	18.0	16.8	17.0
Swinoujscie	17.4	16.2	16.4
Torun	17.9	16.6	16.8
Warszawa	18.2	16.8	17.0
Wroclaw	18.3	17.2	17.6

The method of calculations with use of the Asphalt Institute fatigue criterion has shown that annual equivalent temperature that can be used for asphalt pavement design process is equal to 17°C (rounded to 1,0°C).

The annual equivalent temperature values calculated with the use of the AASHTO 2004 fatigue criterion for different locations of meteorological station were presented in Table 7.

**Table 7.** The annual equivalent temperature values calculated with the use of the AASHTO 2004 fatigue criterion for different locations of meteorological station

Location	Equivalent temperature [°C]		
	KR2	KR4	KR6
Bialystok	16.1	16.1	14.4
Elblag	16.5	16.5	14.9
Katowice	17.1	17.2	15.5
Krosno	16.8	16.9	15.2
Poznan	17.4	17.6	15.9
Szczecin	17.2	17.3	15.7
Swinoujscie	16.6	16.7	15.2
Torun	17.1	17.3	15.5
Warszawa	17.4	17.6	15.7
Wroclaw	17.6	17.9	16.1

The method of calculations with use of the AASHTO 2004 fatigue criterion has shown that annual equivalent temperature that can be used for asphalt pavement design process is equal to 16°C (rounded to 1,0°C).

## 5 Conclusions

Based on the results of calculations and analysis conducted, the following conclusions can be drawn:

1. The results of air temperature measurements from meteorological stations shown quite high variability between mean values of monthly temperatures during the past 32 years especially for winter months.
2. The equivalent temperature is very important issue in design process of asphalt pavements using mechanistic-empirical methods. It was shown that obtained values can vary between 10°C for Shell method through 15°C for the French method, the 16°C for method that use of the AASHTO 2004 fatigue criterion and finally the 17°C for method that use of the Asphalt Institute fatigue criterion.
3. It was found that the value of equivalent temperature mostly depends on the method of calculation and the collected air temperature data. It is very important to collect temperature data from meteorological stations located close to the area of designed pavement.



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