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# On Accelerated Metaheuristic-Based Electromagnetic-Driven Design Optimization of Antenna Structures Using Response Features

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Abstract: Development of present-day antenna systems is an intricate and multi-step process requiring, among others, meticulous tuning of designable (mainly geometry) parameters. Concerning the latter, the most reliable approach is rigorous numerical optimization, which tends to be resourceintensive in terms of computing due to involving full-wave electromagnetic (EM) simulations. The cost-related issues are particularly pronounced whenever global optimization is necessary, typically carried out using nature-inspired algorithms. Although capable of escaping from local optima, population-based algorithms exhibit poor computational efficiency, to the extent of being hardly feasible when directly handling EM simulation models. A popular mitigation approach involves surrogate modeling techniques, facilitating the search process by replacing costly EM analyses with a fast metamodel. Yet, surrogate-assisted procedures feature complex implementations, and their range of applicability is limited in terms of design space dimensionality that can be efficiently handled. Rendering reliable surrogates is additionally encumbered by highly nonlinear antenna characteristics. This paper investigates potential benefits of employing problem-relevant knowledge in the form of response features into nature-inspired antenna optimization. As demonstrated in the recent literature, re-formulating the design task with the use of appropriately selected characteristic locations of the antenna responses permits flattening the functional landscape of the objective function, leading to faster convergence of optimization procedures. Here, we apply this concept to nature-inspired global optimization of multi-band antenna structures, and demonstrate its relevance, both in terms of accelerating the search process but also improving its reliability. The advantages of feature-based nature-inspired optimization are corroborated through comprehensive (based on three antenna structures) comparisons with a population-based search involving conventional (e.g., minimax) design problem formulation.

**Keywords:** antenna design; EM-driven optimization; global optimization; nature-inspired optimization; response features

## 1. Introduction

Modern antenna systems have to satisfy stringent performance specifications and multi-functionality demands [1], implied by the requirements stemming from newly-developed areas such as the Internet of Things (IoT) [2], wireless communications [3] including 5G [4,5], body area networks [6], microwave imaging [7], satellite communications [8], radar [9], or remote sensing [10]. Specific functionalities required for these and other applications include broadband [11] and multi-band functioning [12], multiple-input–multiple-output (MIMO) operation [13], circular polarization [14], beam scanning [15], reconfigurability [16,17], high directivity [18], polarization/pattern diversity [19], etc. Apart from boosting electrical and field parameters, miniaturization demands also become commonplace, being especially important for mobile communications [20], implantable/wearable



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> devices [21], and IoT [22]. This leads to additional design challenges, as reduction of antenna size is detrimental to electrical performance [23,24]. The latter enforces seeking trade-off solutions that satisfy constraints imposed on physical dimensions while ensuring sufficient functionality. Design of high-performance and multi-functional antennas is associated with the development of structures containing defected ground structures [25], stubs [26], slots [27], shorting pins [28], substrate-integrated waveguide (SIW) [29], or metamaterial components [30,31], often implemented as multi-layer geometries [32,33]. Accurate characterization of topologically complex devices requires full-wave electromagnetic (EM) analysis, which has been commonly involved at virtually all design stages, such as topology evolution [34], parametric studies [35], and design closure [36,37].

> Given the antenna geometry, careful adjustment of geometry parameters is the single most important step towards improving electrical performance of the device. Traditionally, this has been commonly realized through parameter sweeping guided by engineering know-how; however, this approach is no longer adequate given the complexity of contemporary antennas, a typically large number of variables, as well as several objectives and constraints that have to be simultaneously handled. Instead, rigorous numerical optimization is preferred [38,39]. Although a large number of optimization techniques are available, a common issue is high computational cost of EM-driven design, which may prove problematic even when carrying out local search using gradient-based [40] or derivative-free methods [41]. On the other hand, the need for global optimization has been growing as well [42]. It is necessary for multimodal tasks (i.e., whenever the presence of multiple local optima is expected), such as synthesis of antenna array patterns [43], design of metamaterials (e.g., broadband frequency selective surfaces or coding metasurfaces [44]), re-design of antennas over wide ranges of operating frequencies (especially in the case of multi-band structures), but also whenever an initial design of a decent quality is not easily obtainable. The latter situation is especially pertinent to miniaturized structures [45], or antennas implementing additional functionalities [46,47]. Understandably, global optimization incurs significantly higher CPU expenses as compared to local search.

> Population-based nature-inspired algorithms are currently the most popular approaches to global optimization [48–50]. Although they have a relatively long history, dating back to late 1960s (evolutionary strategies [51]), their broader utilization started in 1980s with the development of genetic algorithms [52], followed by evolutionary methods [53], genetic programming [54], and ant systems [55]. Particle swarm optimizers (PSO) [56] and differential evolution (DE) [57] were the next significant milestones, especially in terms of continuous optimization. From the early 2000s, nature-inspired methods virtually dominated global searches, and new algorithms have been emerging ever since (e.g., harmony search [58], firefly algorithm [59], grey wolf optimization [60], invasive weed optimization [61], and others [62–64]). Despite this variety, the actual differences between the algorithms, especially the recent ones, are rather minor. Nature-inspired procedures process the sets (population [53], pack [60], swarm [56], etc.) of prospective solutions (individuals, agents, particles, etc.) to a problem at hand. The candidate solutions exchange information and generate new ones by means of exploratory [65] and exploitative operators [66], which allows for finding the most promising parameter space regions but also escaping from local optima. The latter arguably results in global search capability [67]. Also, the algorithms of this class are easy to deploy. Still, population-based operation results in inferior computational efficiency, as a typical merit function call required by a single algorithm run may be as high as many hundreds or even thousands. Clearly, such costs may be prohibitive from the perspective of EM-driven design.

> Poor computational efficiency hinders utilization of population-based methods for antenna design. In practice, their straightforward application is only possible when using low-cost representations (e.g., pattern optimization with analytical array factor models [68], dedicated solvers with evaluation times at the level of seconds), or parallelization, the latter requiring sufficient computational resources and licensing. An alternative is utilization of surrogate modeling techniques [69], more often than not data-driven (kriging [70],



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> Gaussian process regression [71], neural networks [72]), often combined with sequential sampling methods [73]. In the latter, an iterative refinement of the surrogate is carried out using EM-generated data amassed during the optimization process [74]. Within these methodologies, fast metamodels are employed instead of expensive EM simulations to make predictions about potentially better designs [75]. The incorporation of surrogate models constitutes at present the most popular approach to nature-inspired optimization of heavy-cost simulation models. Its limitation, especially when antenna design is considered, is the curse of dimensionality and nonlinearity of antenna characteristics, both impeding a rendition of reliable surrogates at reasonable costs. In practice, conventional modeling methods may handle structures featuring a few variables [76,77]. This difficulty can be somewhat alleviated by means of domain-confined surrogates [78], or utilization of variableresolution EM models [79]. Recently, new surrogate-assisted techniques allowing for global design optimization of antenna [80] and microwave structures [81] have been proposed, where the challenges stemming from the curse of dimensionality have been handled by the employment of a self-adaptive Gaussian process as the underlying surrogate model.

> This work investigates the possibility of mitigating the challenges of EM-driven natureinspired antenna optimization by making use of the problem-specific knowledge expressed as response features [82]. The response feature approach has been developed to speed up local optimization procedures by reformulating the original design task in terms of suitably defined specific locations (response features) of the antenna outputs (e.g., frequencies and levels of antenna resonances, or the frequencies associated with specific levels, e.g.,  $-10 \, dB$ , of antenna characteristics [83]). A close-to-linear nonlinear relationship between the feature point coordinates and antenna dimensions facilitates convergence of the optimization process [84], and—in some cases—enables quasi-global search capabilities even when employing local search routines [85]. Here, the response feature technology is incorporated into EM-driven nature-inspired optimization to improve the convergence and reliability of the optimization procedure when compared to the standard formulation, which is typically based on minimax-type objective functions [86]. Using PSO as a representative populationbased routine, extensive numerical experiments are conducted using three multi-band microstrip antennas to identify potential benefits of feature-based formulation versus the traditional one (here, minimax). The findings corroborate that problem reformulation facilitates identification of the optimum design. In particular, it leads to improving the average performance of the search process as well as repeatability of results. These benefits are obtained owing to the involvement of the problem-relevant knowledge present in the system responses. Finally, utilization of response features allows for decreasing the computational costs of the search process (by over thirty percent on average) to reach the same design quality as that obtained with standard formulation.

## 2. Simulation-Driven Design of Antenna Structures: Minimax and Feature-Based **Problem Formulations**

This section discusses simulation-driven antenna design optimization. We recall the conventional definition of the design task, which is typically expressed as a minimax problem. We also consider an alternative formulation involving response features, and present its potential benefits in the context of global search. Section 3 will present the numerical verification of these advantages. The focus of this work is multi-band antennas. These are representative examples of multi-modal problems, as the optimization process starting from antenna resonances allocated away from the assumed targets normally leads to the optimum being unreachable through local (e.g., gradient-based) optimization.

# 2.1. Simulation-Driven Antenna Optimization: Minimax Formulation

The popularity and significance of rigorous numerical optimization has been gradually increasing in the design of antenna systems. This is related to stringent performance specifications imposed on contemporary antennas, leading to topological complexity (in particular, implying a larger number of geometry parameters that necessitate tuning), as



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> well as several objectives and constraints that need to be handled. Traditional methods, largely based on supervised parameter sweeping, are still widely applied, but their relevance has been greatly diminished. In this work, multi-objective optimization [87] is not considered, so, when few objectives are present, they are being aggregated [88], or handled as constraints. Several specific examples will be considered later in this section (cf. Table 1).

**Table 1.** Typical antenna design scenarios.

Design Requirements	Objective Function (1) and Design Constraints	Objective Function (3) and Penalty Functions		
• Improve in-band matching within the frequency range $F^{\$}$	$U(x) = S(x) = max\{f \in F:  S_{11}(x,f) \}$	$U_P(x) = U(x)$		
<ul> <li>Maximize average in-band gain in the frequency range F \$</li> <li>Ensure that in-band matching does not exceed -10 dB in F \$</li> </ul>	$U(x) = \bar{G}(x) = \frac{1}{F} \int_{F} G(x, f) df$ Constraint: $ S_{11}(x, f)  \le -10 \text{ dB for } f \in F$	$U_P(\mathbf{x}) = \overline{G}(\mathbf{x}) + \beta_1 c_1(\mathbf{x})^2$ where $c_1(\mathbf{x}) = \left[\frac{max(S_{11}(\mathbf{x}) + 10.0)}{10}\right]^2$		
<ul> <li>Minimize in-band axial ratio in the frequency range <i>F</i></li> <li>Ensure that in-band matching does not exceed -10 dB in <i>F</i> \$</li> </ul>	$U(x) = A_R(x) = max\{f \in F: AR(x, f)\}$ Constraint: $ S_{11}(x, f)  \le -10 \text{ dB for } f \in F$	$U_P(x) = A_R(x) + \beta_1 c_1(x)^2$ where $c_1(x) = \left[\frac{max(S_{11}(x) + 10.0)}{10}\right]^2$		
<ul> <li>Reduce size of a circularly polarized antenna</li> <li>Ensure that in-band matching does not exceed -10 dB in the frequency range F \$</li> <li>Ensure that axial ratio does not exceed 3 dB in F \$</li> </ul>	U(x) = A(x) Constraints: $AR(x, f) \le 3$ dB for $f \in F$ and $ S_{11}(x, f)  \le -10$ dB for $f \in F$	$U_{P}(\mathbf{x}) = A(\mathbf{x}) + \beta_{1}c_{1}(\mathbf{x})^{2} + \beta_{2}c_{2}(\mathbf{x})^{2}$ where $c_{1}(\mathbf{x}) = \left[\frac{max(S_{11}(\mathbf{x}) + 10.0)}{10}\right]^{2}$ and $c_{2}(\mathbf{x}) = \left[\frac{max(AR(\mathbf{x}) - 3.0)}{3}\right]^{2}$		

<sup>\$</sup> In general, the frequency range of interest F may be defined as a continuous range of frequencies, i.e.,  $F \in (f_1, f_2)$  $f_2$ ), in the form of a discrete set of operating frequencies  $f_{0k}$ , k = 1, ..., N, or as a single operating frequency  $f_0$ , according to the designer's needs.

In the following, we will utilize  $x = [x_1 \dots x_n]^T$  to represent a vector of designable parameters of the device at hand (typically, antenna dimensions). The problem to be solved is formulated as a minimization task:

$$x^* = \underset{x}{argmin}U(x, f) \tag{1}$$

where  $x^*$  stands for (a possibly global) optimum design, and f represents frequency belonging to the frequency range of interest F. U is a scalar function used as a metric of the design quality, which should be formulated so that a better design x is associated with lower values of U(x). "Better design" is a subjective term representing the designers' understanding of the design quality. Given the nature of the majority of antenna design problems, quantification of design quality is typically expressed in a minimax form, e.g., to minimize the maximum of certain quantities (reflection coefficient, axial ratio) over specific frequency ranges of interest [89]. Rigorous formulations will be discussed later in this section.

The design task (1) is often subject to constraints, belonging to either inequality,  $g_k(x) \leq 0, k = 1, \ldots, n_g$ , or equality type,  $h_k(x) = 0, k = 1, \ldots, n_h$ . Apart from strictly geometrical conditions, the constraints are typically expensive to evaluate (require EM analysis), and their explicit handling is problematic. A workaround is a penalty function approach [90], where the constraints are incorporated into the objective function. The design task takes the form of:



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$$x^* = \underset{x}{\operatorname{argmin}} U_P(x) \tag{2}$$

where:

$$U_P(x) = U(x) + \sum_{k=1}^{n_g + n_h} \beta_k c_k(x)$$
 (3)

The penalty functions  $c_k(x)$  quantify constraint violations, whereas the contributions of individual constraints to  $U_P$  are controlled by the proportionality factors  $\beta_k$ . A few examples of commonly considered design objectives can be found in Table 1. The notation employed therein is the following: f—frequency,  $|S_{11}(x,f)|$ —reflection coefficient at design x and frequency f, G(x,f)—gain, AR(x,f)—axial ratio, A(x)—antenna size (calculated as footprint area covered by the antenna substrate). The definitions of the above figures of interest can be found in any antenna engineering textbook (e.g., [91,92]). The penalty functions included in Table 1 measure relative constraint violations. The power factor  $[]^2$ is used to ensure smoothness of objective function with regard to constraint violation at the boundary of the feasible region. This is vital, as many constraints are active at the optimum solution.

In this work, we are interested in multi-band antennas, parameter tuning of which is a representative multimodal problem that may require global optimization. This is because starting a local search from the design corresponding to allocation of operational frequencies being away from the targets usually leads to a failure. Let  $f_{0k}$ , k = 1, ..., N, be the intended operating frequencies of the N-band antenna, and  $B_k$  represent the target fractional bandwidth across which the reflection coefficient  $|S_{11}|$  should be minimized. Normally, a worst-case scenario is considered, i.e., we target minimizing the maximum  $|S_{11}|$  within all operating bands, with the level of -10 dB typically considered sufficient for most practical applications. Thus, the minimax objective function can be defined as:

$$U(\mathbf{x}) = \max \Big\{ f \in \bigcup_{k=1}^{N} [(1 - B_k/2) f_{0k}, (1 + B_k/2) f_{0k}] : \Big| S_{11}(\mathbf{x}, f) \Big| \Big\}, \tag{4}$$

Note that Equation (4) coincides with the objective function presented in the first row of Table 1 for  $F = [(1 - 0.5B_1)f_{0.1}, (1 + 0.5B_1)f_{0.1}] \cup ... \cup [(1 - 0.5B_N)f_{0.N}, (1 + 0.5B_N)f_{0.N}].$ In some cases, the fractional bandwidths may be identical, i.e.,  $B_1 = ... = B_N = B$ , or we may have  $B_k = 0$  for k = 1, ..., N, meaning that we aim at minimization of the maximum reflection exactly at all operational frequencies  $f_{0,k}$ .

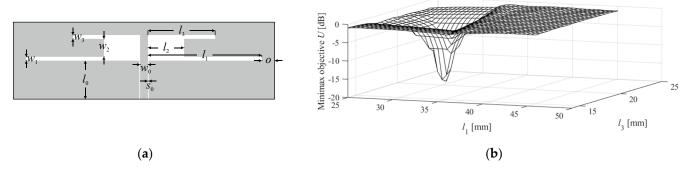
## 2.2. Knowledge-Based Plateau Elimination Using Response Features

Objective functions defined using conventional formulations (including minimax, as outlined in Section 2.1) are often highly nonlinear, which makes them challenging to handle by optimization algorithms. In the case of nature-inspired or other types of global procedures, this translates into difficulties in finding the conducive regions of the parameter space. Figure 1a shows a representative example of a dual-band antenna designed to allocate its operating frequencies at 3.0 GHz (lower band) and 5.3 GHz (upper band), and to minimize the reflection coefficient therein. The objective function is expressed as in Equation (4), with  $f_{0.1} = 3.0$  GHz,  $f_{0.2} = 5.3$  GHz, and  $B_1 = B_2 = 0$ . The antenna is described by six geometry parameters  $x = [l_1 \ l_2 \ l_3 \ w_1 \ w_2 \ w_3]^T$ . Figure 1b shows the objective function profile for  $24 \le l_1 \le 46$  and  $15 \le l_3 \le 24$  with other parameters fixed. It can be noticed that the majority of the graph is a plateau, with only a small region in the vicinity of the optimum associated with large changes of the merit function value. The rationale is that shifting the operating frequencies from the targets results in the maximum reflection being close to zero dB, the latter determining the value of U(x). From the point of view of any optimization algorithm, the plateau regions are difficult to handle due to vanishing gradients (for local methods) or problems in discriminating between the regions of different qualities (for global techniques). It should also be emphasized that the three-dimensional illustration of Figure 1b does not represent the actual level of difficulty: the relative amount



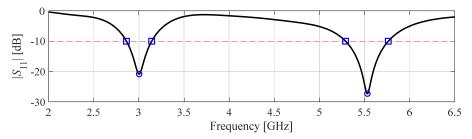
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of 'flat' objective function regions in the multi-dimensional design space is considerably larger than shown in the picture.



**Figure 1.** Conventional design optimization task formulation in the context of global search: (a) exemplary dual-band dipole antenna described by six geometry parameters, optimized for minimum reflection at the operating frequencies 3.0 GHz and 5.3 GHz; (b) objective function landscape with respect to geometry parameters  $l_1$  and  $l_3$  (remaining parameters fixed); note large plateaus, which make the optimization process challenging.

A workaround to these issues, as proposed in this work, is the exploitation of response feature technology. Response features were originally introduced to facilitate local (gradient-based) optimization procedures of antenna structures [82]. The main idea is to express the design task in terms of appropriately defined specific (or feature) points of the system outputs. A particular choice of the feature points, e.g., frequency/level coordinates of antenna resonances, frequencies of specific levels (typically, -10 dB) of antenna reflection, etc., depends on the design specifications [84], cf. Figure 2. As the functional dependence of the characteristic points on antenna dimensions is normally less nonlinear than a similar dependence for the complete outputs, feature-based formulations—due to exploiting the problem-specific knowledge—lead to a faster convergence of optimization procedures [85], or allow for reducing the training data set sizes when constructing data-driven surrogate models [93].



**Figure 2.** Response features for a dual-band antenna: reflection response (—), characteristic locations associated with antenna resonances (o), characteristic locations of -10 dB level of  $|S_{11}|$  ( $\square$ ). The dashed line represents the acceptance limit for antenna reflection.

In this work, the purpose of incorporating response features is to eliminate the objective function plateaus as discussed above. Let  $P(x) = [p_1(x) \dots p_K(x)]$  represent a vector whose entries are K response features selected for a given antenna structure, where  $p_k(x) = [f_k(x) \ l_k(x)]$ ;  $f_k$  and  $l_k$  are the frequency and level coordinates of the kth feature point. If multi-band antenna is optimized in the sense of Equation (4) with  $B_k = 0$  for  $k = 1, \dots, N$  (i.e., minimization of antenna reflection at all operating frequencies), the appropriate selection of the feature points would be the points corresponding to antenna resonances.



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> Then we have K = N with  $f_k$  being the kth resonant frequency and  $l_k$  being the value of  $|S_{11}|$  at  $f_k$ . The feature-based merit function  $U_F$  may be then formulated as:

$$U_F(\mathbf{P}(\mathbf{x})) = \max\{1 \le k \le N: l_k(\mathbf{x})\} + \beta \left\| \begin{bmatrix} f_{0.1} \\ \vdots \\ f_{0.N} \end{bmatrix} - \begin{bmatrix} f_1(\mathbf{x}) \\ \vdots \\ f_N(\mathbf{x}) \end{bmatrix} \right\|^2$$
 (5)

where  $\beta$  is the proportionality coefficient. Note that the first term of Equation (5) represents the maximum reflection over all resonant frequencies, whereas the second one can be considered a penalty term that enforces relocation of the resonances to the target values  $f_{0,k}$ , k = 1, ..., N. Furthermore, the minimum of U(x) and  $U_F(x)$  coincide assuming that the target operating frequencies are attainable, and the coefficient  $\beta$  is sufficiently large.

The formulation (5) can be generalized to non-zero  $B_k$  by including additional feature points corresponding to the frequencies  $(1 - B_k/2)f_k$  and  $(1 + B_k/2)f_k$ . Moreover, featurebased formulation allows for convenient handling of bandwidth enhancement tasks by using characteristic points representing -10 dB levels of antenna reflection (cf. Figure 2).

Figure 3 shows the functional landscape of the objective function  $U_F$  of (5) for the dual-band antenna shown in Figure 1a. The graph is constructed under the same conditions as in Figure 1b, i.e., with respect to parameters  $l_1$  and  $l_3$  over the same ranges thereof, and the remaining parameters fixed at the same values as in Figure 1b. Observe that the plateau regions are not present, and the objective function minimum is easily reachable from any combination of  $l_1$  and  $l_3$ , at least in the considered parameter range. In particular, it is expected that reformulating the design task through response features will also facilitate and expedite nature-inspired optimization. This is because steady trend (monotonicity) of the objective function  $U_F$  fosters relocation of individuals in the population towards the global minimum, whereas standard formulation does not exhibit this behavior when away from the optimum.

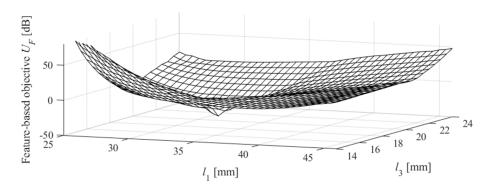
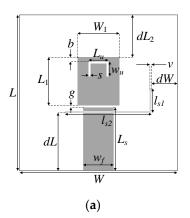


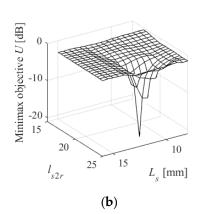
Figure 3. The landscape of the feature-based merit function (5) for the dual-band dipole antenna shown in Figure 1a. The function is assessed over the same ranges of antenna dimensions  $l_1$  and  $l_3$  as in Figure 1b. As the feature-based formulation takes into account the misalignment of the antenna operating frequencies from the target, the plateaus visible in Figure 1b are essentially removed.

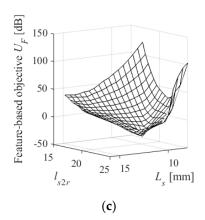
Figure 4 shows an example of a triple-band antenna along with the landscapes characteristic to the minimax and feature-based objective functions plotted over two-dimensional subspace spanned by parameters  $L_s$  and  $l_{s2r}$ . It can be observed that the qualitative difference between the minimax and feature-based merit function is similar to that of dual-band antenna of Figure 1. In particular, the minimax objective function landscape is flat with a sharp minimum corresponding to the design with good alignment of the antenna operational frequencies to the target, whereas the feature-based function shows clear trends in the entire region, which facilitates the optimization process. Also, for this example, the issues pertinent to the minimax objective are more pronounced due to the increased number of operating bands (three versus two for the antenna of Figure 1a).



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**Figure 4.** Triple-band antenna and objective function landscapes over two-dimensional subspace of parameters  $L_s$  and  $l_{s2r}$  (the latter controlling the parameter  $l_{s2} = l_{s2r}(W - dW)$ ); target operational frequencies are 3.5 GHz, 5.8 GHz, and 7.5 GHz: (a) antenna geometry; (b) landscape of the minimax merit function (4); (c) landscape of the feature-based objective function (5).

## 2.3. Particle Swarm Optimization with Response Features

In this work, particle swarm optimizer (PSO) [94,95] is utilized as the underlying optimization engine. PSO was chosen as one of the most widely employed nature-inspired population-based algorithms with applications in various fields of engineering, including electrical engineering (e.g., [96–99]). PSO handles a population (swarm) comprising N parameter vectors (particles), and each particle is characterized by its position vector  $x_i$  as well as velocity vector  $v_i$ . The updating of velocity and position occurs through the following process:

$$\mathbf{v}_i \leftarrow \chi[\mathbf{v}_i + c_1 \mathbf{r}_1 \bullet (\mathbf{x}_i^* - \mathbf{x}_i) + c_2 \mathbf{r}_2 \bullet (\mathbf{g} - \mathbf{x}_i)]$$
 (6)

$$\mathbf{x}_i \leftarrow \mathbf{x}_i + \mathbf{v}_i \tag{7}$$

where  $r_1$  and  $r_2$  refer to the vectors comprising uniformly distributed random numbers from the range 0–1, and the symbol  $\bullet$  denotes component-wise multiplication;  $x_i^*$  denotes the personal best, i.e., the best design identified for the ith particle in the course of the optimization run until the current iteration. It should be noted that in numerical experiments, a standard setup of PSO algorithm parameters is employed. This is to avoid unnecessary over-tuning of the optimization routine with regard to a specific optimization task that is being solved, and to demonstrate that standard parameter setting is sufficient. The following setup is utilized: swarm size N=10, maximum number of iterations  $k_{\text{max}}=100$ , and the remaining parameters  $\chi=0.73$ ,  $c_1=c_2=2.05$ , cf. [100].

The first step of modifying of the positions  $x_i$  of the particles consists of the partially stochastic adjustment of the velocity vector (see Equation (6)). Three factors affect the aforementioned process: the first involves current velocity, the second facilitates particle shift towards its (local) best position  $x_i^*$ , and the third propels the particle towards global best position g discovered by the swarm thus far.

In the context of nature-inspired optimization, the replacement of the conventional formulation of an antenna design task by its feature-based version (cf. Section 2.2) leaves the optimization algorithm intact; it is only the objective function that is altered in accordance with the assumed selection of the characteristic points. In this work, we use particle swarm optimizer (PSO) [101] as a widely-used nature-inspired algorithm to illustrate the potential benefits of problem reformulation. Section 3 provides comprehensive verification and benchmarking that involve three multi-band antenna structures. We illustrate the advantages of a feature-based approach using the simplified case of a dual-band antenna of Figure 1, reduced to a two-dimensional case (variables  $l_1$  and  $l_3$ ), which allows for a convenient visualization of the optimization process, including relocation of the swarm.



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> Figure 5 presents a comparison of the PSO algorithm optimizing the minimax objective function  $U_r$ , and the feature-based function  $U_F$ . It should be noted that even for this simplistic setup, the advantages of feature-based formulation are clearly pronounced. On the one hand, optimization of  $U_F$  leads to a faster convergence, which is indicated by a tighter arrangement of the swarm throughout the iterations (Figure 5a,b). On the other hand, the feature-based formulation reaches a better-quality solution earlier. This means that faster convergence is not a premature one; in other words, it is not detrimental to the efficacy of the optimization process. The explanation is that optimization of  $U_F$  capitalizes on strong trends (monotonicity) of this objective function over large portions of the objective space, as opposed to the presence of the flat regions pertinent to the minimax objective function *U* (cf. Figure 1b or Figure 4b).

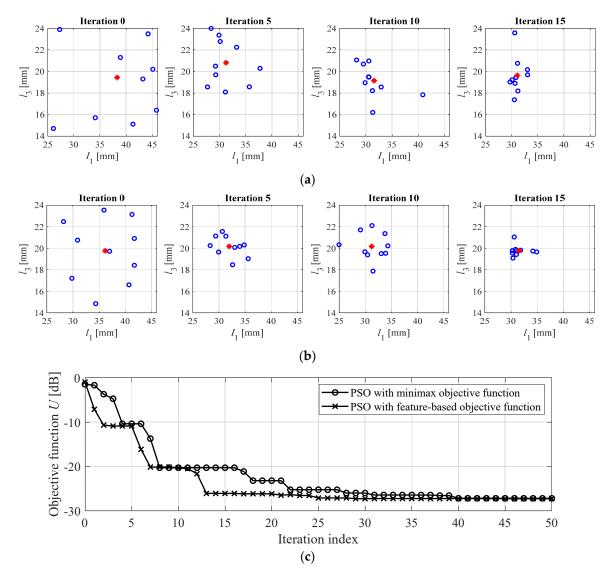


Figure 5. Nature-inspired optimization of dual-band antenna restricted to a two-dimensional subspace spanned by parameters  $l_1$  and  $l_3$  (cf. Figure 1a). Optimization carried out with the use of the standard PSO algorithm with swarm size equal ten. Shown is the allocation of the swarm (o) as well as the center of gravity of the swarm (\*) at selected iterations: (a) minimax objective function *U*; (b) feature-based objective function  $U_F$ ; (c) convergence plots for the algorithm with minimax (o) and feature-based objective function (×). Note that utilization of the feature-based merit function leads to a faster convergence of the algorithm, which is not detrimental to the design quality because of monotonicity of  $U_F$  (cf. Figure 3 vs. Figure 1b, see also Figure 4).

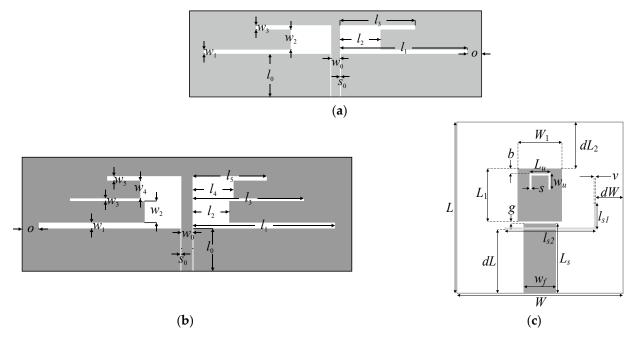


#### 3. Verification Studies

This section comprehensively verifies potential advantages of feature-based formulation for population-based optimization of antenna structures. We consider three multi-band antennas, including a dual-band uniplanar antenna, as well as two triple-band antennas. The particle swarm optimization (PSO) algorithm is utilized as an optimization engine, being a representative and widely used nature-inspired procedure. The primary question is whether a feature-based approach yields computational benefits, either with regard to improving the design quality (for a given computational cost of the design procedure) or accelerating convergence over the standard (here, minimax) formulation of the design task. Numerical experiments conducted in this section purposely assume limited computational budget so that the cost of nature-inspired optimization can be made practically acceptable. All considered optimization procedures, i.e., the proposed one using the feature-based formulation of the optimization task, as well as the benchmark routines, including PSO and gradient-based algorithm [102] (both employing standard (minimax) formulation of the optimization task) were executed ten times, and the statistical results are presented. Specifically, we are interested in the average objective function value, along with its standard deviation (to quantify the solutions' repeatability).

### 3.1. Verification Antennas

Numerical verification of the relevance of feature-based re-formulation described in Section 2 is executed using the following microstrip antenna structures: (i) Antenna I: a dual-band uniplanar dipole antenna [103] presented in Figure 6a, (ii) Antenna II: a triple-band uniplanar dipole antenna [93] shown in Figure 6b, along with (iii) Antenna III: a triple band U-slotted patch featuring L-slot defected ground structure (DGS) [104] presented in Figure 6c. Note that Antennas I and III have been already considered as illustration examples in Section 2; however, they are shown again in Figure 6 to make this section self-contained. Futhermore, Figure 7 illustrates computational mesh and 3D radiation patterns at the target operating frequencies of selected designs for all antenna verification structures.



**Figure 6.** Antenna structures used as verification examples: (a) Antenna I [103]; (b) Antenna II [93]; (c) Antenna III [104]; the ground-plane slot is indicated using light-grey shading.



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> The important data concerning these antennas can be found in Table 2. These data include substrate parameters (height, relative dielectric permittivity), vectors of designable parameters, target operating frequencies, as well as the search spaces, delimited by the lower bound l and the upper bounds u on the geometry parameters. Observe that the parameter ranges are broad: the average ratio of the upper and lower bounds is 2.5, 5.0, and 1.5 for Antennas I through III, respectively. In fact, the antenna structures employed in this work for verifying the proposed framework are challenging when compared to the verification case structures utilized for validating global simulation-driven design optimization algorithms reported in the literature [94,105–111]. This pertains to both the number of the designable variables (six, ten, and eleven geometry parameters for Antenna I through III), as well as their ranges. The juxtaposition of the optimization frameworks and the case studies used therein is provided in Table 3.

Table 2. Verification case studies.

		Case Study	
	Antenna I	Antenna II	Antenna III
Substrate	$\varepsilon_r = 3.5, h = 0.76 \text{ mm}$ metallization thickness $t = 17.5 \mu\text{m}$	$\varepsilon_r = 3.5, h = 0.76 \text{ mm}$ $t = 17.5  \mu\text{m}$	$\varepsilon_r = 3.2, h = 3.1 \text{ mm}$ $t = 17.5  \mu\text{m}$
Designable parameters	$x = [l_1 \ l_2 \ l_3 \ w_1 \ w_2 \ w_3]^T$	$x = [l_1 \ l_2 \ l_3 \ l_4 \ l_5  w_1 \ w_2 \ w_3 \ w_4 \ w_5]^T$	$x = [L_1 L_s L_u W W_1 dL  dW g l_{s1} l_{s2} w_u]^T$
Other parameters	$l_0 = 30, w_0 = 3,$ $s_0 = 0.15, o = 5$	$l_0 = 30, w_0 = 3,$ $s_0 = 0.15, o = 5$	$b = 1, w_f = 7.4, s = 0.5,$ $w = 0.5, dL_2 = L_1,$ $L = L_s + g + L_1 + dL_2$
Target operating frequencies	3.0 GHz and 5.5 GHz	2.45 GHz, 3.6 GHz, and 5.3 GHz	3.5 GHz, 5.8 GHz, and 7.5 GHz
Parameter space	$l = [25 5 0.5 0.5 1.8 0.5]^{T}$ $u = [50 10 1.0 1.5 3.0 2.0]^{T}$	$l = [20 5 15 5 12 0.2 1.0 0.2$ $1.0 0.1]^{T}$ $u = [50 15 35 16 25 1.5 3.0$ $1.5 3.0 1.5]^{T}$	$l = [10 17 5 45 8 15 9 0.2 4$ $20 2]^{T}$ $u = [16 25 8 55 12 20 12 0.4$ $6 24 3]^{T}$

Table 3. Juxtaposition of the verification examples used by the state-of-the art works concerning global simulation-driven design optimization of antennas.

Technique	Optimization Algorithm	Test Case	Number of Design Variables	Average Upper-to-Lower Bound Ratios
[105]	Bayesian optimization	Dual-band antenna	3	1.7
	•	Monopole antenna	8	3.3
	Clabal	Wideband antenna	9	6.1
[106]	Global trust-region parallel Bayesian	Circular patch antenna	4	1.3
		U-slot antenna array	12	2.0
[107]	Hybrid bacterial foraging-PSO	Fractal antenna	3	4.5
[108]	Chameleon swarm algorithm	U-slot quad-band antenna	12	1.5
[109]	Ü	Single-band MIMO antenna	4	3.0
	Binary PSO	Dual-band MIMO antenna	3	3.3



Table 3. Cont.

Technique	Optimization Algorithm	Test Case	Number of Design Variables	Average Upper-to-Lower Bound Ratios
[110]	Brain storm optimization	Yagi-Uda antenna	11	1.9
	•	Dual-band antenna	6	2.5
This work	PSO with response	Triple-band antenna	10	5.0
	features	Triple band U-slotted patch antenna	11	1.5

It should be emphasized that the developed methodology is not aimed at solving design tasks for any specific application area. In particular, it may be successfully applied to globally optimize antennas that are intended to be integrated with smart technologies and implemented in IoT devices. The presented test cases incorporate multi-band antenna structures, which are widely employed in a broad range of wireless communication applications. Optimization of input characteristics, as considered here, constitutes the most common type of antenna optimization tasks.

The simulation models of all antennas are calculated using transient solver of CST Microwave Studio, which utilizes the Finite Integration Technique (FIT) [111] for antenna evaluations. The goal has been formulated as a reflection minimization at the target operating frequencies. The minimax objective functions are defined as in Equation (4), with  $B_k = 0$ , whereas the feature-based merit functions follow Equation (5), cf. Section 2.2.

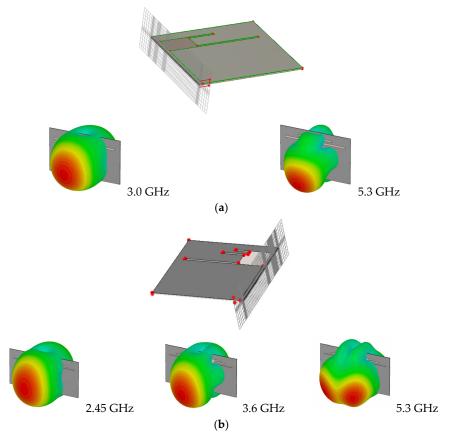
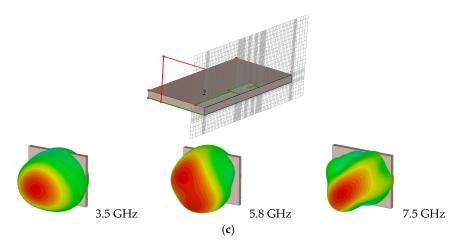


Figure 7. Cont.





**Figure 7.** Illustration of the computational mesh (time-domain solver of CST Microwave Studio) and 3D radiation patterns at the target operating frequencies (cf. Table 2) of selected designs optimized for these frequencies: (a) Antenna I, (b) Antenna II, (c) Antenna III. For all structures, hexahedral mesh is employed, and the underlying simulation procedure is the Finite Integration Technique (FIT) [111].

## 3.2. Results

The numerical results have been gathered in Tables 4–6 for Antennas I, II, and III, respectively. Figure 8 shows the evolution of the objective function, averaged over all performed runs of the respective algorithms. Furthermore, Figures 9–11 show antenna characteristics at the final designs rendered in the chosen runs of the PSO optimizer using the feature-based problem formulation. The final optimal geometry parameter vectors for the designs shown in Figures 9–11 are gathered in Table 7. The figures of interest are the average merit function values and their standard deviations. The latter is used as a measure of solution repeatability.

**Table 4.** Antenna I: Optimization results.

Algorithm	Number of Iterations	Problem Formulation	Average Objective Function Value [dB] $CI^{\$}$ [dB]	Standard Deviation of Objective Function [dB]	Cost
			-19.0 [-23.1, -14.9]	2.5	
PSO	20	Feature- based (this work)	-20.6 [-25.0, -16.2]		200
150		Standard (minimax)	-26.8 [-33.0, -20.6]	3.8	
	50		$ \begin{array}{c} -26.5 \\ [-32.6, -20.4] \end{array} $ 3.7		500
Gradient- based	_	Standard (minimax)	-13.5 [-21.4, -5.6]	4.8	84.2

<sup>\$</sup> CI—90 percent confidence interval.



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 $\textbf{Table 5.} \ \, \textbf{Antenna II: Optimization results.}$ 

Algorithm	Number of Iterations	Problem Formulation	Average Objective Function Value [dB] CI <sup>\$</sup> [dB]	Standard Deviation of Objective Function [dB]	Cost	
		Standard (minimax)	-10.9 [-17.3, -4.5]			
PSO —	20	Feature- based (this work)	based $-12.8$ $[-19.3, -6.2]$ 4.0		200	
150		Standard (minimax)	-14.1 [-22.3, -5.9]	5.0		
50		Feature- based (this work)	-17.2 [-22.4, -12.0]	3.2	500	
Gradient- based	_	Standard (minimax)	-7.8 [-16.3, -0.7]	5.2	105.8	

<sup>\$</sup> CI—90 percent confidence interval.

Table 6. Antenna III: Optimization results.

Algorithm	Number of Problem Iterations Formulati		Average Objective Function Value [dB] CI <sup>\$</sup> [dB]	Standard Deviation of Objective Function [dB]	Cost
		Standard (minimax)	-14.4 [-21.6, -7.2]	4.4	
PSO	20	Feature- based (this work)	-16.4 [-20.5, -12.3]	2.5	200
150		Standard (minimax)	-19.4 [-30.9, -7.9]	7.0	
50		Feature- based (this work)	-20.7 [-25.8, -15.6]	3.1	500
Gradient- based	-	Standard (minimax)	-12.1 [-20.3, -3.9]	5.0	125.4

<sup>\$</sup> CI—90 percent confidence interval.

**Table 7.** Final optimal parameter vectors of Antennas I through III (shown in Figures 9–11).

Antenna		I				II				III	
		Design				Design				Design	-
Parameter	1	2	3	Parameter	1	2	3	Parameter	1	2	3
$l_1$	28.5369	28.2285	29.0147	$l_1$	37.9823	36.1606	35.6987	$L_1$	12.2576	11.3321	11.1938
$l_2$	5.0000	8.0000	5.6175	$l_2$	15.0000	11.8375	10.7800	$L_s$	17.0000	17.0000	19.4227
$l_3$	0.5262	0.6189	0.5314	$l_3^-$	29.4173	20.0000	26.6328	$L_u$	7.5690	7.4518	8.0000
$w_1$	1.5000	0.5000	1.4373	$l_4$	16.0000	9.9495	12.8472	W	50.6422	52.6515	55.0000
$w_2$	1.8000	2.7000	2.0245	$l_5$	23.6288	25.0000	21.1045	$W_1$	10.2412	11.0431	12.0000
$w_3$	1.3030	1.0133	1.0733	$w_1$	0.5000	0.9097	0.9973	dL	20.0000	17.0565	20.0000
				$w_2$	1.4692	2.0000	1.0905	dW	11.0485	10.4042	11.2354
				$\overline{w_3}$	1.0000	1.0000	0.5059	g	0.2424	0.4000	0.2000
				$w_4$	1.0000	1.0000	1.8633	$l_{s1}$	5.8355	5.0185	4.9634
				$w_5$	1.0000	0.5000	0.5000	$l_{s2}$	20.7977	23.1403	22.8999
				,				$w_u$	2.9078	2.0000	2.0000



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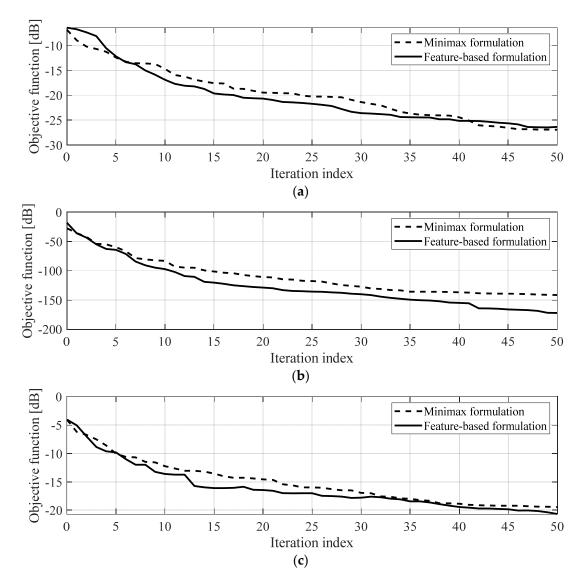


Figure 8. Objective function versus iteration index for minimax and feature-based formulations: (a) Antenna I; (b) Antenna II; (c) Antenna III. The merit function is averaged across the ten algorithm runs performed for each antenna structure.

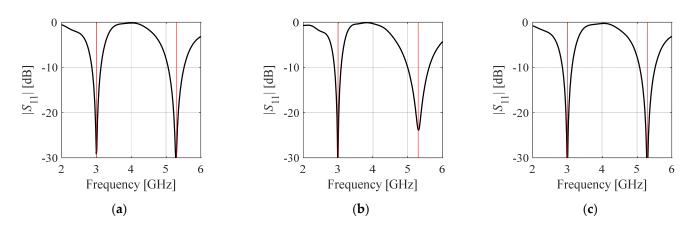
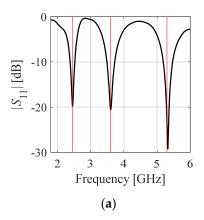
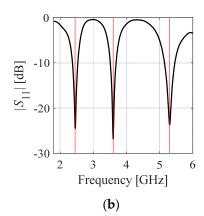
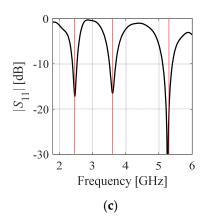


Figure 9. Reflection responses of Antenna I for designs obtained with PSO using feature-based formulation of the optimization problem. Shown are the results generated in the chosen executions of the algorithm: (a) design 1; (b) design 2; (c) design 3. The vertical lines indicate the target operational frequencies.

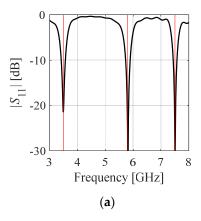


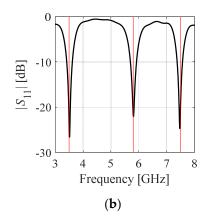


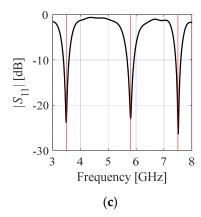




**Figure 10.** Reflection responses of Antenna II for designs obtained with PSO using feature-based formulation of the optimization problem. Shown are the results generated in the chosen executions of the algorithm: (a) design 1; (b) design 2; (c) design 3. The vertical lines indicate the target operational frequencies.







**Figure 11.** Reflection responses of Antenna III for designs obtained with PSO using feature-based formulation of the optimization problem. Shown are the results generated in the chosen executions of the algorithm: (a) design 1; (b) design 2; (c) design 3. The vertical lines indicate the target operational frequencies.

## 3.3. Discussion

The results shown in Tables 4–6 prove the advantages of feature-based formulation of the design task when applied to a global optimization of multi-band antenna structures. It can be noted that the average objective function is noticeably better for the feature-based approach after 20 iterations of the PSO algorithm. This is the case for all antenna structures considered in this study. After 50 iterations, the feature-based formulation yields better results for Antennas II and III, which are more challenging cases, both with regard to the design space dimensionality as well as the number of operating bands of the device. For Antenna I, both approaches render similar design qualities. At the same time, it can be noticed that the results' repeatability (measured by the standard deviation of the results) is considerably better for feature-based formulations for Antennas II and III, which also indicates the advantages of the considered approach from the standpoint of design reliability.

Finally, utilization of response features allows for achieving noticeable computational speedup. For example, the number of iterations necessary to obtain the same average objective function levels as those produced by the feature-based formulation in 20 iterations, is about 30. The corresponding average speedup is therefore over 30 percent.

Let us also emphasize that—as mentioned before—the PSO algorithm was intentionally set up with a limited computational budget, which is to make the optimization costs



reasonably low from the practical perspective. Although extending the optimization run beyond 50 iterations would likely lead to reducing the quality differences between the minimax and feature-based formulations, the primary objective of this work is to show that the latter brings in definite benefits under a tight CPU budget.

The presented results also demonstrate superiority of the performance of the proposed optimization procedure utilizing feature-based formulation of the design task over a local trust-region (TR) gradient-based algorithm. For each considered antenna structure, the average objective function value is significantly worse in the case of the TR routine than for the PSO algorithm (both using standard and feature-based formulation of the objective function). This is because the success rate of a TR algorithm is poor for all antennas: it equals 6/10 for Antenna I (meaning that the design specifications have been met in only six out of ten algorithm runs), and it is 4/10 for Antennas II and III. This clearly worsens solution repeatability for the local routine, which equals 5.0 (on average across all benchmark antenna sets), as compared to 3.3 (on average) for our algorithm with a higher computational budget.

The limitations of the proposed approach are twofold. Firstly, our algorithm solves the antenna design optimization task directly, i.e., no surrogate model is involved whatsoever. The employment of the feature-based formulation of the design task allows for slightly accelerating the process. Nevertheless, in the cases where the antenna simulation model is costly, the overall optimization expenses may be impractically high. Thus, the designer may need to default to the usage of machine-learning-based procedures. The second type of limitation stems from the fact the developed framework utilizes feature-based formulation of the design task. Thus, its employment is limited to the cases where easily identifiable characteristic points may be distinguished in the antenna frequency characteristics which enable encoding design specifications. Overall, the developed algorithm might not be as flexible as other frameworks that do not place any restrictions on the antenna response structure.

#### 4. Conclusions

In this paper, we investigated potential benefits of incorporating feature-based formulation of design tasks when applied to nature-inspired optimization of antenna structures. The studies were focused on input characteristics of multi-band antennas, handling of which is representative in terms of the level of difficulty, and a multimodal nature of the problem. On the conceptual level, it has been demonstrated that problem reformulation, from the conventional (minimax) setup to that employing response features, significantly alters the functional landscape that needs to be tackled in the optimization process. These changes suggested that improved performance of the nature-inspired search processes may be expected. This was corroborated to the fullest extent through comprehensive numerical experiments conducted for three microstrip antennas, using a particle swarm optimizer as the algorithm of choice. In order to maintain the optimization expenses at practically acceptable levels, the computational budget was significantly restricted to only 500 objective function evaluations, with the intermediate results verified after 200 evaluations. The major findings are that exploiting problem-relevant knowledge in the form of response features to solve the considered antenna design optimization tasks noticeably improves both the quality of designs rendered by the algorithm and the overall reliability of the search process, as indicated by the lower values of standard deviation estimated from multiple independent algorithm runs. Future work will focus on the development of computationally-efficient, nature-inspired antenna optimization procedures involving both the response feature approach and other acceleration mechanisms, e.g., variable-resolution simulation models.



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